Planning Introduction

Explicit State-Space Search Symmetry reduction Partial Order Reduction Heuristics Planning with SAT Parallel plans Plan search SAT solving Symbolic search Algorithms Operations ∃/∀-abstraction Images Normal forms Planning System Implementations Algorithm portfolios **Evaluation of Planners Timed Systems** Models Explicit state-space Constraint-based methods Continuous change

Search Methods for Classical and Temporal Planning



Planning

What to do to achieve your objectives?

Which actions to take to achieve your objectives?

- Number of agents
 - single agent, perfect information: s-t-reachability in succinct graphs
 - + nondeterminism/adversary: and-or tree search
 - + partial observability: and-or search in the space of beliefs

Time

- asynchronous or instantaneous actions (integer time, unit duration)
- rational/real time, concurrency

Objective

- Reach a goal state.
- Maximize probability of reaching a goal state.
- Maximize (expected) rewards.
- temporal goals (e.g. LTL)

Hierarchy of Planning Problems



Classical (Deterministic, Sequential) Planning

- states and actions expressed in terms of state variables
- single initial state, that is known
- ► all actions deterministic
- actions taken sequentially, one at a time
- ► a goal state (expressed as a formula) reached in the end

Deciding whether a plan exists is PSPACE-complete [GW83, Loz88, LB90, Byl94]. With a polynomial bound on plan length, NP-complete [KS96].

Domain-Independent Planning

What is domain-independent?

- general language for representing problems (e.g. PDDL)
- general algorithms to solve problems expressed in it

Advantages and disadvantages:

- + Representation of problems at a high level
- + Fast prototyping
- + Often easy to modify and extend
- Often very high performance penalty w.r.t. specialized algorithms
- Trade-off between generality and efficiency



What is domain-specific?

- application-specific representation
- application-specific constraints/propagators
- application-specific heuristics

There are some planning systems that have aspects of these, but mostly this means: implement everything from scratch.



Introduction

Introduction

Related Problems, Reductions

planning, diagnosis [SSL+95], model-checking (verification)



PDDL: Planning Domain Description Language

Introduction

- ► Defined in 1998 [GHK⁺98], with several extensions later.
- Lisp-style syntax
- Widely used in the planning (competition) community.
- Most basic version with Boolean state variables only.
- Action sets expressed as schemata instantiated with objects.

(:action unload

:parameters (?obj - obj ?airplane - vehicle ?loc - location)
:precondition (and (in ?obj ?airplane) (at ?airplane ?loc))
:effect (and (not (in ?obj ?airplane))))

How to Represent Planning Problems?



9/128 Different strengths and weaknesses; No single "right" language.

States

States are valuations of state variables.

One state is LOCATION =312	
GEAR = 4	
FUEL = 58	
SPEED =110	
DIRECTION = 90	
	One state is LOCATION =312 GEAR = 4 FUEL = 58 SPEED =110 DIRECTION = 90

State-space transition graphs





Actions How values of state variables change

General form

precondition: A=1 \land C=1 effect: A := 0; B := 1; C := 0;

STRIPS representation

PRE: A, C ADD: B DEL: A, C



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Weaknesses in Existing Languages

High-level concepts not easily/efficiently expressible.
 Examples: graph connectivity, transitive closure, inductive definitions.

Introduction

- Limited or no facilities to express domain-specific information (control, pruning, heuristics).
- The notion of classical planning is limited:
 - Real world rarely a single run of the sense-plan-act cycle.
 - Main issue often uncertainty, costs, or both.
 - Often rational time and concurrency are critical.

Formalization of Planning in This Tutorial

A problem instance in (classical) planning consists of the following.

Introduction

- ▶ set *X* of state variables
- set A of actions $\langle p, e \rangle$ where
 - p is the precondition (a set of literals over X)
 - e is the effects (a set of literals over X)
- initial state $I: X \to \{0, 1\}$ (a valuation of X)
- ▶ goals G (a set of literals over X)

(We will later extend this with time and continuous change.)

Introduction

Introduction

The planning problem

Development of state-space search methods



- The most basic search method for transition systems
- Very efficient for small state spaces (1 million states)
- Easy to implement
- Very well understood
- Also known as "forward search" (in contrast to "backward search" with regression [Rin08])
- Pruning methods:
 - symmetry reduction [Sta91, ES96]
 - partial-order reduction [God91, Val91]
 - Iower-bounds / heuristics, for informed search [HNR68]

Every state represented explicitly \Rightarrow compact state representation important

- Boolean (0, 1) state variables represented by one bit
- Inter-variable dependencies enable further compaction:
 - ¬(at(A,L1)∧at(A,L2)) always true
 - automatic recognition of invariants [BF97, Rin98, Rin08]
 - *n* exclusive variables x_1, \ldots, x_n represented by $1 + \lfloor \log_2(n-1) \rfloor$ bits

(See [GV03] for references to representative works on compact representations of state sets.)

Search Algorithms

Symmetry Reduction [Sta91, ES96]

- uninformed/blind search: depth-first, breadth-first, ...
- informed search: "best first" search (always expand best state so far)
- informed search: local search algorithms such as simulated annealing, tabu search and others [KGJV83, DS90, Glo89] (little used in planning)
- optimal algorithms: A* [HNR68], IDA* [Kor85]

Idea

- 1. Define an equivalence relation \sim on the set of all states: $s_1 \sim s_2$ means that state s_1 is symmetric with s_2 .
- 2. Only one state s_C in each equivalence class $[s_C]$ needs to be considered.
- 3. If state $s \in [s_C]$ with $s \neq s_C$ is encountered, replace it with s_C .

Example

States $P(A) \land \neg P(B) \land P(C)$ and $\neg P(A) \land P(B) \land P(C)$ are symmetric because of the permutation $A \mapsto B, B \mapsto A, C \mapsto C$.

State-Space Search Symmetry reduction

Symmetry Reduction

Example: 11 states, 3 equivalence classes



State-Space Search Part. Order Red.

Partial Order Reduction

Stubborn sets and related methods

Idea [God91, Val91]

Independent actions unnecessary to consider in all orderings, e.g. A_1, A_2 and A_2, A_1 .

Example

Let there be lamps 1, 2, ..., n which can be turned on. There are no other actions. One can restrict to plans in which lamps are turned on in the ascending order: switching lamp n after lamp m > n unnecessary.¹

¹The same example is trivialized also by symmetry reduction!

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Heuristics for Classical Planning

Definition of h^{max} , h^+ and h^{relax}

The most basic heuristics used for non-optimal *domain-independent* planning:

h^{max}	[BG01, McD96]	best-known admissible heuristic
h^+	[BG01]	still state-of-the-art
1		

 h^{relax} [HN01] often more accurate but performs like h^+

 Basic insight: estimate distances between possible state variable values, not states themselves.

•
$$g_s(l) = \begin{cases} 0 & \text{if } s \models l \\ \min_a \text{ with effect } p(1 + g_s(\operatorname{prec}(a))) & \end{cases}$$

•
$$h^+$$
 defines $g_s(L) = \sum_{l \in L} g_s(l)$ for sets S.

TF

4

Distance of $A1 \wedge B1$ is 4.

TF

- h^{max} defines $g_s(L) = \max_{l \in L} g_s(l)$ for sets S.
- h^{relax} counts the number of actions in computation of h^{max} .

TF

TF

TF

TF

TF

TF



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- from 3 to 2: $T32 = \langle T3, \{T2, \neg T3\} \rangle$
- 2. Tractor pushes A:
 - from 2 to 1: $A21 = \langle T2 \land A2, \{T1, A1, \neg T2, \neg A2\} \rangle$
 - from 3 to 2: $A32 = \langle T3 \land A3, \{T2, A2, \neg T3, \neg A3\} \rangle$
- 3. Tractor pushes B:
 - from 2 to 1: $B21 = \langle T2 \land B2, \{T1, B1, \neg T2, \neg B2\} \rangle$
 - from 3 to 2: $B32 = \langle T3 \land B3, \{T2, B2, \neg T3, \neg B3\} \rangle$

TF

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h^{max} Underestimates

Computation of h^+

Tractor example

Example

Estimate for lamp1on \land lamp2on \land lamp3on with

 $\begin{array}{l} \langle \top, \{lamp1on\} \rangle \\ \langle \top, \{lamp2on\} \rangle \\ \langle \top, \{lamp3on\} \rangle \end{array}$

is 1. Actual shortest plan has length 3. By definition, $h^{max}(G_1 \wedge \cdots \wedge G_n)$ is the maximum of $h^{max}(G_1), \ldots, h^{max}(G_n)$. If goals are independent, the sum of the estimates is more accurate.

t	T1	T2	Т3	A1	A2	A3	B1	B2	B3
0	Т	F	F	F	F	Т	F	F	Т
1	TF	TF	F	F	F	Т	F	F	Т
2	TF	TF	TF	F	F	Т	F	F	Т
3	TF	TF	TF	F	TF	TF	F	TF	TF
4	TF	TF	TF	F	TF	TF	F	TF	TF
5	TF								

 $h^+(T2 \land A2)$ is 1+3. $h^+(A1)$ is 1+3+1 = 5 (h^{max} gives 4.)



- ► For the Tractor example:
 - actions in the shortest plan: 8
 - h^{max} yields 4 (never overestimates).
 - h⁺ yields 10 (may under or overestimate).
- The sum-heuristic and its various extensions, including relaxed plan heuristics [HN01, KHH12, KHD13] are used in practice for non-optimal planners.



YAHSP3 [Vid04, Vid11]

- LAMA [RW10] PROBE [LG11]
- LAMA adds a preference for actions suggested by the computation of heuristic as good "first actions" towards goals [Vid04, RH09].
- YAHSP2/YAHSP3 and PROBE do from each encountered state with a best-first search with h⁺ – incomplete local searches to find shortcuts towards the goals.

Performance of State-Space Search Planners

Planning Competition Problems 2008-2011



Planning with SAT

- Proposed by Kautz and Selman [KS92].
- Idea as in Cook's proof of NP-hardness of SAT [Coo71]: encode each step of a plan as a propositional formula.
- ► Intertranslatability of NP-complete problems ⇒ reductions to many other problems possible, often simple.



constraint satisfaction (CSP)	[vBC99, DK01]
NM logic programs / answer-set programs	[DNK97]
Mixed Integer Linear Programming (MILP)	[DG02]

Heuristics for Optimal Planning

Admissible heuristics are needed for finding optimal plans, e.g with A* [HNR68]. Scalability much poorer.

Pattern Databases [CS96, Ede00]

Abstract away many/most state variables, and use the length/cost of the optimal solution to the remaining problem as an estimate.

Generalized Abstraction (compose and abstract) [DFP09]

A generalization of pattern databases, allowing more complex aggregation of states (not just identification of ones agreeing on a subset of state variables.) Planning people call it "merge and shrink".

Landmark-cut [HD09] has worked well with standard benchmarks.

SAT

Transition relations in propositional logic

State variables are $X = \{a, b, c\}.$

 $\begin{array}{l} (\neg a \wedge b \wedge c \wedge \neg a' \wedge b' \wedge \neg c') \lor \\ (\neg a \wedge b \wedge \neg c \wedge a' \wedge b' \wedge \neg c') \lor \\ (\neg a \wedge \neg b \wedge c \wedge a' \wedge b' \wedge c') \lor \\ (a \wedge b \wedge c \wedge a' \wedge b' \wedge \neg c') \end{array}$

I he corresponding matrix	İS	
---------------------------	----	--

	000	001	010	011	100	101	110	111
000	0	0	0	0	0	0	0	0
001	0	0	0	0	0	0	0	1
010	0	0	0	0	0	0	1	0
011	0	0	1	0	0	0	0	0
100	0	0	0	0	0	0	0	0
101	0	0	0	0	0	0	0	0
110	0	0	0	0	0	0	0	0
111	0	0	0	0	0	0	1	0



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Encoding of Actions as Formulas

for Sequential Plans

Actions as propositional formulas

New value of state variable x_i is a function of the old values of x_1, \ldots, x_n : action $j = \text{conjunction of the precondition } P_j@t$ and

$$x_i@(t+1) \leftrightarrow F_i(x_1@t,\ldots,x_n@t)$$

for all $i \in \{1, \ldots, n\}$. Denote this by $E_j@t$.

Example (move-from-X-to-Y)

 $\overbrace{atX@t}^{\text{precond}} \land \overbrace{(atX@(t+1)\leftrightarrow\bot)\land(atY@(t+1)\leftrightarrow\top)}^{\text{effects}} \land (atX@(t+1)\leftrightarrow\bot)\land(atY@(t+1)\leftrightarrow\top) \land (atU@(t+1)\leftrightarrow atU@t)$

Choice between actions $1, \ldots, m$ expressed by the formula

$$\mathcal{R}@t = E_1@t \lor \cdots \lor E_m@t.$$

SAT Parallel plan

Parallel Plans: Motivation



- Don't represent the relative ordering of some consecutive actions.
- ► Reduced number of explicitly represented states ⇒ smaller formulas



Finding a Plan with SAT solvers

Let

- I be a formula expressing the initial state, and
- ► *G* be a formula expressing the goal states.

Then a plan of length T exists iff

$$I@0 \wedge \bigwedge_{t=0}^{T-1} \mathcal{R}@t \wedge G_T$$

SAT

is satisfiable.

Remark

Most SAT solvers require formulas to be in CNF. There are efficient transformations to achieve this [Tse68, JS05, MV07].

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SAT Parallel plans

Parallel plans (V-step plans)

Blum and Furst [BF97], Kautz and Selman 1996 [KS96]

Allow actions $a_1 = \langle p_1, e_1 \rangle$ and $a_2 = \langle p_2, e_2 \rangle$ in parallel whenever they don't interfere, i.e.

- ▶ both $p_1 \cup p_2$ and $e_1 \cup e_2$ are consistent, and
- ▶ both $e_1 \cup p_2$ and $e_2 \cup p_1$ are consistent.

Theorem

If $a_1 = \langle p_1, e_1 \rangle$ and $a_2 = \langle p_1, e_1 \rangle$ don't interfere and *s* is a state such that $s \models p_1$ and $s \models p_2$, then $exec_{a_1}(exec_{a_2}(s)) = exec_{a_2}(exec_{a_1}(s))$.

∀-step plans: encoding

Define $\mathcal{R}^{\forall}@t$ as the conjunction of

 $x@(t+1) \leftrightarrow ((x@t \wedge \neg a_1@t \wedge \dots \wedge \neg a_k@t) \vee a_1'@t \vee \dots \vee a_{k'}'@t)$

for all $x \in X$, where a_1, \ldots, a_k are all actions making x false, and $a'_1, \ldots, a'_{k'}$ are all actions making x true, and

 $a@t \rightarrow l@t$ for all l in the precondition of a,

and

 $\neg(a@t \land a'@t)$ for all a and a' that interfere.



∀-step plans: linear encoding Rintanen et al. 2006 [RHN06]

Action a with effect l disables all actions with precondition \overline{l} , except a itself. This is done in two parts: disable actions with higher index, disable actions with lower index.



This is needed for every literal.



Allow actions $\{a_1, \ldots, a_n\}$ in parallel if they can be executed in at least one order.

- $\triangleright \bigcup_{i=1}^{n} p_i$ is consistent.
- $\triangleright \bigcup_{i=1}^{n} e_i$ is consistent.
- There is a total ordering a_1, \ldots, a_n such that $e_i \cup p_i$ is consistent whenever i < j: disabling an action earlier in the ordering is allowed.

Several compact encodings exist [RHN06].

Fewer time steps are needed than with \forall -step plans. Sometimes only half as many.

Choose an arbitrary fixed ordering of all actions a_1, \ldots, a_n . Action a with effect l disables all later actions with precondition \overline{l} .



This is needed for every literal.

Disabling graphs Rintanen et al. 2006 [RHN06]

Summary of Notions of Plans

Define a disabling graph with actions as nodes and with an arc from a_1 to a_2 (a_1 disables a_2) if $p_1 \cup p_2$ and $e_1 \cup e_2$ are consistent and $e_1 \cup p_2$ is inconsistent.

The test for valid execution orderings can be limited to strongly connected components (SCC) of the disabling graph.

SAT

Plan search

In many structured problems all SCCs are singleton sets. \implies No tests for validity of orderings needed during SAT solving.

plan type	reference	comment
sequential	[KS92]	one action per time point
∀-parallel	[BF97, KS96]	parallel actions independent
∃-parallel	[DNK97, RHN06]	executable in at least one order

The last two expressible in terms of the relation disables restricted to applied actions:

- \blacktriangleright \forall -parallel plans: the disables relation is empty.
- ► ∃-parallel plans: the disables relation is acyclic.

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Search through Horizon Lengths

The planning problem is reduced to the satisfiability tests for

$$\begin{split} \Phi_0 &= I@0 \wedge G@0\\ \Phi_1 &= I@0 \wedge \mathcal{R}@0 \wedge G@1\\ \Phi_2 &= I@0 \wedge \mathcal{R}@0 \wedge \mathcal{R}@1 \wedge G@2\\ \Phi_3 &= I@0 \wedge \mathcal{R}@0 \wedge \mathcal{R}@1 \wedge \mathcal{R}@2 \wedge G@3\\ \vdots\\ \Phi_u &= I@0 \wedge \mathcal{R}@0 \wedge \mathcal{R}@1 \wedge \cdots \mathcal{R}@(u-1) \wedge G@u \end{split}$$

where u is the maximum possible plan length.

Q: How to schedule these satisfiability tests?

Search through Horizon Lengths

algorithm	reference	comment
sequential	[KS92, KS96]	slow, guarantees min. horizon
binary search	[SS07]	prerequisite: "tight" length UB
n processes	[Rin04b, Zar04]	fast, more memory needed
geometric	[Rin04b]	fast, more memory needed

SAT

Plan search

- sequential: first test Φ_0 , then Φ_1 , then Φ_2, \ldots
 - This is breadth-first search / iterative deepening.
 - Guarantees shortest horizon length, but is slow.
- parallel strategies: solve several horizon lengths simultaneously
 - depth-first flavor
 - usually much faster
 - no guarantee of minimal horizon length

Some runtime profiles





SAT SAT solving

Solving the SAT Problem

Geometric Evaluation

Example

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goal state



Problem solved almost without search:

- Formulas for lengths 1 to 4 shown unsatisfiable without any search.
- Formula for plan length 5 is satisfiable: 3 nodes in the search tree.
- Plans have 5 to 7 operators, optimal plan has 5.

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Solving the SAT Problem

SAT problems obtained from planning are solved by

- generic SAT solvers
 - ► Mostly based on Conflict-Driven Clause Learning (CDCL) [MMZ⁺01].

SAT

SAT solving

- Very good on hard combinatorial planning problems.
- Not designed for solving the extremely large but "easy" formulas (arising in some types of benchmark problems).
- specialized SAT solvers [Rin10, Rin12]
 - Replace standard CDCL heuristics with planning-specific ones.
 - For certain problem classes substantial improvement
 - New research topic: lots of unexploited potential

Solving the SAT Problem

Example

012345	012345	012345
clear(a) F F	FFF TT	FFFTTT
clear(b) F F	FF TTF	FETTTE
clear(c) TT FF	TTTTEE	TTTTEE
clear(d) FTTFFF	FTTEEE	ETTEEE
clear(e) TTFFFF	TTEEEE	TTEEEE
on(a,b) FFF T	FFFFFT	FFFFFT
on(a,c) FFFFFF	FFFFFF	FFFFFF
on(a,d) FFFFFF	FFFFFF	FFFFFF
on(a,e) FFFFFF	FFFFFF	FFFFFF
on(b,a) TT FF	TTT FF	TTTFFF
on(b,c) F F T T	FFFFTT	FFFFTT
on(b,d) FFFFFF	FFFFFF	FFFFF
on(b,e) FFFFFF	FFFFFF	FFFFF
on(c,a) FFFFFF	FFFFFF	FFFFFF
on(c,b) T FFF	TT FFF	TTFFFF
on(c,d) FFFTTT	FFFTTT	FFFTTT
on(c,e) FFFFFF	FFFFFF	FFFFFF
on(d,a) FFFFFF	FFFFFF	FFFFFF
on(d,b) FFFFFF	FFFFFF	FFFFFF
on(d,c) FFFFFF	FFFFFF	FFFFFF
on(d,e) FFTTTT	FFTTTT	FFTTTT
on(e,a) FFFFFF	FFFFFF	FFFFFF
on(e,b) F F F F F F F	FFFFFF	FFFFF
on(e,c) F F F F F F F	FFFFFF	FFFFFF
on(e,d) T F F F F F	TEEEE	TEEEE
ontable(a) T T T F	TTTTTF	TTTTTF
ontable(b) F F F F	FFF FF	FFFTFF
ontable(c) F FFF	FF FFF	FFTFFF
ontable(d) T T F F F F	TTFFFF	TTEEE
ontable(e) F T T T T T	FTTTTT	FTTTTT

1. State variable values inferred from initial values and goals.
2. Branch: ¬clear(b) ¹ .
3. Branch: clear(a) ³ .
4. Plan found: 01234 fromtable(a,b) FFFFT fromtable(b,c) FFFTF fromtable(c,d) FFTFF
fromtable(d,e) FTFFF totable(b,a) FFTFF totable(c,b) FTFFF totable(e,d) TFFFF



Symbolic search

Performance of SAT-Based Planners

Planning Competition Problems 1998-2008

Performance of SAT-Based Planners

Planning Competition Problems 1998-2011 (revised)



all domains 1998-2011

SAT

SAT solving

Symbolic Search Methods

- logical formulas as data structure for sets, relations
- state-space search (planning, model-checking, diagnosis, ...) in terms of set & relational operations
- Algorithms that can handle very large state sets, bypassing inherent limitations of enumerative methods.

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Symbolic search

Symbolic Search Methods **Motivation**

- SAT and explicit state-space search: primary use finding one path from an initial state to a goal state
- Symbolic" search methods can be used for more general problems:
 - Finding set of all reachable states
 - Distances/plans from the initial state to all states
 - Distances/plans to goal states from all states
- Competitive for optimal planning and detecting unsolvability.
- BDDs are a representation of belief states [BCRT01, Rin05].

Symbolic search

Algebraic Decision Diagrams (ADD) [FMY97, BFG⁺97] can represent value functions in probabilistic planning [HSAHB99].

Transition relations in propositional logic

State variables are $X = \{a, b, c\}.$

 $(\neg a \land b \land c \land \neg a' \land b' \land \neg c') \lor$ $(\neg a \land b \land \neg c \land a' \land b' \land \neg c') \lor$ $(\neg a \land \neg b \land c \land a' \land b' \land c') \lor$ $(a \land b \land c \land a' \land b' \land \neg c')$

The correspond	ling ı	matr	ix is	
000 001 010 0				

	000	001	010	011	100	101	110	111
000	0	0	0	0	0	0	0	0
001	0	0	0	0	0	0	0	1
010	0	0	0	0	0	0	1	0
011	0	0	1	0	0	0	0	0
100	0	0	0	0	0	0	0	0
101	0	0	0	0	0	0	0	0
110	0	0	0	0	0	0	0	0
111	0	0	0	0	0	0	1	0



Image operations

The image of a set T of states w.r.t. action a is

$$img_a(T) = \{s' \in S | s \in T, sas'\}$$

The pre-image of a set T of states w.r.t. action a is

$$preimg_a(T) = \{s \in S | s' \in T, sas'\}$$

These operations reduce to the relational join and projection operations with a logic-representation of sets (unary relations) and binary relations.

(Pre-image corresponds to regression used with backward-search [Rin08].)

Symbolic search Algorithms

Finding All Plans with a Symbolic Algorithm [BCL+94]

All reachable states with breadth-first search

 $S_0 = \{I\}$ $S_{i+1} = S_i \cup \bigcup_{a \in A} \operatorname{img}_a(S_i)$

If $S_i = S_{i+1}$, then $S_j = S_i$ for all $j \ge i$, and the computation can be terminated.

- ▶ $S_i, i \ge 0$ is the set of states with distance $\le i$ from the initial state.
- $S_i \setminus S_{i-1}, i \ge 1$ is the set of states with distance *i*.
- If $G \cap S_i$ for some $i \ge 0$, then there is a plan.

Action sequence recovered from sets S_i by a sequence of backward-chaining steps (linear in plan length and number of state variables) (Approximations of the above algorithm compute invariants [Rin08]).

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Symbolic State-Space Search Algorithms

Symbolic Breadth-First [BCL+94]

- Symbolic (BDD) versions of A*:
 - BDDA* [ER98]
 - SetA* [JVB08]
 - ADDA* [HZF02]
- The Saturation algorithm [CLS01, CLM07, YCL09] trades optimality (as obtained with breadth-first) to far better scalability: find all reachable states, without accurate distance information.

Representation of Sets as Formulas

state sets	formulas over X
those $\frac{2^{ X }}{2}$ states where x is true	$x \in X$
\overline{E} (complement)	$\neg E$
$E \cup F$	$E \lor F$
$E \cap F$	$E \wedge F$
$E \setminus F$ (set difference)	$E \wedge \neg F$
the empty set \emptyset the universal set	⊥ (constant <i>false</i>) ⊤ (constant <i>true</i>)
question about sets	question about formulas
$E \subseteq F$?	$E \models F$?
$E \subset F$?	$\models E \models F$ and $F \not\models E$?
E = F?	$\models E \models F$ and $F \models E$?



Formulas	over X	represent sets	

 $a \lor b$ over $X = \{a, b, c\}$ represents the set $\{ \substack{abc \\ 010}, 011, 100, 101, 110, 111 \}$.

Formulas over $X \cup X'$ represent binary relations

 $a \wedge a' \wedge (b \leftrightarrow b')$ over $X \cup X'$ where $X = \{a, b\}, X' = \{a', b'\}$ represents the binary relation $\{(10, 10), (11, 11)\}$. Valuations $\overset{a\,b\,a'b'}{10\,1\,0}$ and 1111 of $X \cup X'$ can be viewed respectively as pairs of valuations $\begin{pmatrix} ab & a'b' \\ 10 & 10 \end{pmatrix}$ and (11, 11) of X.

relation operation	logical operation
projection	abstraction
ioin	conjunction

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Existential and Universal Abstraction

Definition

Existential abstraction of a formula ϕ with respect to $x \in X$:

 $\exists x.\phi = \phi[\top/x] \lor \phi[\bot/x].$

Universal abstraction is defined analogously by using conjunction instead of disjunction.

Definition

Universal abstraction of a formula ϕ with respect to $x \in X$:

$$\forall x.\phi = \phi[\top/x] \land \phi[\bot/x]$$

∃-Abstraction

Example

$$\begin{split} \exists b.((a \rightarrow b) \land (b \rightarrow c)) \\ &= ((a \rightarrow \top) \land (\top \rightarrow c)) \lor ((a \rightarrow \bot) \land (\bot \rightarrow c)) \\ &\equiv c \lor \neg a \\ &\equiv a \rightarrow c \end{split}$$

 $\begin{aligned} \exists ab.(a \lor b) &= \exists b.(\top \lor b) \lor (\bot \lor b) \\ &= ((\top \lor \top) \lor (\bot \lor \top)) \lor ((\top \lor \bot) \lor (\bot \lor \bot)) \\ &\equiv (\top \lor \top) \lor (\top \lor \bot) \equiv \top \end{aligned}$

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Symbolic search	∃/∀-abstraction		Symbolic search	Images

\forall and \exists -Abstraction in Terms of Truth-Tables

 $\forall c \text{ and } \exists c \text{ correspond to combining lines with the same valuation for variables other than } c.$

Example

	$\exists c$	$a \vee (b)$	$(\land c)) \equiv a \lor$	$b \forall c$	$a \vee (b \wedge c)$)) ≡
a b c	$a \vee (b \wedge c)$	$a b \exists c$	$(a \lor (b \land c))$	$a \ b \forall c$	$a.(a \lor (b \land c))$)
000	0	0.0	0	0.0	0	
001	0					
010	0	$0 \ 1$	1	$0 \ 1$	0	
$0\ 1\ 1$	1					
100	1	$1 \ 0$	1	$1 \ 0$	1	
101	1					
110	1	1 1	1	11	1	
111	1					

Encoding of Actions as Formulas

Let *X* be the set of all state variables. An action *a* corresponds to the conjunction of the precondition P_j and

 $x' \leftrightarrow F_i(X)$

for all $x \in X$. Denote this by $\tau_X(a)$.

Example (move-from-A-to-B)

 $atA \wedge (atA' \leftrightarrow \bot) \wedge (atB' \leftrightarrow \top) \wedge (atC' \leftrightarrow atC) \wedge (atD' \leftrightarrow atD)$

This is exactly the same as in the SAT case, except that we have x and x' instead of x@t and x@(t+1).

a

Images as Relational Operations



Computation of Successor States

Let

- $\blacktriangleright X = \{x_1, \dots, x_n\},\$
- $X' = \{x'_1, \dots, x'_n\},\$
- ϕ be a formula over X that represents a set T of states.

Image Operation

The image $\{s' \in S | s \in T, sas'\}$ of T with respect to a is

 $img_a(\phi) = (\exists X.(\phi \land \tau_X(a)))[X/X'].$

Normal form

The renaming is necessary to obtain a formula over X.

Computation of Predecessor States

Let

- $\blacktriangleright X = \{x_1, \dots, x_n\},\$
- $X' = \{x'_1, \dots, x'_n\},$
- ϕ be a formula over X that represents a set T of states.

Symbolic search

Images

Preimage Operation

The pre-image $\{s \in S | s' \in T, sas'\}$ of T with respect to a is

 $preimg_a(\phi) = (\exists X'.(\phi[X'/X] \land \tau_X(a))).$

The renaming of ϕ is necessary so that we can start with a formula over X.

Normal Forms

normal form	reference	comment
NNF Negation Normal Form		
DNF Disjunctive Normal Form		
CNF Conjunctive Normal Form		
BDD Binary Decision Diagram	[Bry92]	most popular
DNNF Decomposable NNF	[Dar01]	more compact
d-DNNF deterministic DNNF	[Dar02]	

Symbolic search

Darwiche's terminology: knowledge compilation languages [DM02]

Trade-off

- ▶ more compact → less efficient operations
- But, "more efficient" is in the size of a correspondingly inflated formula. (Also more efficient in terms of wall clock?)
 BDD-SAT is O(1), but e.g. translation into BDDs is (usually) far less efficient than testing SAT directly.

Complexity of Operations

	\vee	\land	-	TAUT	SAT	$\phi \equiv \phi'?$	#SA
NNF	poly	poly	poly	co-NP	NP	co-NP	#P
DNF	poly	exp	exp	co-NP	Ρ	co-NP	#P
CNF	exp	poly	exp	Р	NP	co-NP	#P
BDD	exp	exp	poly	Р	Ρ	Р	poly
DNNF	poly	exp	exp	co-NP	Ρ	co-NP	#P
d-DNNF	poly	exp	exp	co-NP	Ρ	co-NP	poly

Remark

For BDDs one \vee/\land is polynomial time/size (size is doubled) but repeated \vee/\land lead to exponential size.

Planners Algorithm portfolios

Algorithm Portfolios

- Algorithm portfolio = combination of two or more algorithms
- Useful if there is no single "strongest" algorithm.



- Gap between Theory and Practice large: engineering details of implementation critical for performance in current planners.
- > Few of the most efficient planners use textbook methods.
- Explanations for the observed differences between planners lacking: this is more art than science.

Planners Algorithm portfolios

Algorithm Portfolios

Composition methods

Methods fo	r composing a portfolio	
selection parallel sequential	choose one for current instance [XHHLB08] run components in parallel [GS97, HLH97] run consecutively, according to a schedule	
Other variatio	ns of the above [HDH ⁺ 00].	
Early upon in	planning: PLACKPOX [KS00] (manual configuration)	

Early uses in planning: BLACKBOX [KS99] (manual configuration), FF [HN01] and LPG [GS02] (fixed configuration)

Lots of works in the SAT area [XHHLB08], directly applicable to planning as the main methods are no specific to SAT or planning.

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Algorithm Portfolios



Sampling from the Set of All Instances [Byl96, Rin04c]

- Generation:
 - 1. Fix number N of state variables, number M of actions.
 - 2. For each action, choose preconditions and effects randomly.
- Has a phase transition from unsolvable to solvable, similarly to SAT [MSL92] and connectivity of random graphs [Bol85].
- Exhibits an easy-hard-easy pattern, for a fixed N and an increasing M, analogously to SAT [MSL92].
- Hard instances roughly at the 50 per cent solvability point.
- Hardest instances are very hard: 20 state variables (2²⁰ states) too difficult for many planners.

Evaluation of planning systems is based on

- Hand-crafted problems (from the planning competitions)
 - This is the most popular option.
 - + Problems with (at least moderately) different structure.
 - Real-world relevance mostly low.
 - Instance generation uncontrolled: not known if easy or difficult.
 - Many have a similar structure: objects moving in a network.

Evaluation

- Benchmark sets obtained by translation from other problems
 - ► graph-theoretic problems: cliques, colorability, ... [PMB11]
- Instances sampled from all instances [Byl96, Rin04c].
 - + Easy to control problem hardness.
 - No direct real-world relevance (but: core of any "hard" problem)

Evaluation

Sampling from the Set of All Instances

Experiments with planners



Model A: Distribution of runtimes with SAT

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Introduction to Temporal Planning

Motivation 1: How long does executing a plan take?

Minimization of the duration of the execution phase:

- Two short actions may be better than one long one.
- Actions can be taken in parallel.
- Connection to scheduling problems [SFJ00].

This is a core consideration in most mixed planning+scheduling problems. (Duration and especially concurrency ignored in classical planning and basic state-space search methods.) Inherent concurrency of actions

Motivation 2: Plans require concurrency

Taking an action may require other concurrent actions.

Introduction to Temporal Planning

Some effects may only be achieved as joint effects of multiple actions.

Less important in practice: can often (always?) be avoided by modelling problem differently.

- Actions that must be used concurrently can be combined.
- Replace one complex action by several simpler ones: go to Paris = go to airport, board plane, fly, exit, take train to city



If each action needs 1 unit of the resource, no more than n actions can

Action Dependencies through Resources

Simultaneous use of resource can be at most n units.

Multiple actions can use the resource in the same state.

Example: generator that can produce 110V,60Hz or 220V,50Hz

Relation to scheduling

- Planning = action selection + scheduling.
- Scheduling = assignment of starting times to tasks/actions, respecting resource constraints
- Expressive languages for temporal planning include scheduling and hence support the representation of resources.
- Resources and ordering constraints are the mechanism for guaranteeing that plans are executable.

Timed Systems Explicit state-space

Complexity

Most important scheduling problems are NP-complete [GJ79]. Temporal planning complete for PSPACE or EXPSPACE [Rin07]. Action selection is the main difference between them.

Timed Systems Models

Embedding of Scheduling in Temporal Planning

Representation of a simple job-shop scheduling problem in temporal planning.

- 1. For each job j = a sequence of tasks $t_1^j, \ldots, t_{n_j}^j$, introduce state variable $p_j : \{1, \ldots, n+1\}$.
- 2. Each task is mapped to action a_i^j with
 - precondition $p_j = i$,

► *n*-ary resources

state resources

be using it simultaneously.

Example: *n* identical tools or machines

A resource is in at most one state at a time.

- effect $p_j = i + 1$ after the duration of t_i^j ,
- resource requirements as in the scheduling problem.
- 3. In the initial state $p_j = 1$ for every job j.
- 4. In the goal we have $p_j = n_{j+1}$.

Tasks and their ordering inside the job are fixed. Remaining problem is scheduling the tasks/actions for different jobs relative to other jobs' tasks/actions and minimizing the makespan.

Solutions of the temporal planning problem are exactly the solutions to the job-shop scheduling problem.

Timed State-Space

- state = values of state variables + values of clocks
- Clocks induce a schedule of future events.
- Actions initialize clocks.
- ► Time progresses, affecting all clocks.
- Reaching a critical clock value triggers scheduled events:
 - effects taking place later than the action's "starting" time point
 - resources allocated and later freed

This is the model behind all search methods.

Seemingly simple route to temporal planning with explicit state-space search.

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Timed Systems Explicit state-space

Updates to the timed state

Advancing time

Take action with precondition $x_2 = 1$ and effect $x_5 := 0$ at time 3.

- $x_1 = 10$
- $x_2 = 1$
- $x_3 = 0$
- $x_4 = 0$
- $x_5 = 10$



Completeness of Timed State-Space Search

- Simplistic policies for advancing time lead to incompleteness [MW06]. Most early temporal planners are incomplete. Few temporal planners have been proved to be complete.
- region abstraction [AD94] abstracts an infinite number of timed states to finitely many behaviorally equivalent regions.

Timed Systems Explicit state-space

Separation of planning and scheduling CPT planner [VG06]

- Separate two problems
 - 1. selection of actions (only ordering, no timing)
 - 2. scheduling of these actions

and interleave their solution.

- Action selection induces temporal constraints [DMP91]
- These temporal constraints can be solved separately.
- Completeness regained.

Systems for Temporal Planning

- Probably the most powerful verification tool based on explicit state-space search in the state-space induced by timed automata and their extension hybrid automata is UPPAAL [BLL+96].
 UPPAAL has been used in modelling and solving planning scenarios for example in robotics [QBZ04] and autonomous embedded systems [AAG+07, KMH01].
- CPT [VG06]
- Temporal Fast-Downward, based on the Fast-Downward planner for classical planning

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Temporal Planning by Constraint Satisfaction

- Temporal planning can be encoded in
 - SAT modulo Theories (SMT) [WW99, ABC⁺02].
 - Constraint Programming [RvBW06]
 - Mixed Integer Linear Programming [DG02]

(Similarly to scheduling [ABP+11].)

- ► The encoding methods for all are essentially the same. Differences in surface structure of the encoding, especially the types of constraints that can be encoded directly.
- In this tutorial we focus on SMT, due to its closeness to SAT.
- Differences in performance and pragmatic differences:
 - CP: support for customized search (heuristics, propagators, ...)
 - SMT: fully automatic, powerful handling of Boolean constraints.
 - MILP: for problems with intensive linear optimization

Encodings of Timed Problems in SMT Variables

Each SMT instance fixes the number of steps *i* analogously to untimed (asynchoronous) state-space problems in SAT.

variables in SMT encoding

var	type	description
Δ_i	real	time between steps $i - 1$ and i
a@i	bool	Is action a taken at step i?
$c_a@i$	real	Value of clock for action a at step i
x@i	bool	Value of Boolean state variable at step i

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Timed Systems Constraint-based methods		Timed Systems Constraint-based methods	
Encodings of Timed Problems in SMT		Encodings of Timed Problems in SMT	
Action cannot be taken if it is already active:		Formula ϕ with every variable x replaced by $x@i$ is denoted by $\phi@i$.	
$a@i \rightarrow (c_a@(i-1) \geq \textit{dur}(a))$ (<i>dur</i> (<i>a</i>) denotes the duration <i>a</i>).	(1)	Action with precondition p : $a@i \rightarrow p@i$	(5)
If actions actions a_1 and a_2 use the same unary resource respectively at		If action is taken, its clock is initialized to 0:	
$[t_1,t_1']$ and at $[t_2,t_2']$ then we have		$a@i \rightarrow (c_a@i = 0)$	(6)
$t_2 + t_2' - c_{a_1} @i \le t_1$	(2)	If action is not taken, its clock advances:	
Additionally, if $[t_1, t_1']$ and $[t_2, t_2']$ overlap, we have	(3)	$\neg a@i \rightarrow (c_a@i = c_a@(i-1) + \Delta_i)$	(7)
$\neg a_1 @i \lor \neg a_2 @i$	(4)		
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 $(c_a@i = t) \rightarrow l@i$

Encodings of Timed Problems in SMT

An effect l scheduled at relative time t:

Encodings of Timed Problems in SMT Passage of time





Let
$$(a_1, t_1), \ldots, (a_k, t_k)$$
 be all actions and times such that action a_i makes x true at time t relative to its start.

$$(\neg x@(i-1) \land x@i) \rightarrow ((c_{a_1}@i=t_1) \lor \dots \lor (c_{a_k}@i=t_k))$$
 (11)

The frame axiom for x becoming false is analogous.

- Real variables in SMT incur a performance penalty.
- The encoding we gave is very general. In many practical cases (e.g. unit durations, small integer durations) more efficient encodings possible (SAT rather than SMT), similarly to scheduling problems.

Planning with Continuous Change

Hybrid systems = discrete change + continuous change

Planning with Continuous Change Example

- Physical systems have continuous change.
 - movement of physical objects, substances, liquids (velocity, acceleration)
 - chemical and biological processes
 - light, electromagnetic radiation
 - electricity: voltage, charge, AC frequency, AC phase
- Discrete parts make the overall system piecewise continuous:
 - Discrete changes triggered by continuous change.
 - Continuous change controlled by discrete changes.
- Inherent issues with physical systems: lack of predictability, inaccuracy of control actions
- > Problems primarily researched in control theory: Hybrid Systems Control, Model Predictive Control ("Planning" with continuous change not a separate research problem!)





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- Continuous change a function of time.
- Type of change determined by discrete parts of the system.
- Example: heater on, heater off, temperature $f(w_0, \Delta)$
- Example: object in free fall, on ground, altitude $f(h_0, \Delta)$
- Both actions and continuous values trigger discrete change.
- Example: Falling object reaches ground.
- Example: Container becomes full of liquid.

- Basic framework exactly as in the discrete timed case.
- Value of continuous variables directly a function of Δ . law. explanation

onplatiation
linear change proportional to Δ
exponential change
new constant value
no change, previous value

Other forms of change require a clock variable and an initial value. For example polynomials $c + x^n$.

[HKPV95, CL00, PC07]: complete algorithms only for narrow problem

decidable cases for reachability: rectangular automata [HKPV95], 2-d

semi-decision procedures: no termination when plans don't exist.

Hybrid systems: computational properties

classes.

Simple decision problems about hybrid systems undecidable

PCD [AMP95], planar multi-polynomial systems [ČV96]

stability: sensitivity to small inaccuracies in control [YMH98]

Hybrid systems: reasoning and analysis

- Main approaches generalize those for discrete timed systems.
 - explicit state-space search (e.g. HyTech [HHWT97])
 - SAT, constraints [SD05]
- Linear systems handled by efficient standard methods (MILP, linear arithmetics) in tools like MILP solvers and SAT modulo Theories solvers [SD05, ABCS05].
- Challenge: non-linear change
 - non-linear programming a very wide subarea of mathematical optimization. mixed integer nonlinear programming solvers (MINLP):

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- AIMMS
- MAPLE
- Mathematica
- MATLAB
- SMT solvers with non-linear arithmetic [JDM12, GKC13].

105/128 106/128 Timed Systems Continuous change Reference **Model Predictive Control References** Inaccuracy of control, uncertainty, unpredictability Yasmina Abdeddaïm, Eugene Asarin, Matthieu Gallien, Félix Ingrand, Charles Lesire, Mihaela Sighireanu, et al. Planning robust temporal plans: A comparison between CBTP and TGA approaches. In ICAPS 2007. Proceedings of the Seventeenth International Conference on Automated Planning and Scheduling, pages 2-10. AAAI Press, 2007. Model Predictive Control [GPM89] ("Dynamical Matrix Control", "Generalized Gilles Audemard, Piergiorgio Bertoli, Alessandro Cimatti, Artur Korniłowicz, and Roberto Sebastiani. Predictive Control", "Receding Horizon Control") A SAT based approach for solving formulas over Boolean and linear mathematical propositions. In Andrei Voronkov, editor, Automated Deduction - CADE-18, 18th International Conference on Physical systems often not predictable enough for deterministic control. Automated Deduction, Copenhagen, Denmark, July 27-30, 2002, Proceedings, number 2392 in Lecture Notes in Computer Science, pages 195-210. Springer-Verlag, 2002. Continuous observation - prediction - control cycle. Gilles Audemard, Marco Bozzano, Alessandro Cimatti, and Roberto Sebastiani Predictions over a finite receding horizon Verifying industrial hybrid systems with MathSAT. Electronic Notes in Theoretical Computer Science, 119(2):17-32, 2005. Hybrid Model Predictive Control, integrating discrete variables. Carlos Ansótegui, Miquel Bofill, Miquel Palahı, Josep Suy, and Mateu Villaret. Satisfiability modulo theories: An efficient approach for the resource-constrained project scheduling Mixed Logical Dynamical (MLD) systems [BM99] problem. In Proceedings of the 9th symposium on abstraction, reformulation and approximation (SARA 2011), pages 2-9, 2011. Rajeev Alur and David L. Dill. A theory of timed automata. Theoretical Computer Science, 126(2):183-235, 1994

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