

Light



Today

- What is light?
 - Intuitive properties
 - Ray optics model
- Quantifying light under ray optics
 - Radiance, radiosity, irradiance, etc.
- Application: soft shadows from area light sources

**Rendering \Leftrightarrow
what is the radiance hitting my sensor?**

A sunset over a beach. The sun is low on the horizon, casting a bright orange glow across the sky and reflecting on the water. Silhouettes of people are visible on the beach, and a large tree is silhouetted against the sun. The sky is filled with clouds, some of which are illuminated by the setting sun.

Rendering \Leftrightarrow
what is the radiance hitting my sensor?
“Radiance”? That’s what we’ll see today.

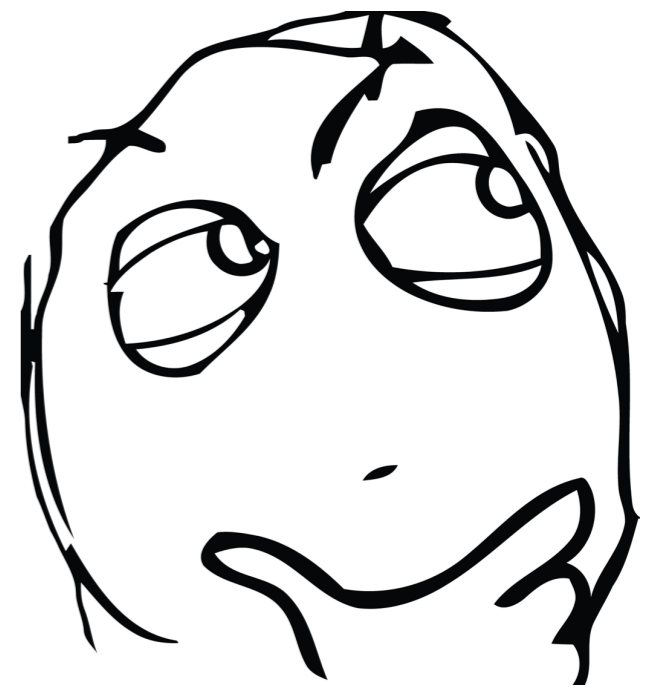


Properties of Light, Intuitively

- How “*bright*” something is doesn’t directly tell you how brightly it *illuminates* something
 - The lamp appears just as bright from across the room and when you stick your nose to it (“intensity does not attenuate”)
 - Also, the lamp’s apparent brightness does not change much with the angle of exitance

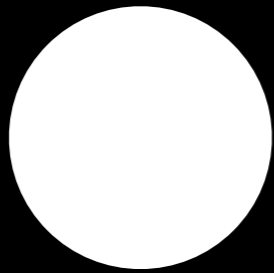
Properties of Light, Intuitively

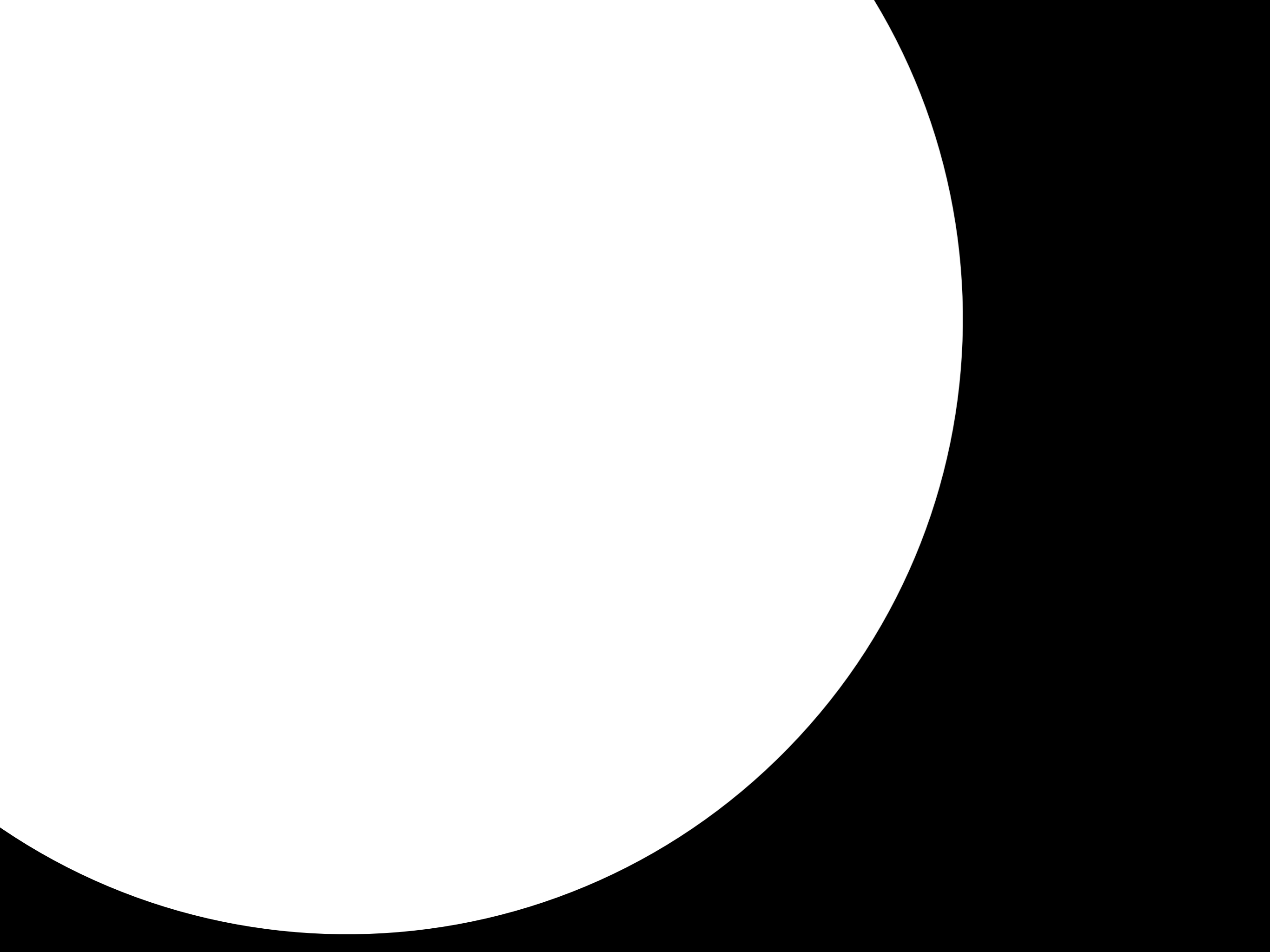
- How “*bright*” something is doesn’t directly tell you how brightly it *illuminates* something
 - The lamp appears just as bright from across the room and when you stick your nose to it (“intensity does not attenuate”)
 - Also, the lamp’s apparent brightness does not change much with the angle of exitance
- **However**
 - if you take the receiving surface further away, it will reflect less light and appear darker
 - If you tilt the receiving surface, it will reflect less light and appear darker



What's Going On?

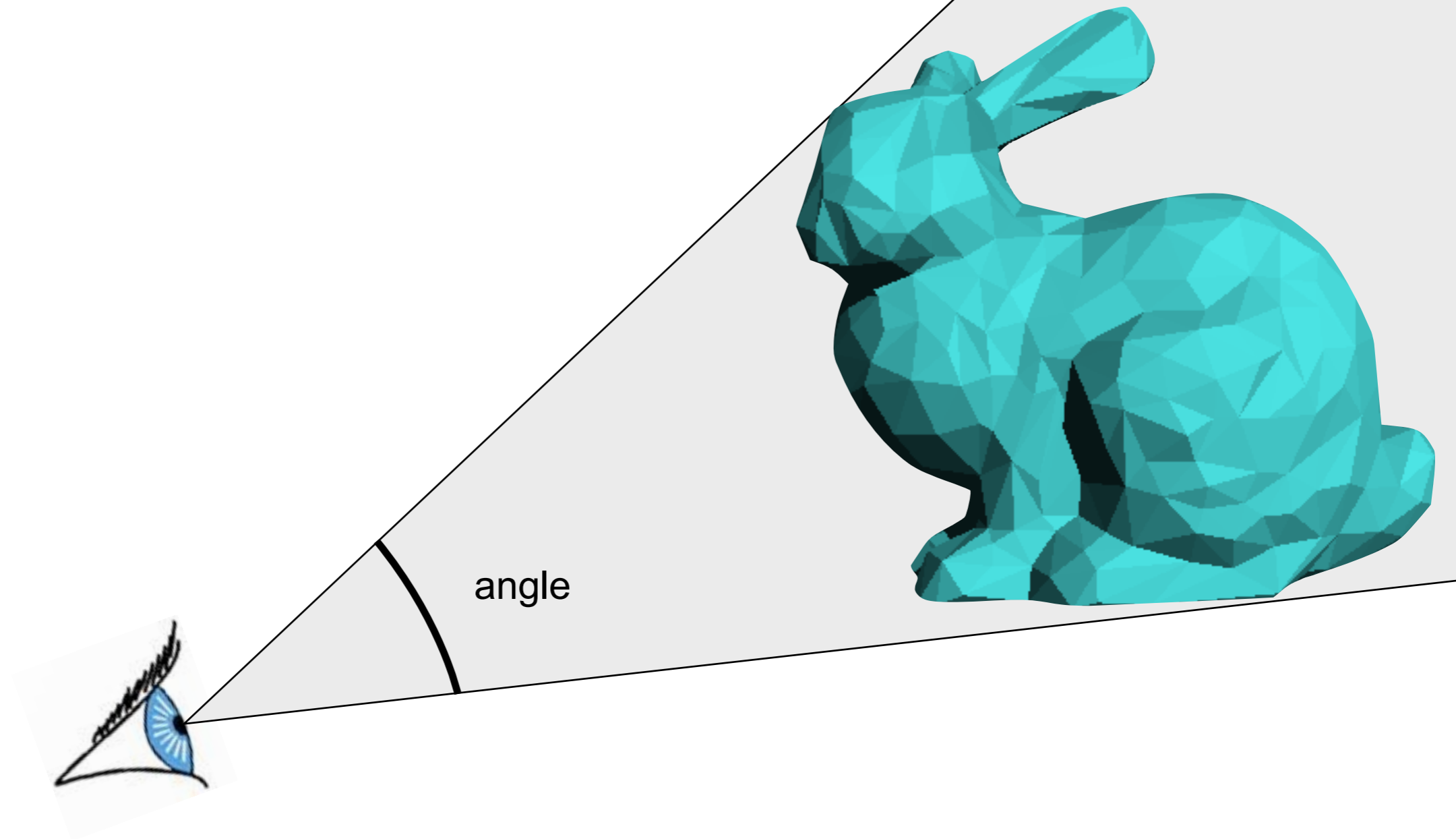
- “Illumination power” determined by **solid angle** subtended by the light source
 - Simple: “how big something looks”
 - Remember this well!
 - (Receiver orientation also has a role: a little later)





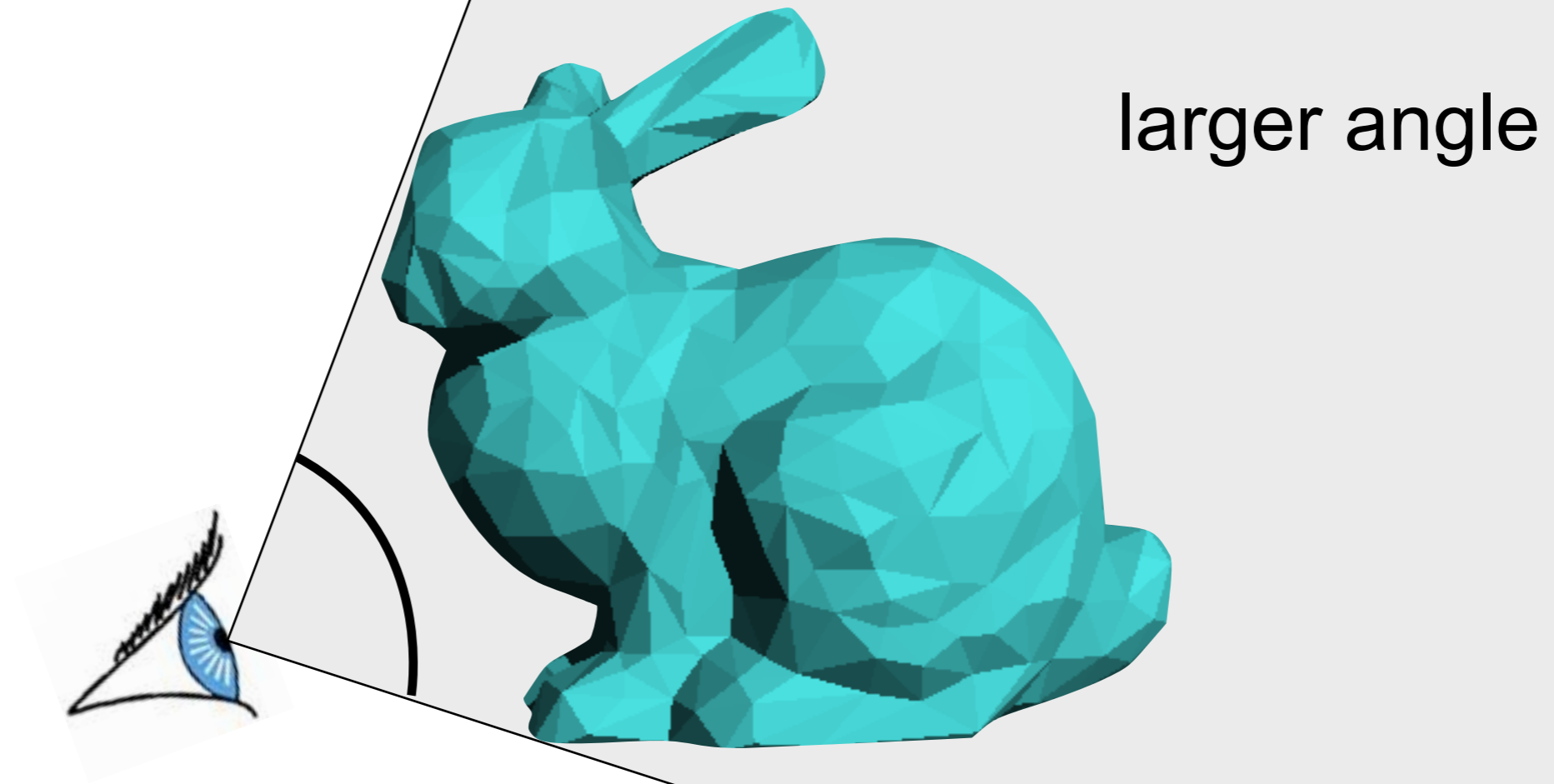
“How Big Something Looks”

- First, 2D

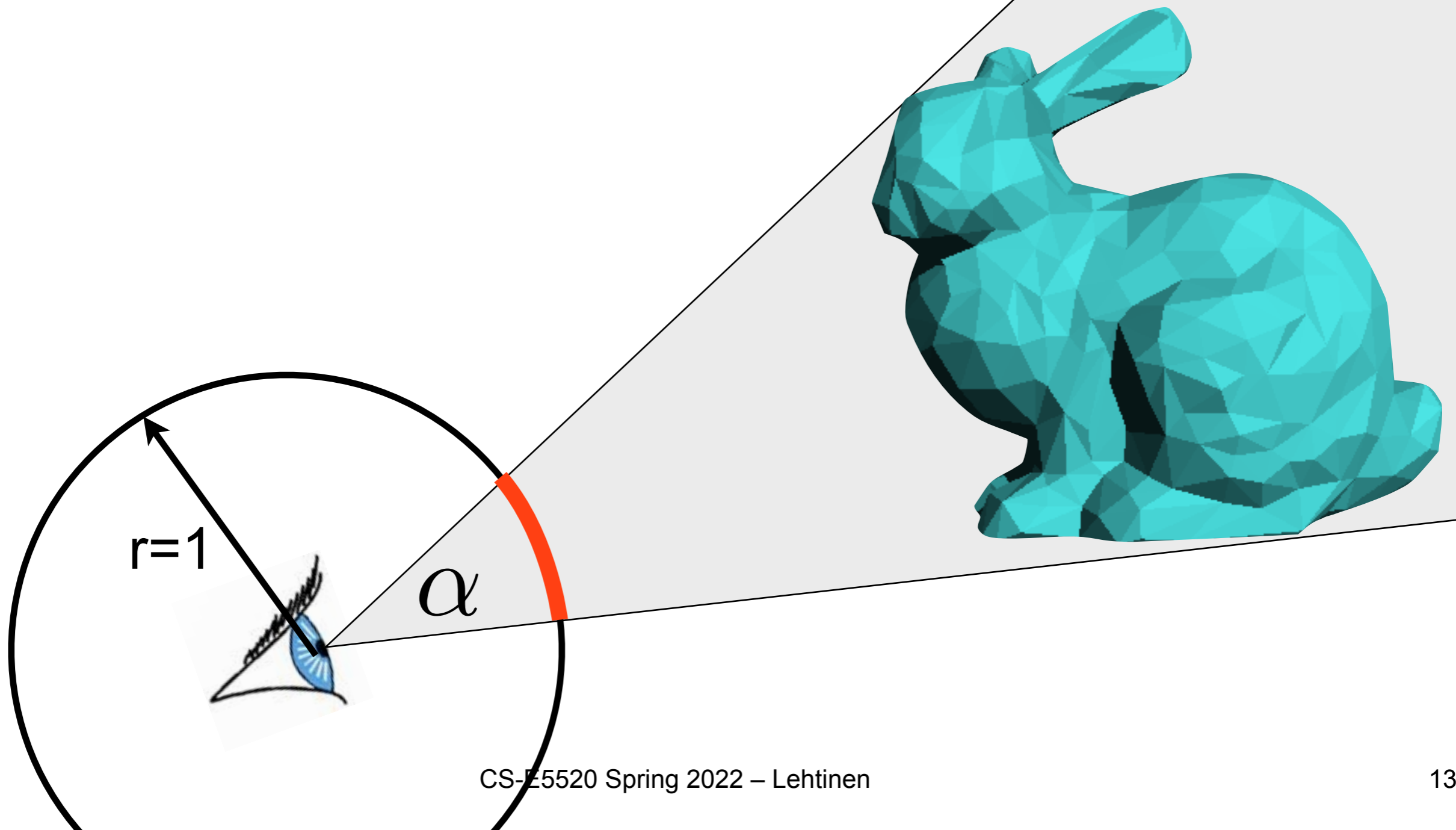


“How Big Something Looks”

- First, 2D

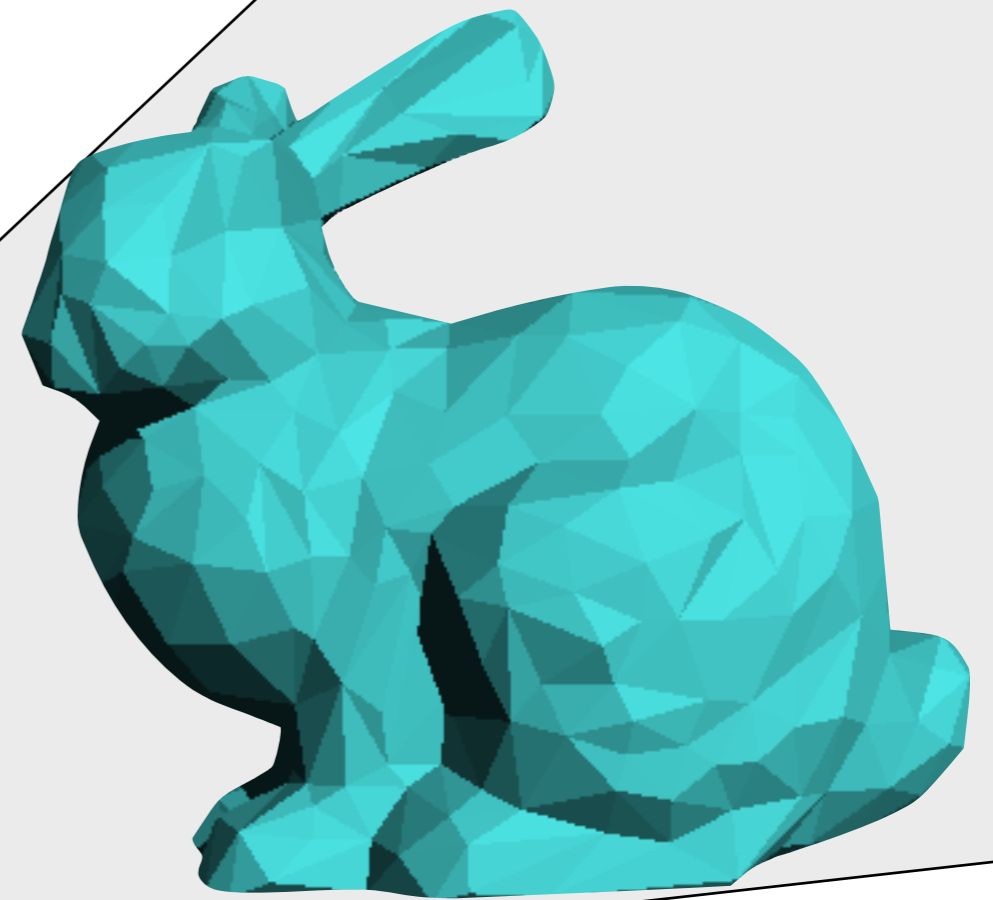
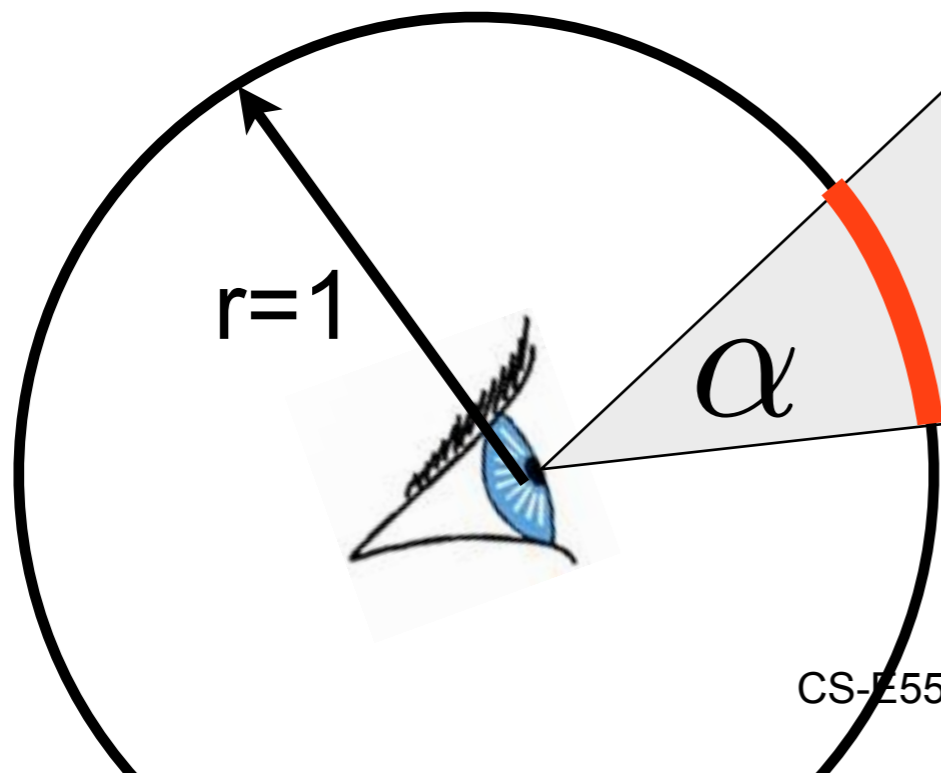


Angle measures “how big something looks”



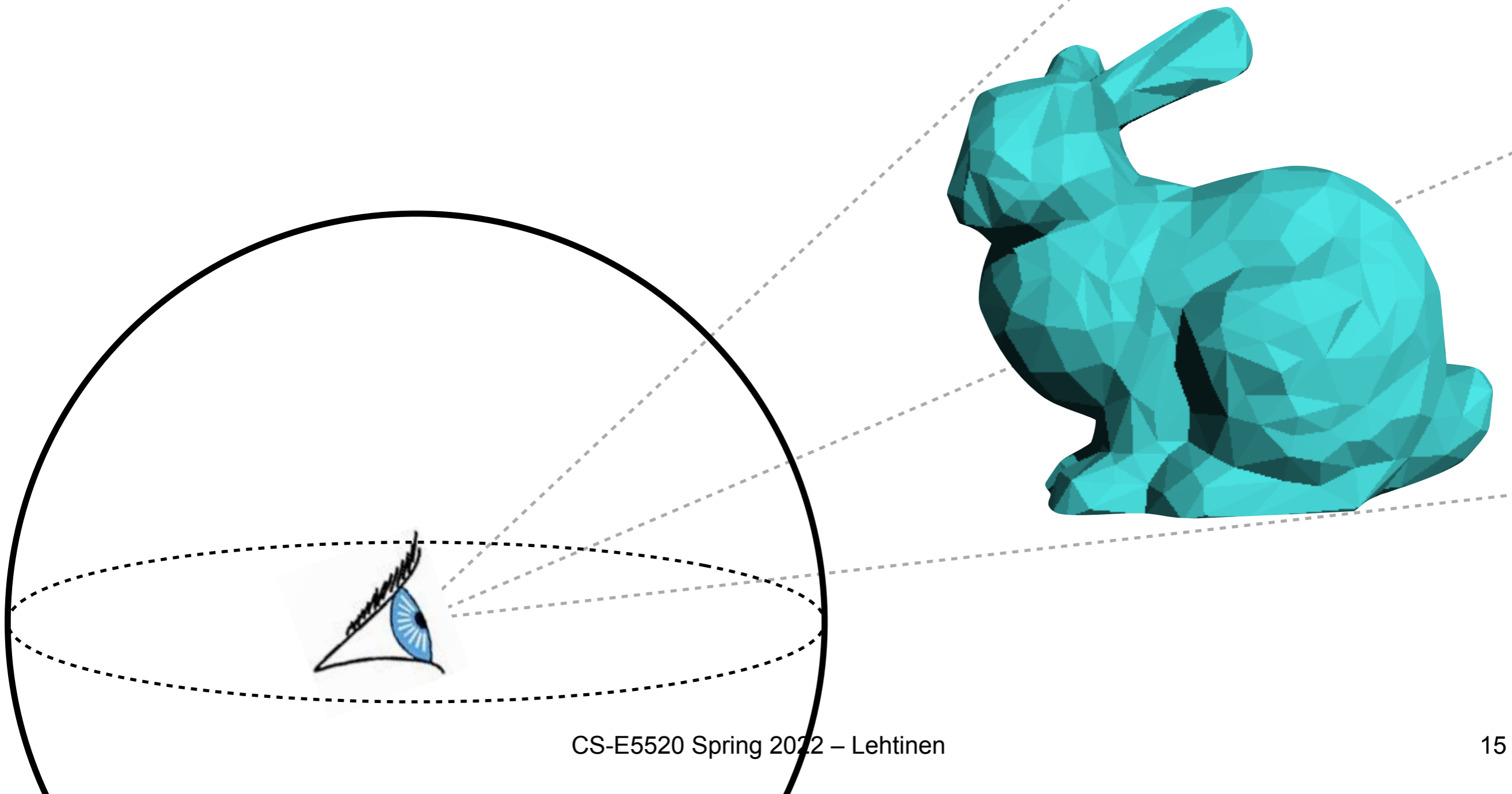
Angle measures “how big something looks”

- Angle α in radians \Leftrightarrow
length on unit circle
 - Hence: full circle is 2π radians



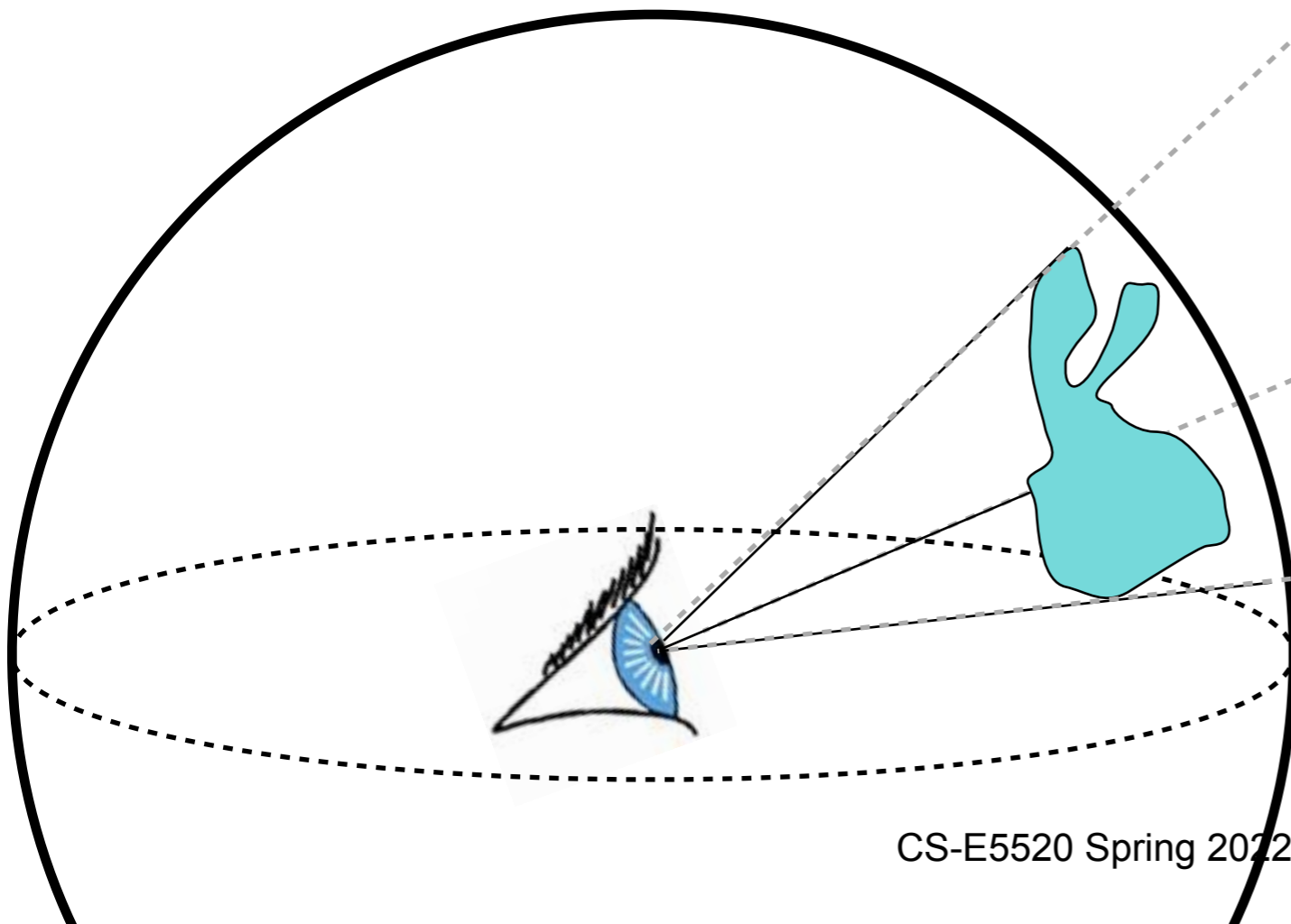
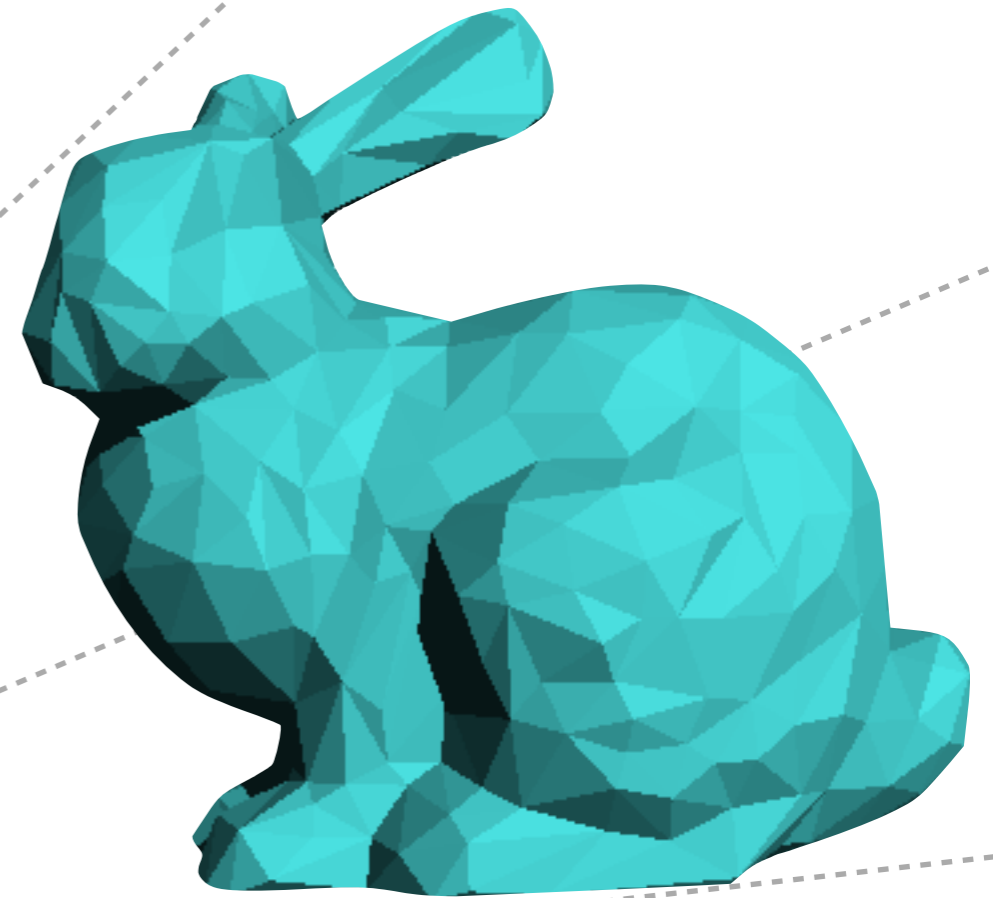
“How Big Something Looks”

- Then 3D: replace unit circle with unit sphere

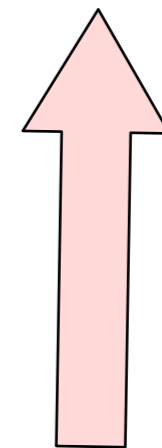
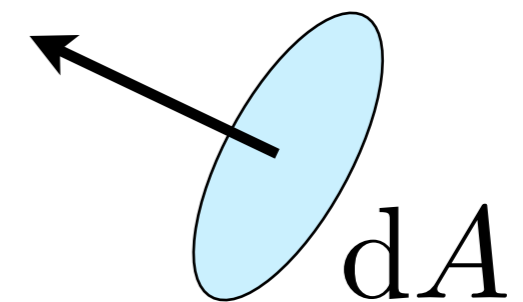
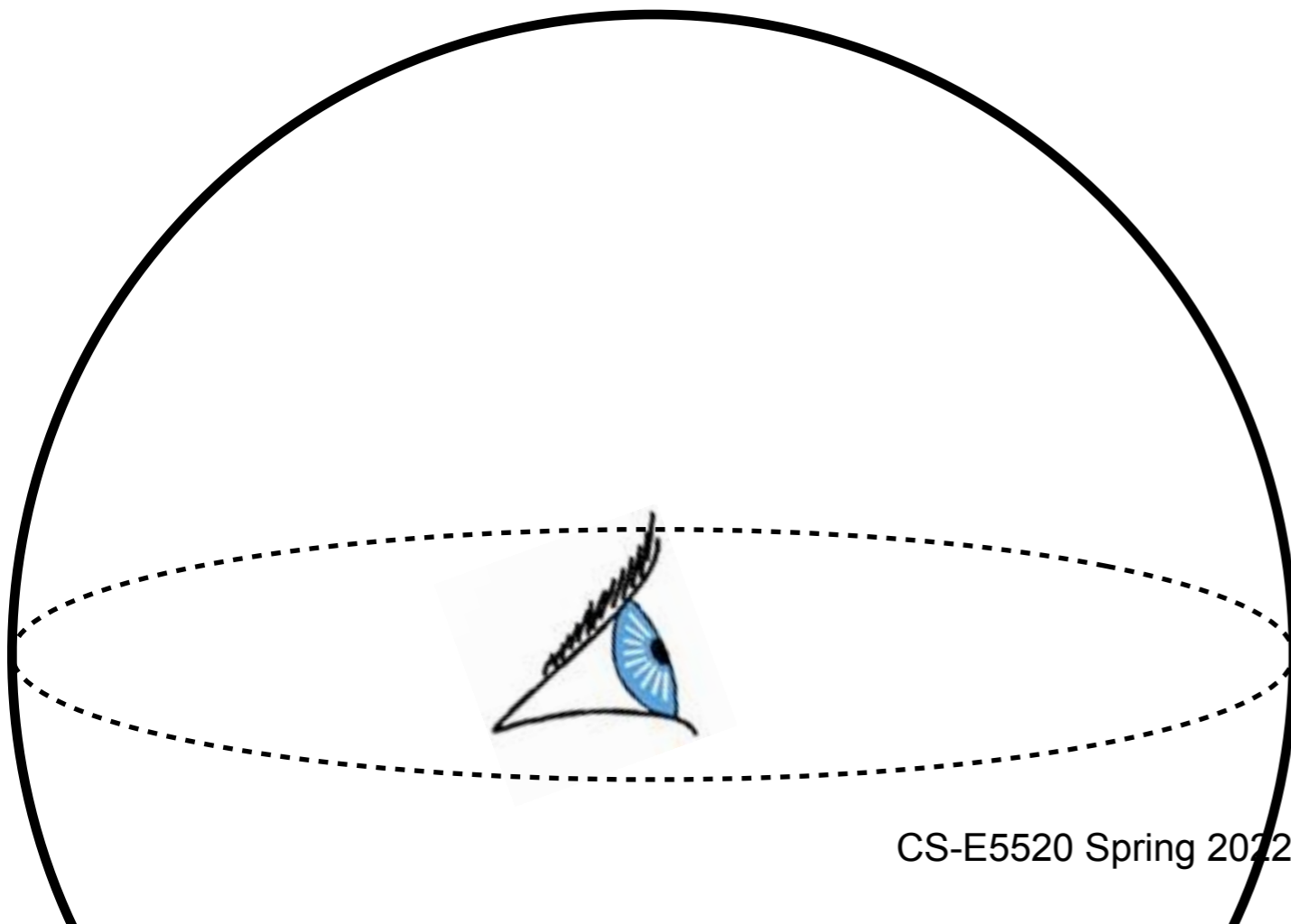


“How Big Something Looks”

- Then 3D: replace unit circle with unit sphere
 - Same thing: **solid angle** \Leftrightarrow projected area on unit sphere
 - Unit: **steradian (sr)**
 - Hence: full solid angle 4π steradians



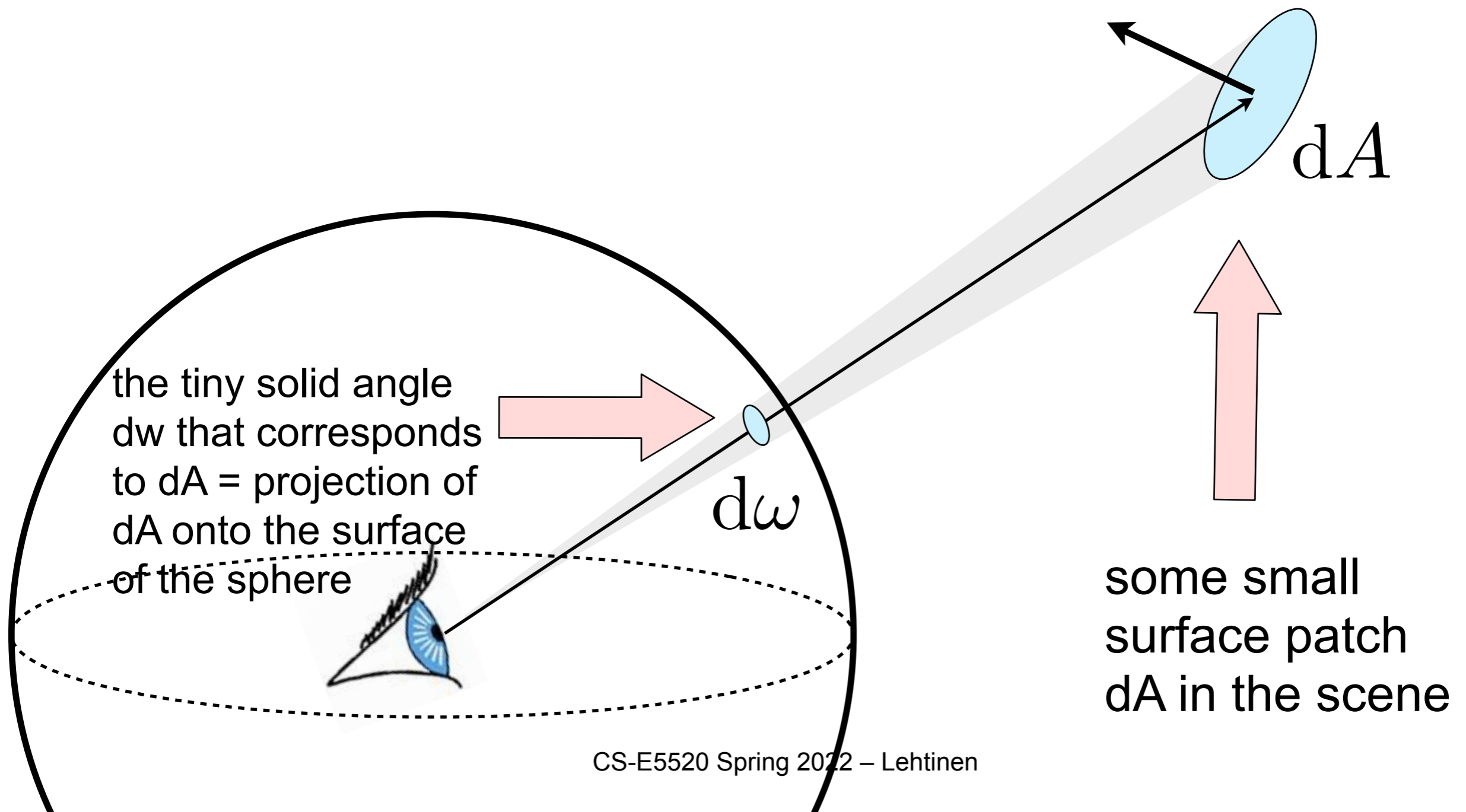
Relationship of Area and Solid Angle



some small
surface patch
 dA in the scene

Relationship of Area and Solid Angle

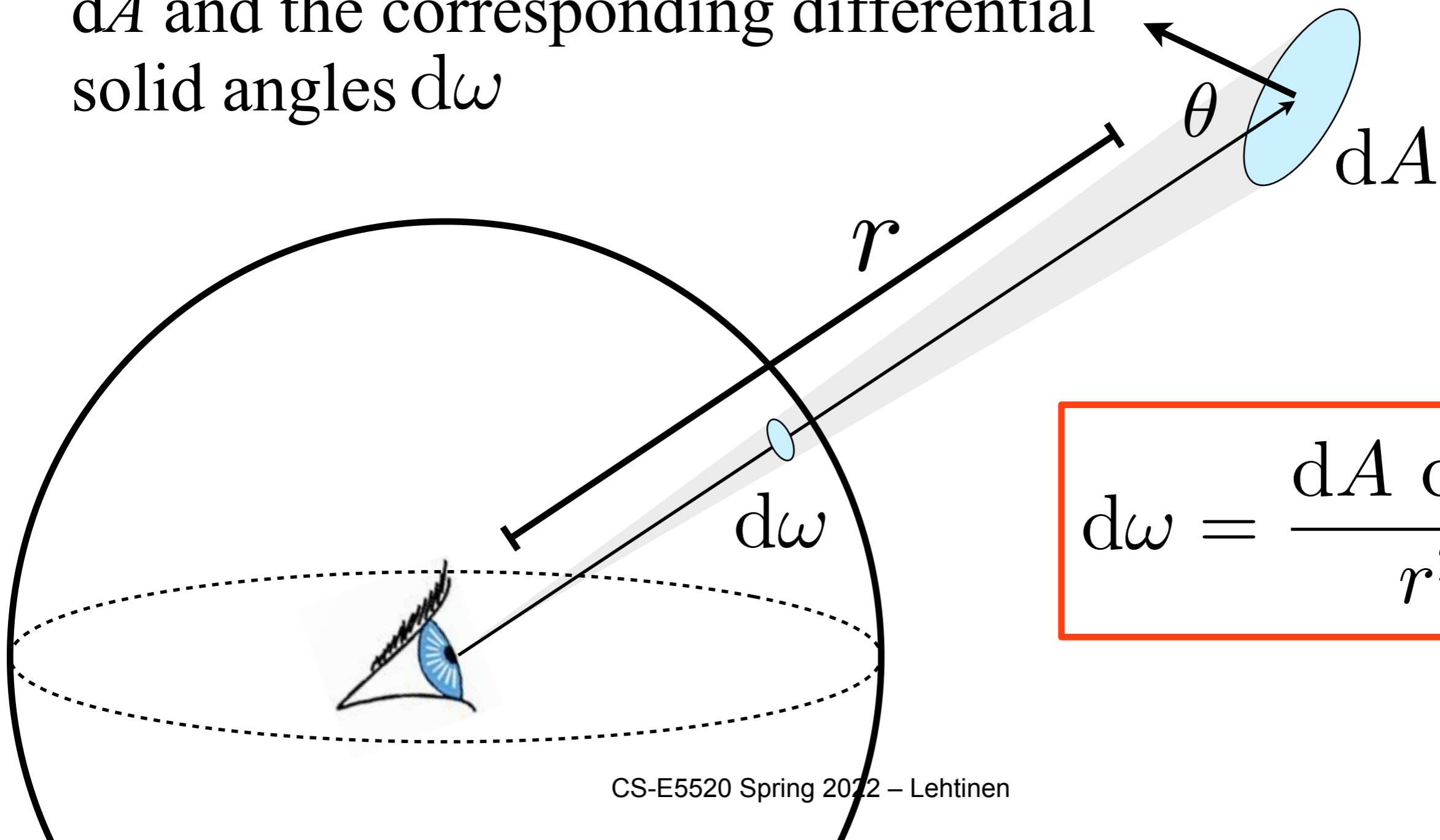
- What determines the area of the projected patch $d\omega$?



Relationship of Area and Solid Angle

- This simple relationship holds for infinitesimally small surface patches dA and the corresponding differential solid angles $d\omega$

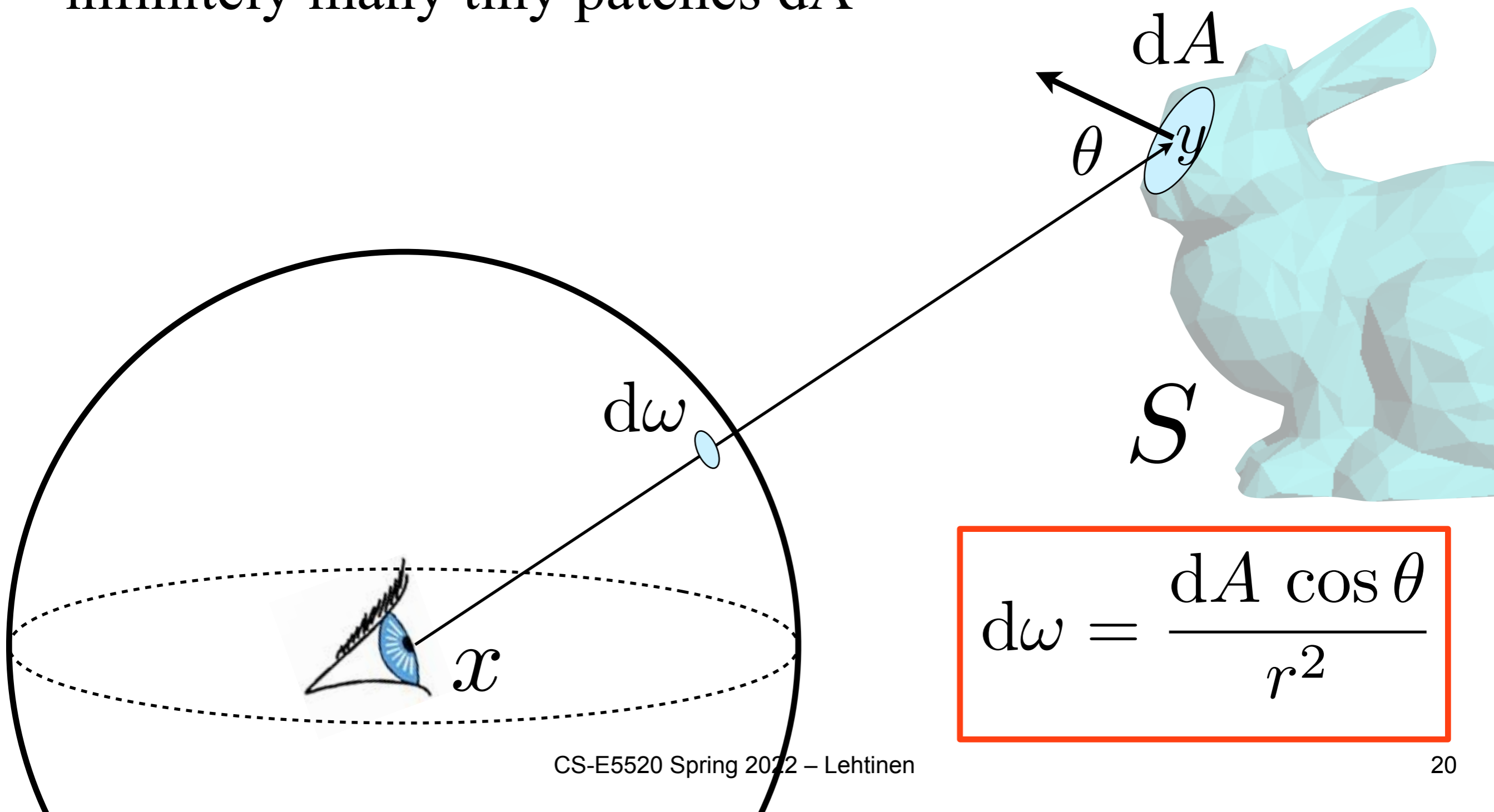
Distance r
Angle θ



$$d\omega = \frac{dA \cos \theta}{r^2}$$

Larger Surfaces

- Actual surfaces consist of infinitely many tiny patches dA



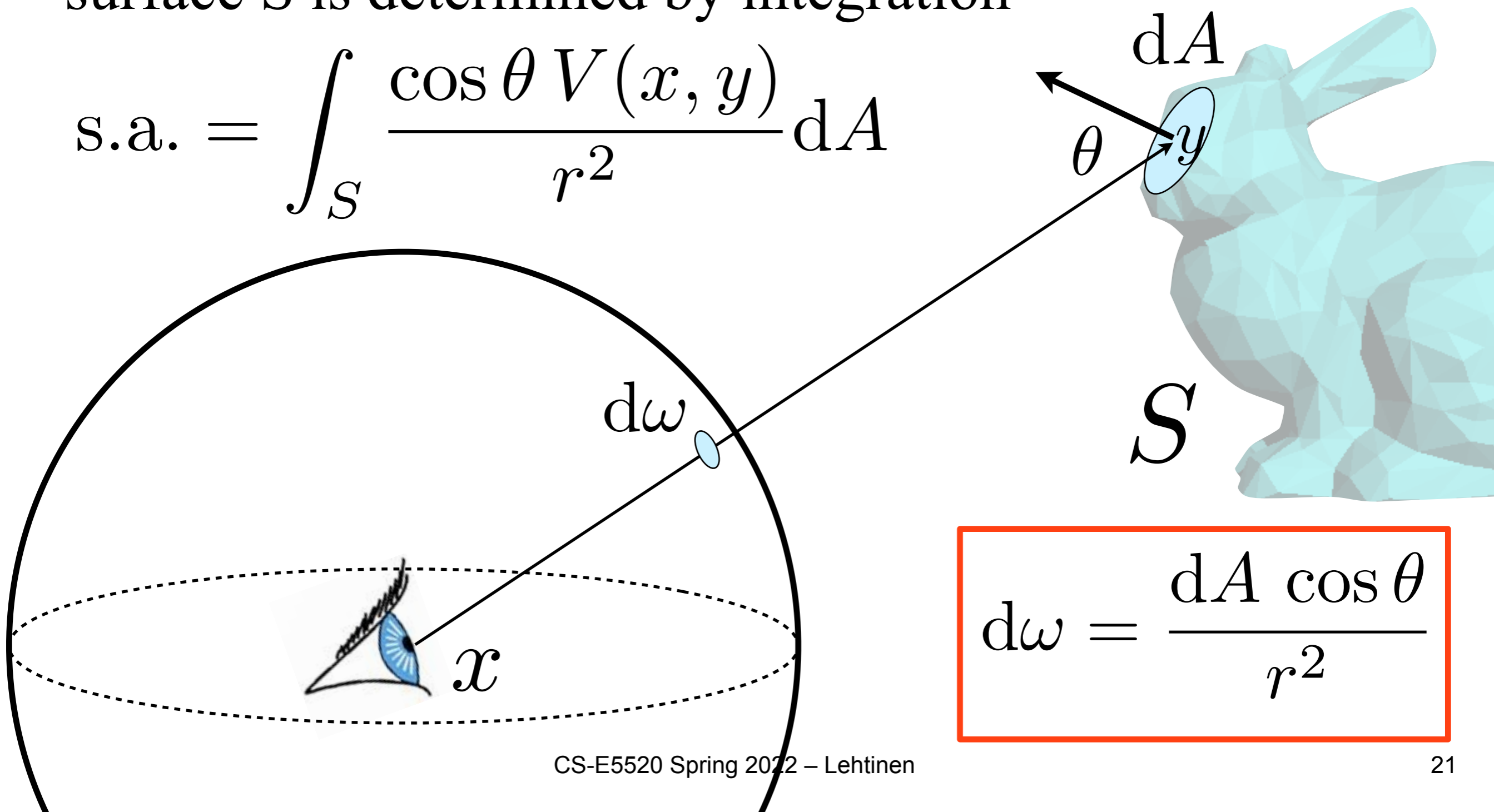
$$d\omega = \frac{dA \cos \theta}{r^2}$$

Larger Surfaces

$V(x,y) = (\text{are } x \text{ and } y \text{ visible to each other? } 1 : 0)$

- Solid angle subtended by actual, non-infinitesimal surface S is determined by integration

$$\text{s.a.} = \int_S \frac{\cos \theta V(x, y)}{r^2} dA$$

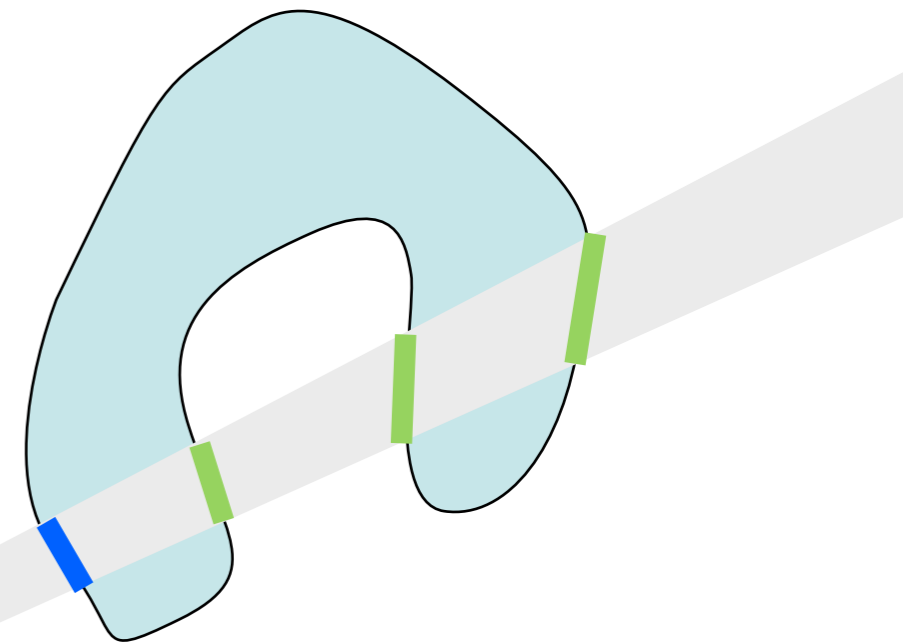


Larger Surfaces

$V(x,y)$ = (are x and y visible to each other? 1 : 0)

$$\text{s.a.} = \int_S \frac{\cos \theta V(x,y)}{r^2} dA$$

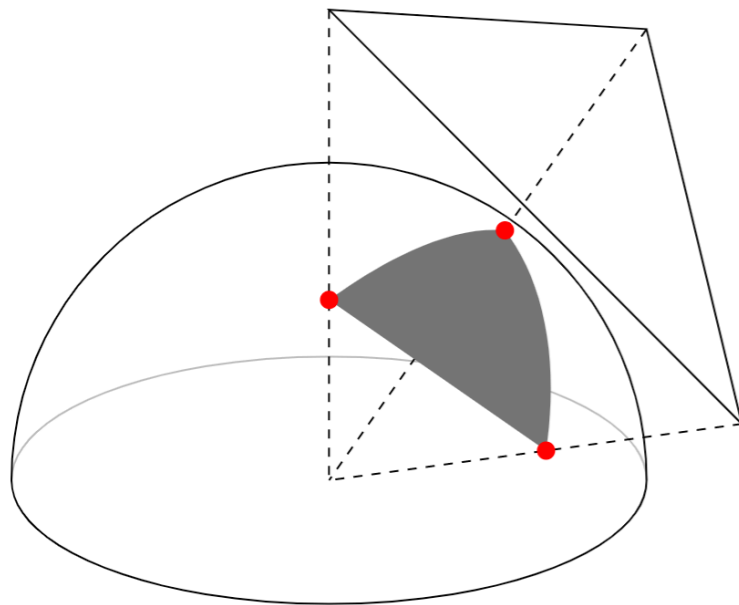
- Why visibility function V ?
 - Don't want to count surfaces behind the first



$$d\omega = \frac{dA \cos \theta}{r^2}$$

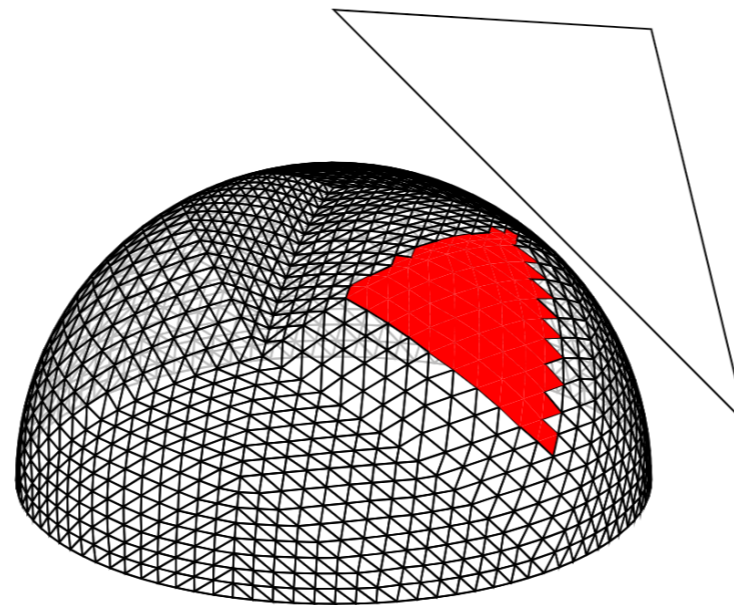
Cool visualisation by TA Pauli (link)

- Compares different ways of integrating same thing



s.a.(Triangle)
(from the [spherical excess](#) of angles)

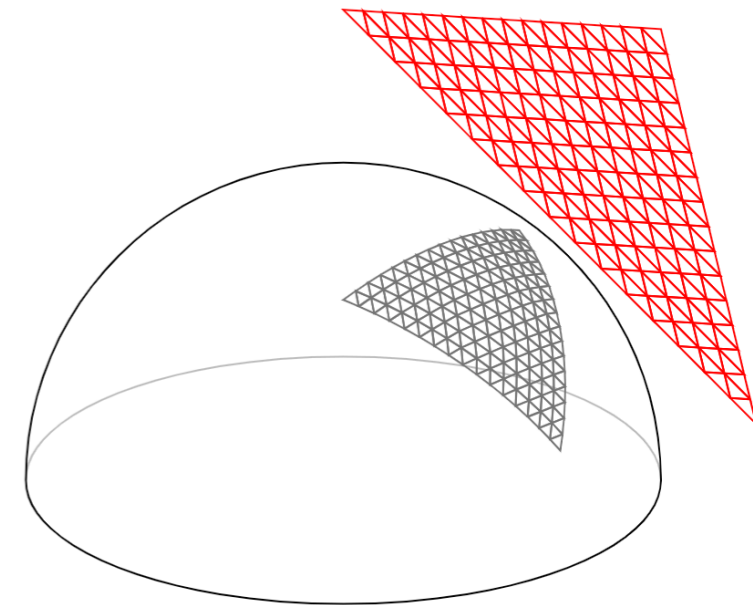
Direct evaluation: 0.3480304171399027sr



$\int V(w) dw$
(integral over hemisphere area)

Hemisphere discretization: 0.3585889439183479sr

Subdivide
Reset subdivision



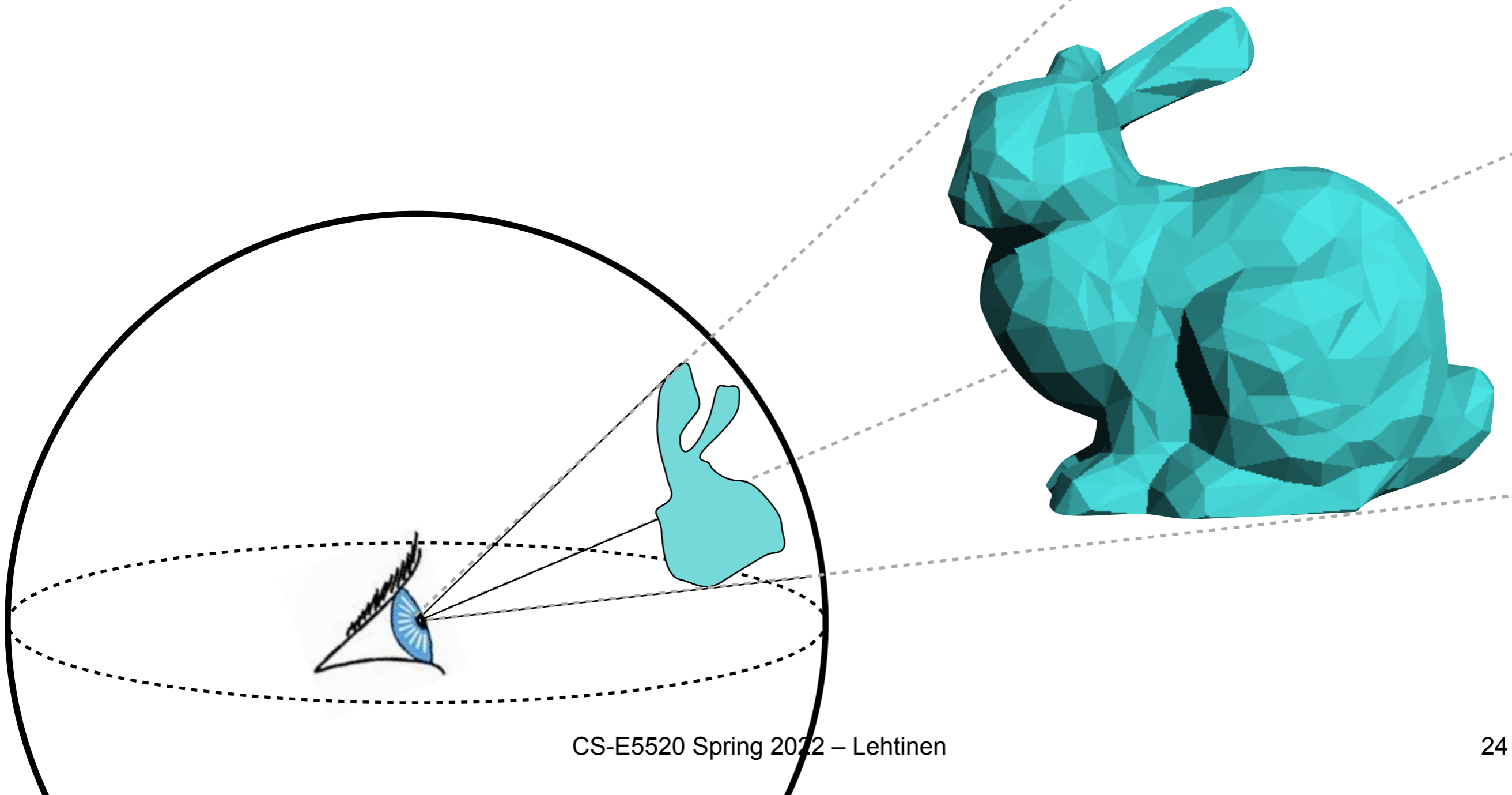
$\int V(A) \cos\theta/r^2 dA$
(integral over triangle area)

Area discretization: 0.34811299516831434sr

Subdivide
Reset subdivision

Remember: “How Big Something Looks”

- **Solid angle** \Leftrightarrow projected area on unit sphere



Don't be Scared of Integrals

- Think of Riemann sums from high school. Intuition:
 1. break the surface down into many, many tiny patches A_i
 2. evaluate integrand f at a point \mathbf{x}_i within each patch: $f(\mathbf{x}_i)$
 3. multiply by the area ΔA_i and then sum over all patches:

$$\sum_i f(\mathbf{x}_i) \Delta A_i$$

- Same holds for integrals over solid angle: they are just integrals over the surface of the sphere, that's all
 - Same logic applies: break sphere surface down to many tiny patches, sum them up

Area Integrals as Riemann Sums

- break the surface down into many, many tiny patches, evaluate the integrand, multiply by the area ΔA , and then sum over all patches

$$\text{s.a.} = \int_S \frac{[\cos \theta] V(x, y)}{r^2} dA$$

$$= \lim_{N \rightarrow \infty} \sum_{i=1}^N \frac{[\cos \theta] V(x, y)}{r^2} \Delta A$$

$[\cos \theta] = \max(0, \cos \theta)$ to rule out contributions from surface patches pointing away from the center

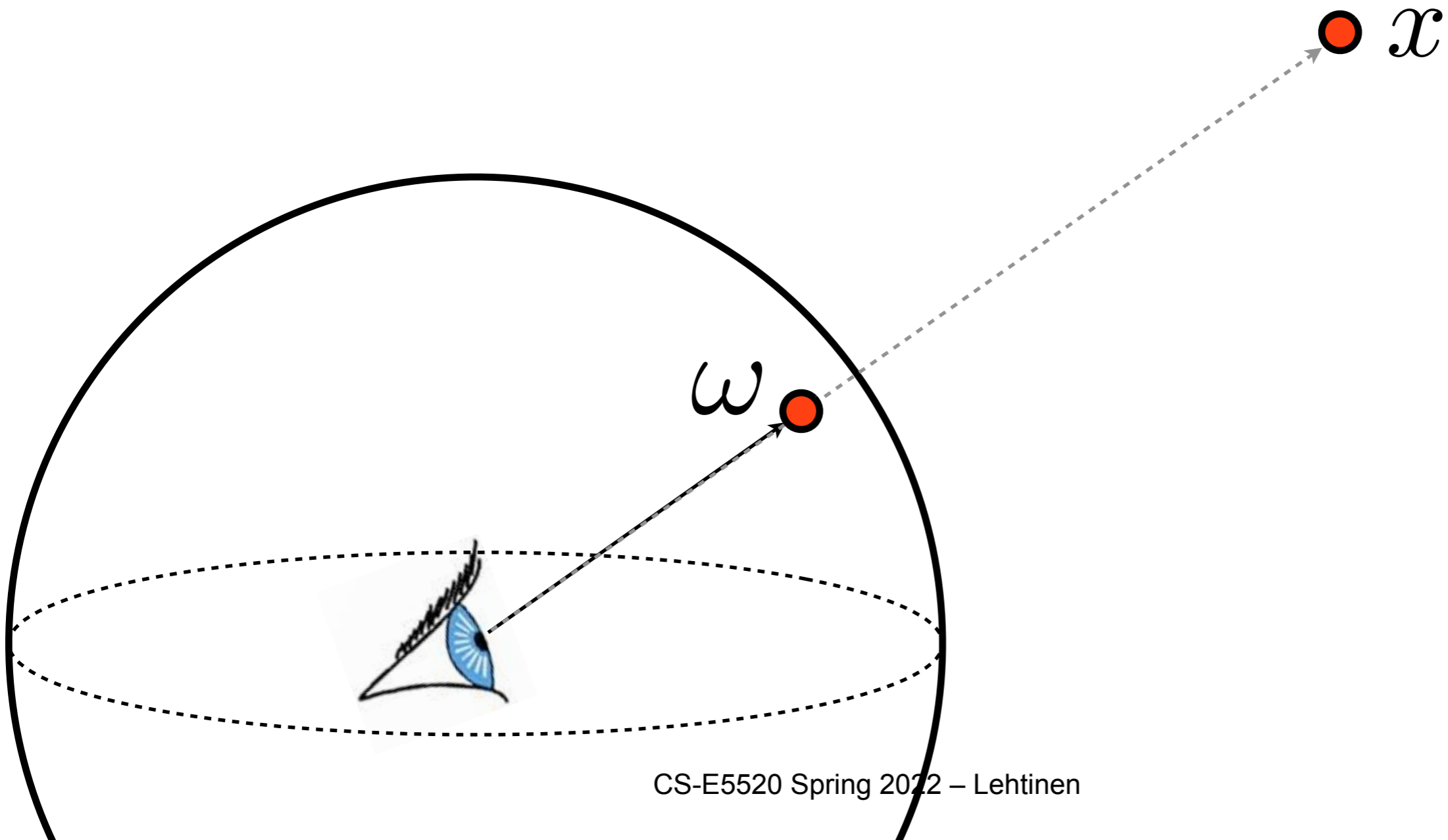
OK, Let's Explain the Intuition

- Take the lamp further away
=> **solid angle decreases**
=> illumination less powerful
- Tilt the lamp away from yourself
=> **solid angle decreases**
=> illumination less powerful
- But all the time, the points on the lamp are ~constant “brightness”!



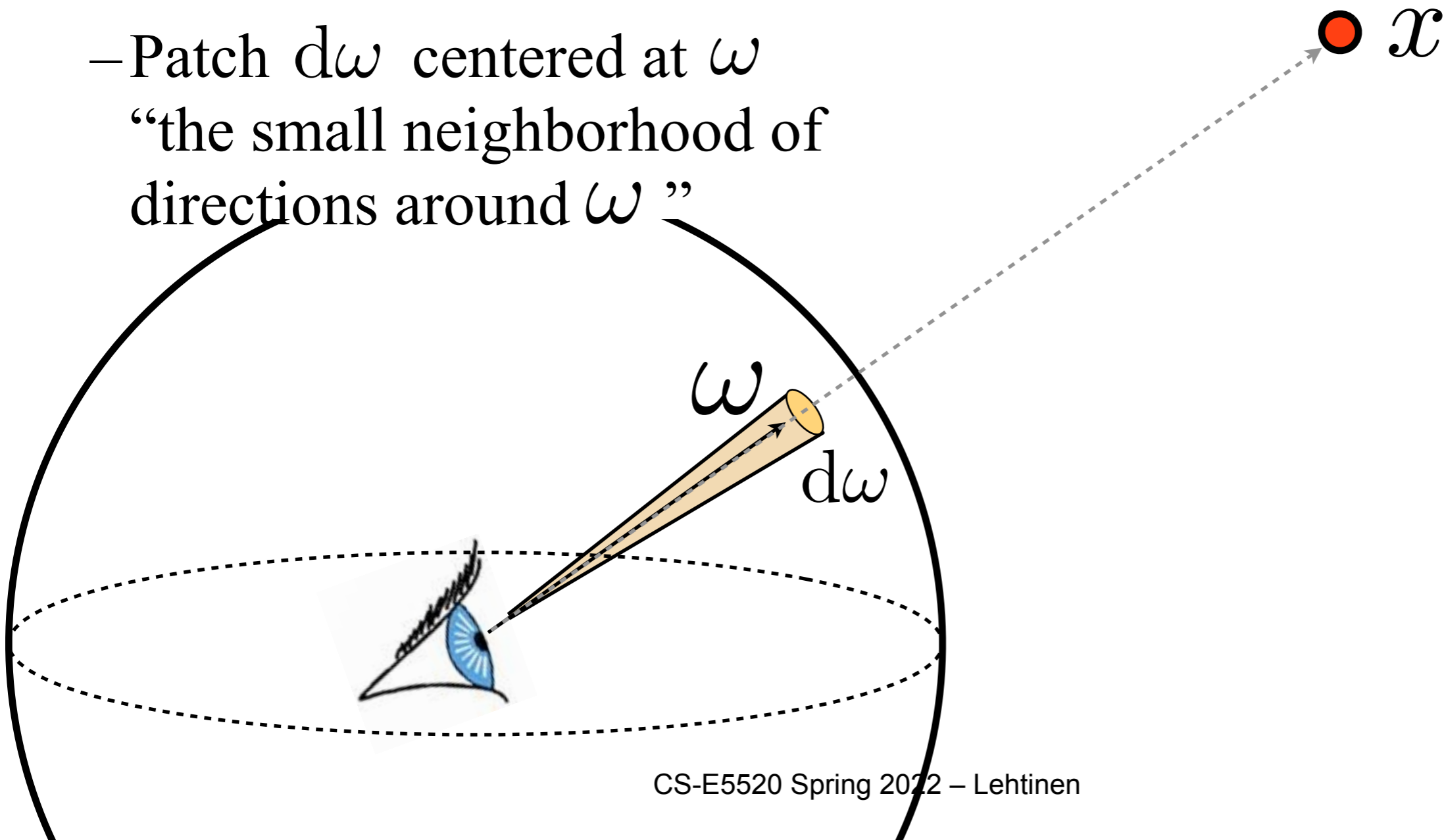
Points on Sphere also Encode Direction

- Point on unit sphere \Leftrightarrow direction
 - Just as with usual angles in the plane
 - “Point x is in direction ω ”



Points on Sphere also Encode Direction

- Point on unit sphere \Leftrightarrow direction
 - Just as with usual angles in the plane
 - “Point x is in direction ω ”
 - Patch $d\omega$ centered at ω
“the small neighborhood of directions around ω ”



Questions?

Assumptions

- We assume the Ray Optics Model
 - Also called geometric optics
 - Disregard quantum phenomena like diffraction
 - Rendering optical disks is hard :)
 - Basically, assume scene features are “large” w.r.t. wavelength
 - Assume wavelengths are separate
 - No energy transfer between frequencies (fluorescence)
=> a photon does not change its energy, only gets scattered and absorbed
 - In principle: carry out computations separately for each wavelength
 - Usually in practice: do separate calculations for R, G, B
 - Usually, don't care about much polarization

How to Measure Light?

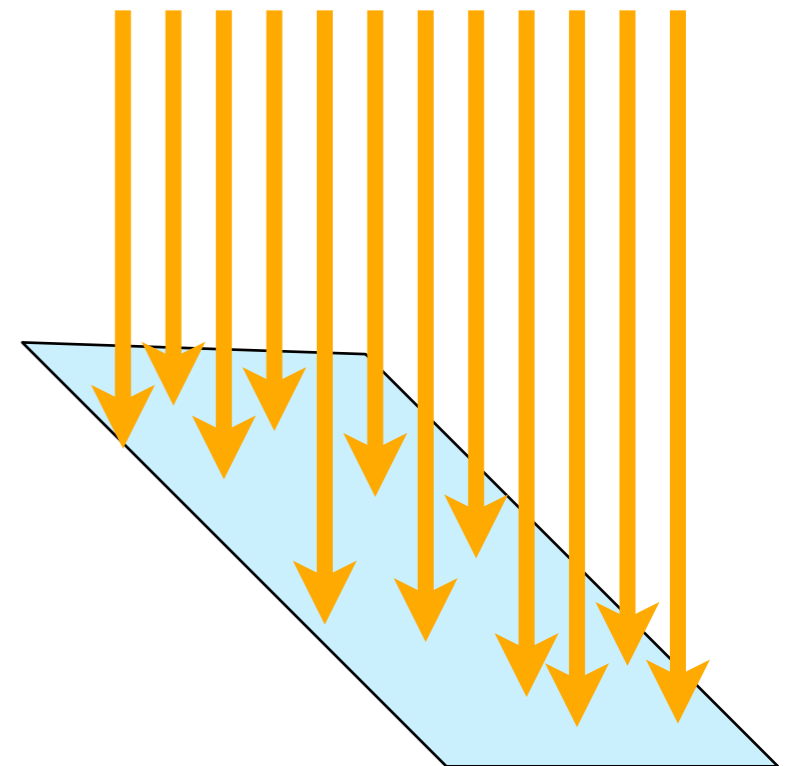
- Geometric optics assumes light energy is a continuum defined over continuous area and angle measurements
 - Basically: how much “stuff” flows in a certain area and direction
- Not incompatible with photons
 - We can think of measuring how many photons land on a small surface from a tiny set of directions in a second
 - Each photon carries some constant energy (depending on its wavelength), so [photons/second] \Leftrightarrow [J/s] = [W]
 - Power carried by light is called **flux**, denoted Φ

A Little More Formally: Irradiance

- **Irradiance** E is the flux Φ [W] per unit area [$1/m^2$] landing on a surface

$$E = \frac{d\Phi}{dA} \quad \left[\frac{W}{m^2} \right]$$

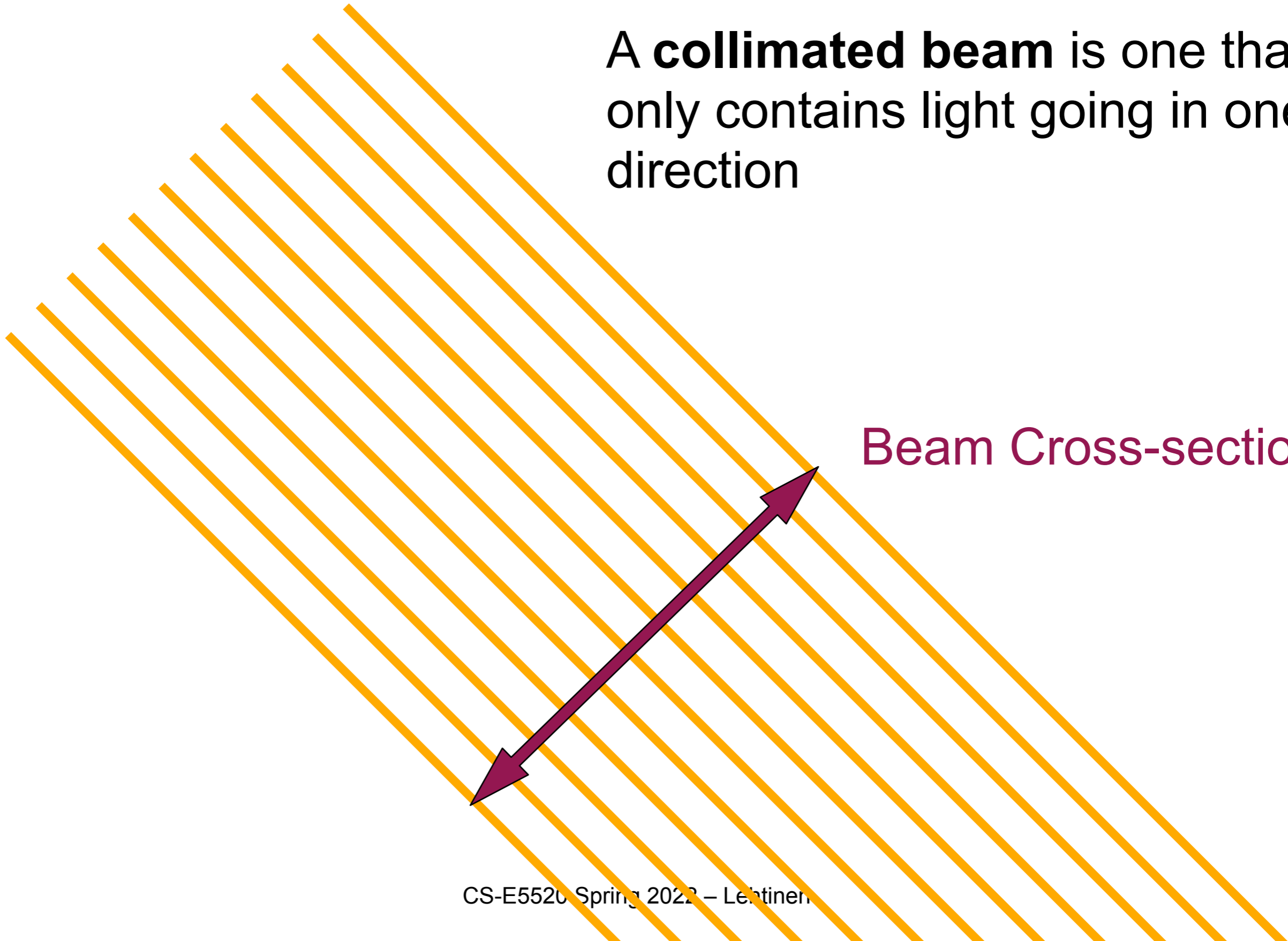
- You can really think of counting photons
- (Brightness of diffuse surface determined directly by irradiance)
 - (We'll come to this in a bit)



Beam Power

A **collimated beam** is one that only contains light going in one direction

Beam Cross-section A

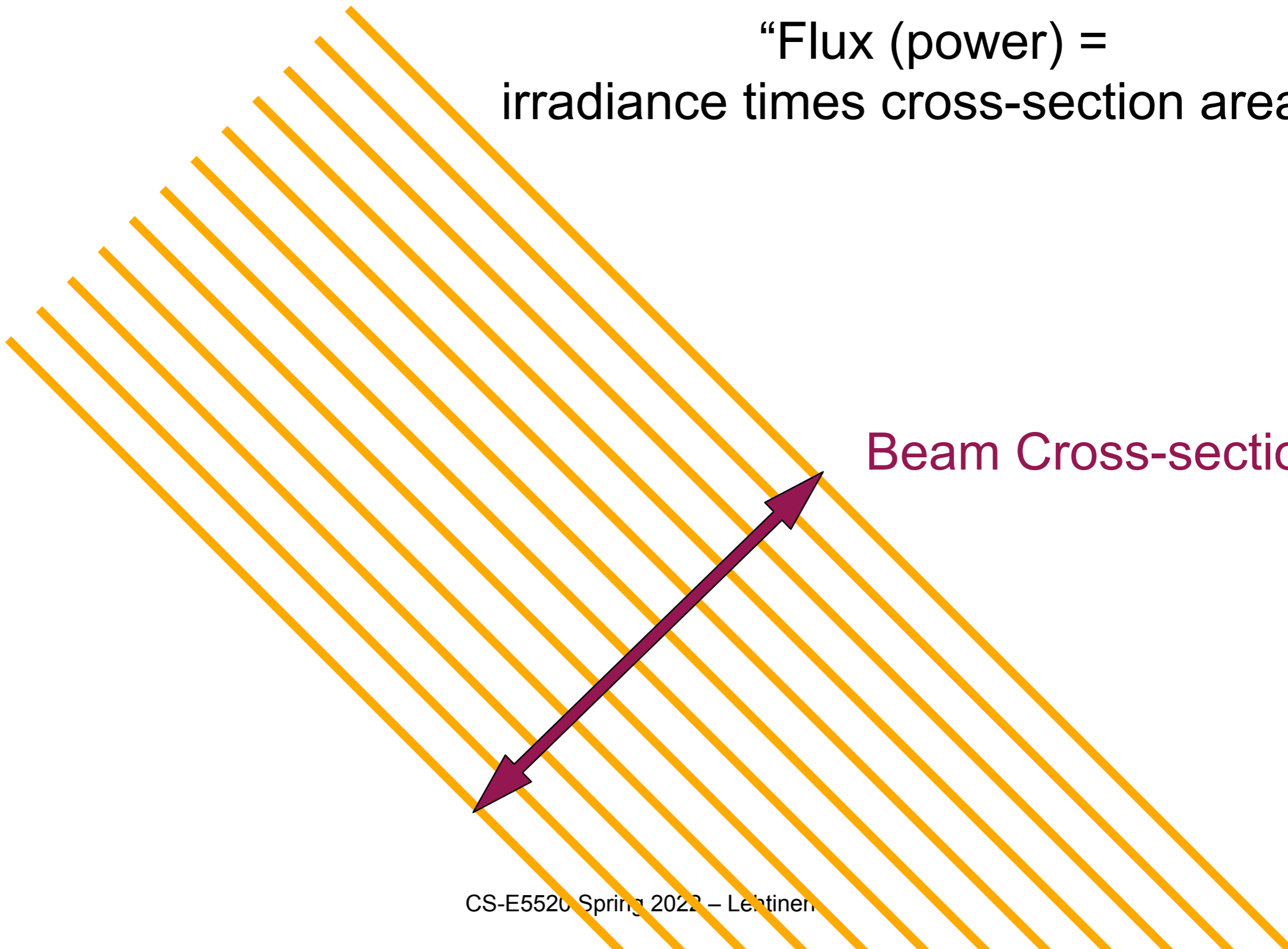


Beam Power

$$\Phi = EA$$

“Flux (power) =
irradiance times cross-section area”

Beam Cross-section A



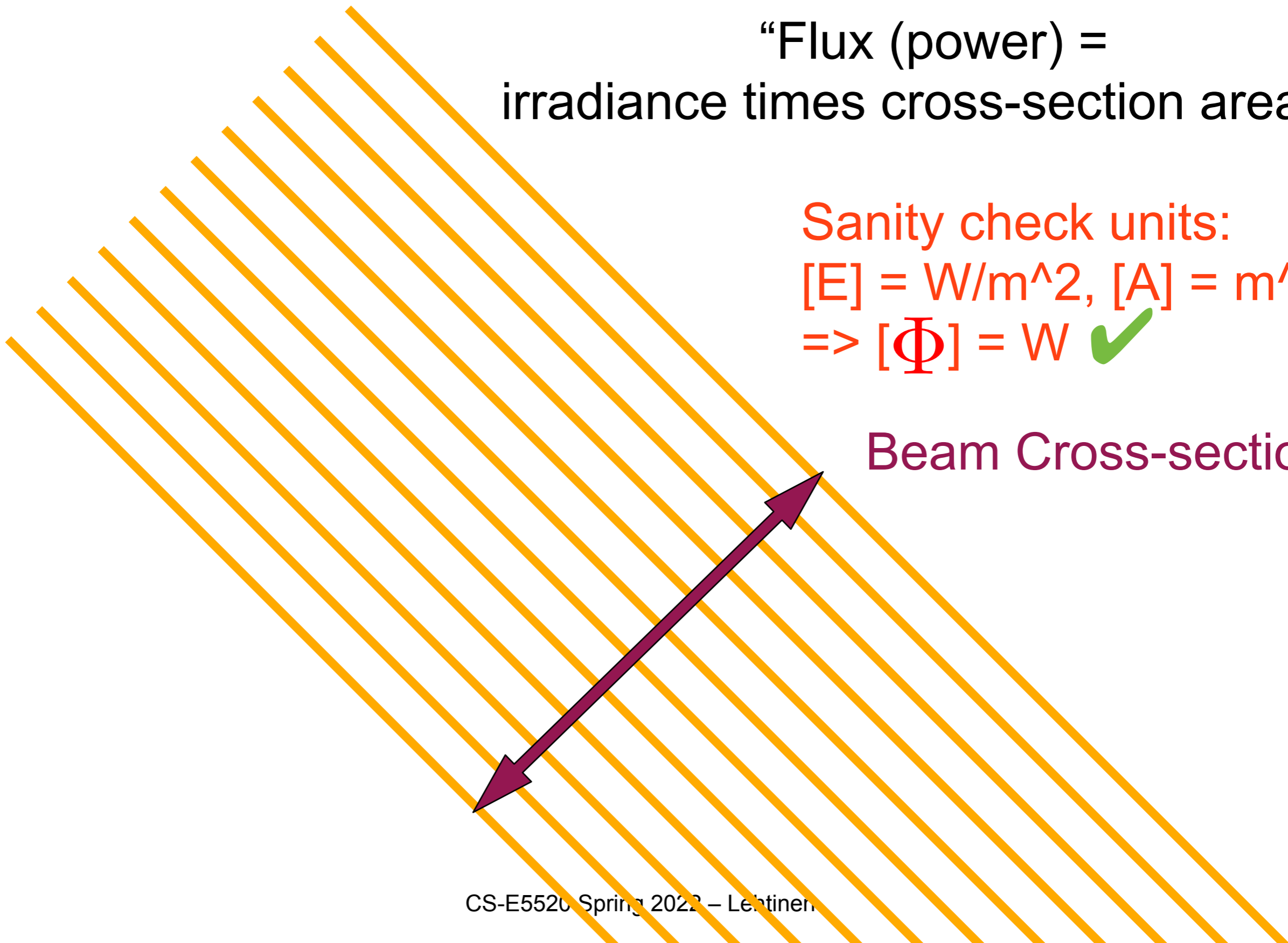
Beam Power

$$\Phi = EA$$

“Flux (power) = irradiance times cross-section area”

Sanity check units:
[E] = W/m², [A] = m²
=> [Φ] = W ✓

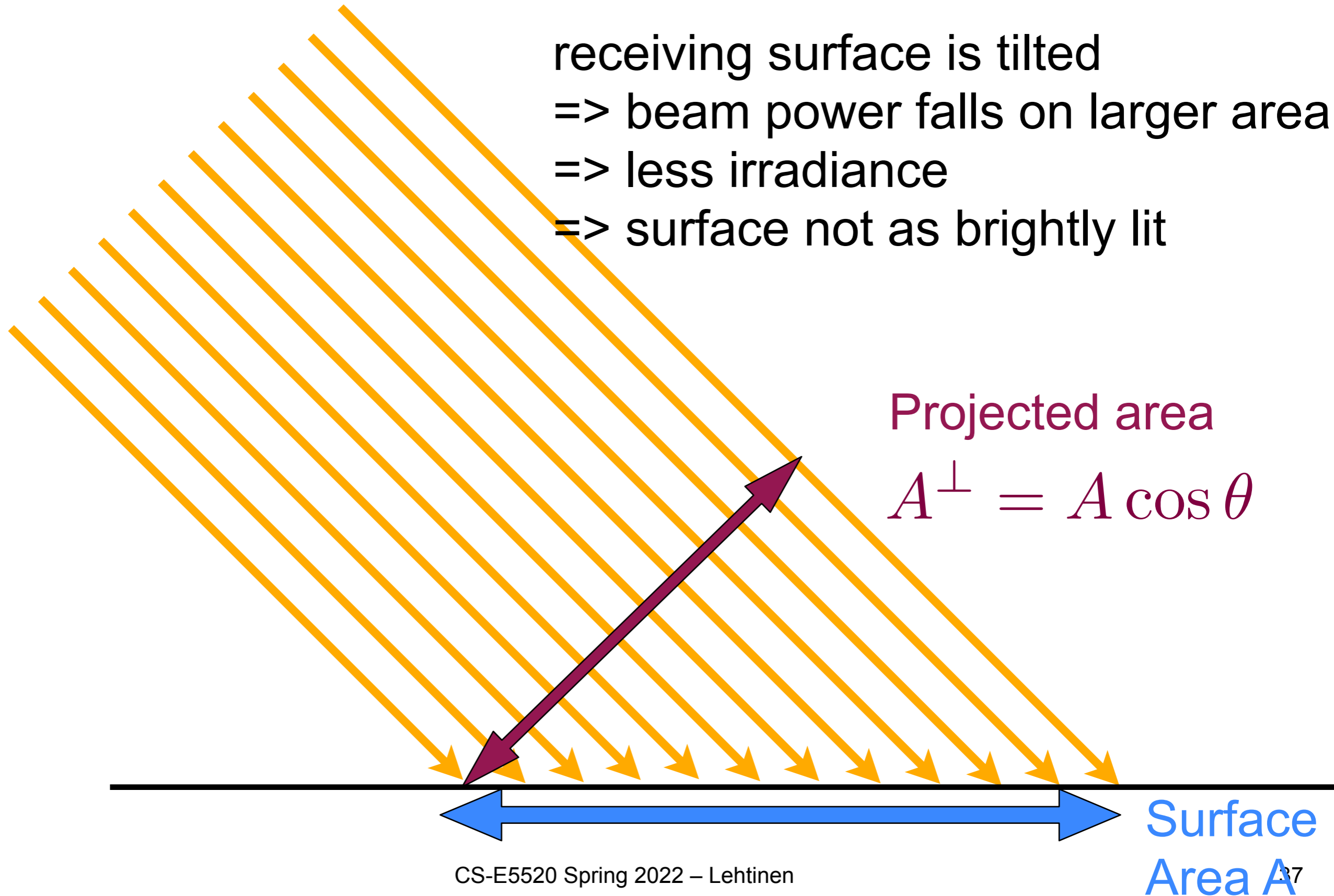
Beam Cross-section A



Projected Area and Irradiance

receiving surface is tilted
=> beam power falls on larger area
=> less irradiance
=> surface not as brightly lit

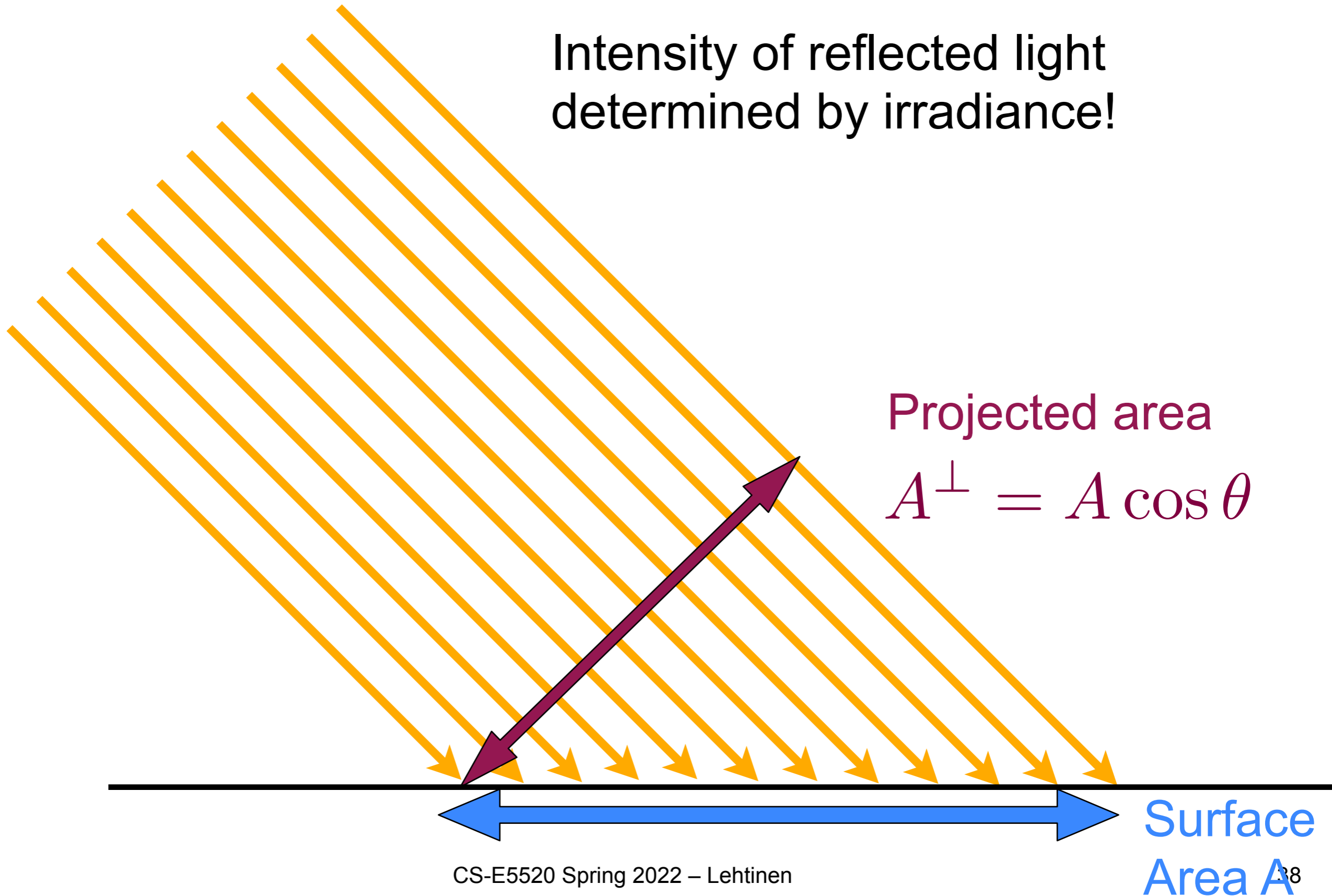
Projected area
 $A^\perp = A \cos \theta$



Projected Area and Irradiance

Intensity of reflected light
determined by irradiance!

Projected area
 $A^\perp = A \cos \theta$



That's Not the Whole Story

- Clearly, light is rarely collimated
- Clearly, there is light everywhere going to every direction



Radiance

- **Radiance** is the fundamental quantity that simultaneously explains effects of both light source size and receiver orientation

Radiance

- Let's consider a tiny almost-collimated beam of cross-section $dA^\perp = dA \cos \theta$ where the directions are all within a differential angle $d\omega$ of each other



Radiance

- Radiance L =
flux per unit projected area
per unit solid angle

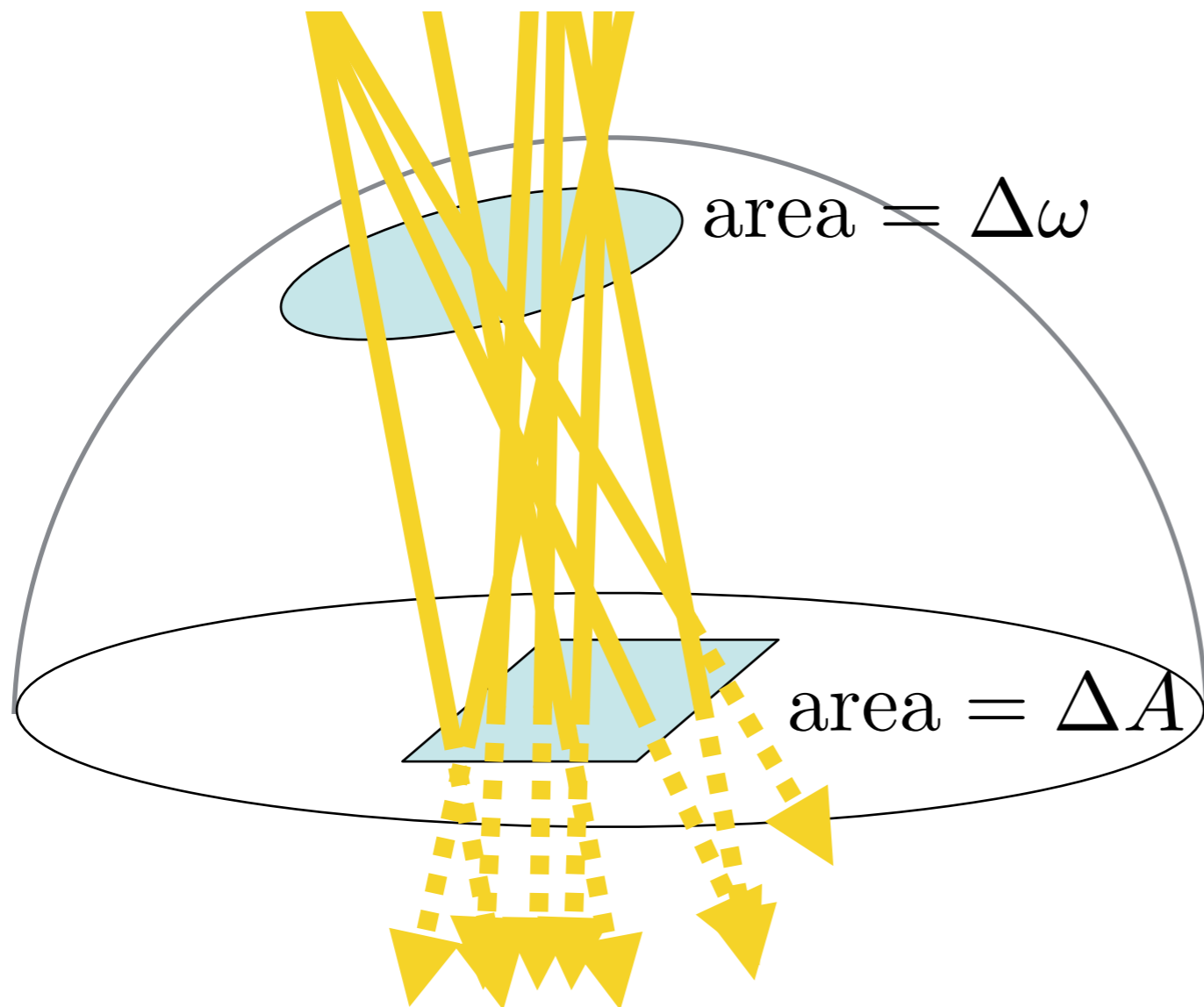
$$L = \frac{d\Phi}{dA^\perp d\omega}$$

$$[L] = \left[\frac{W}{m^2 sr} \right]$$



Radiance, intuitively

- Let's count energy packets, each ray carries the same $\Delta\Phi$

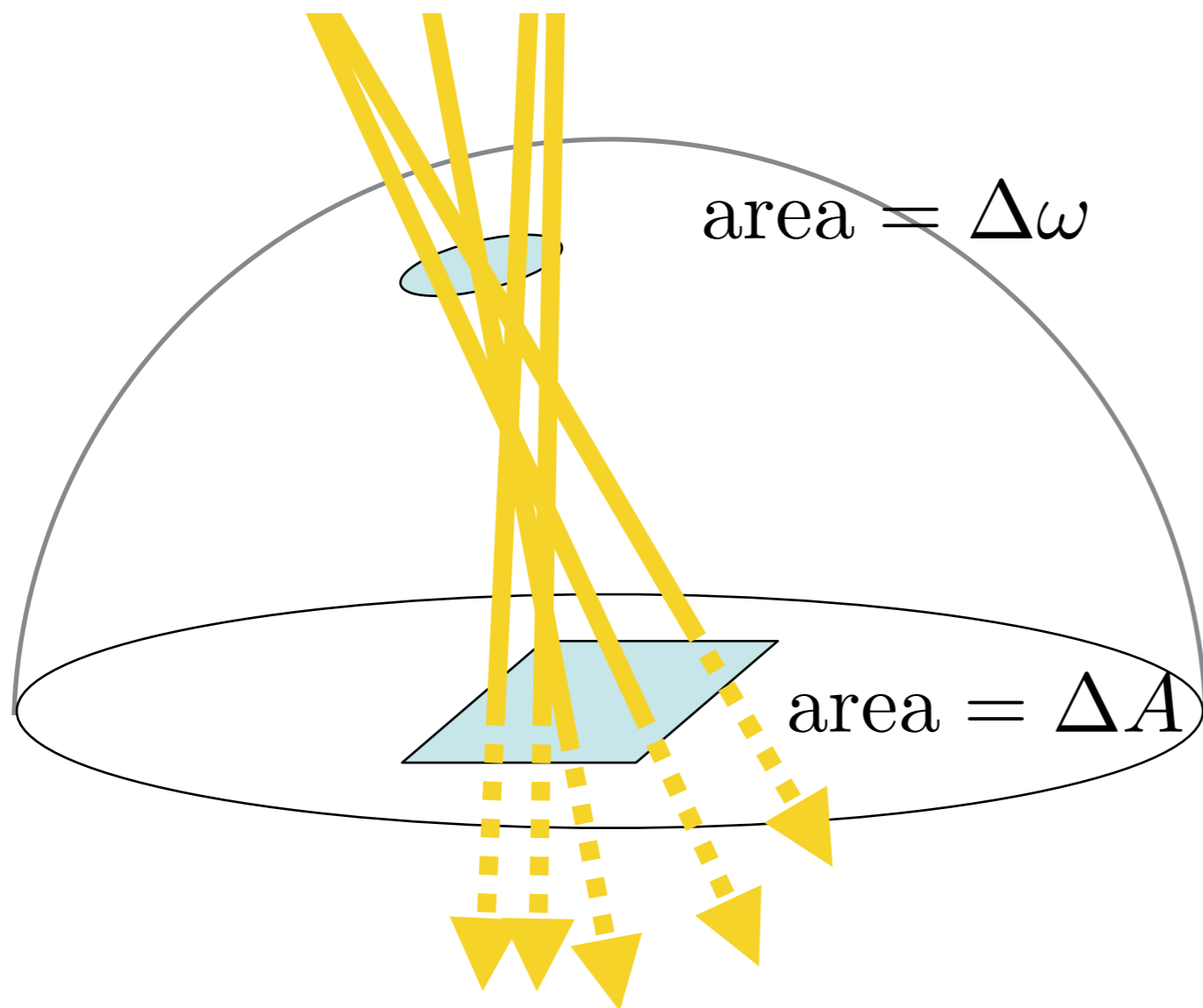


$$L = \frac{d\Phi}{dA^\perp d\omega}$$

$$[L] = \left[\frac{W}{m^2 sr} \right]$$

Radiance, intuitively

- Smaller solid angle \Rightarrow
fewer rays \Rightarrow less energy

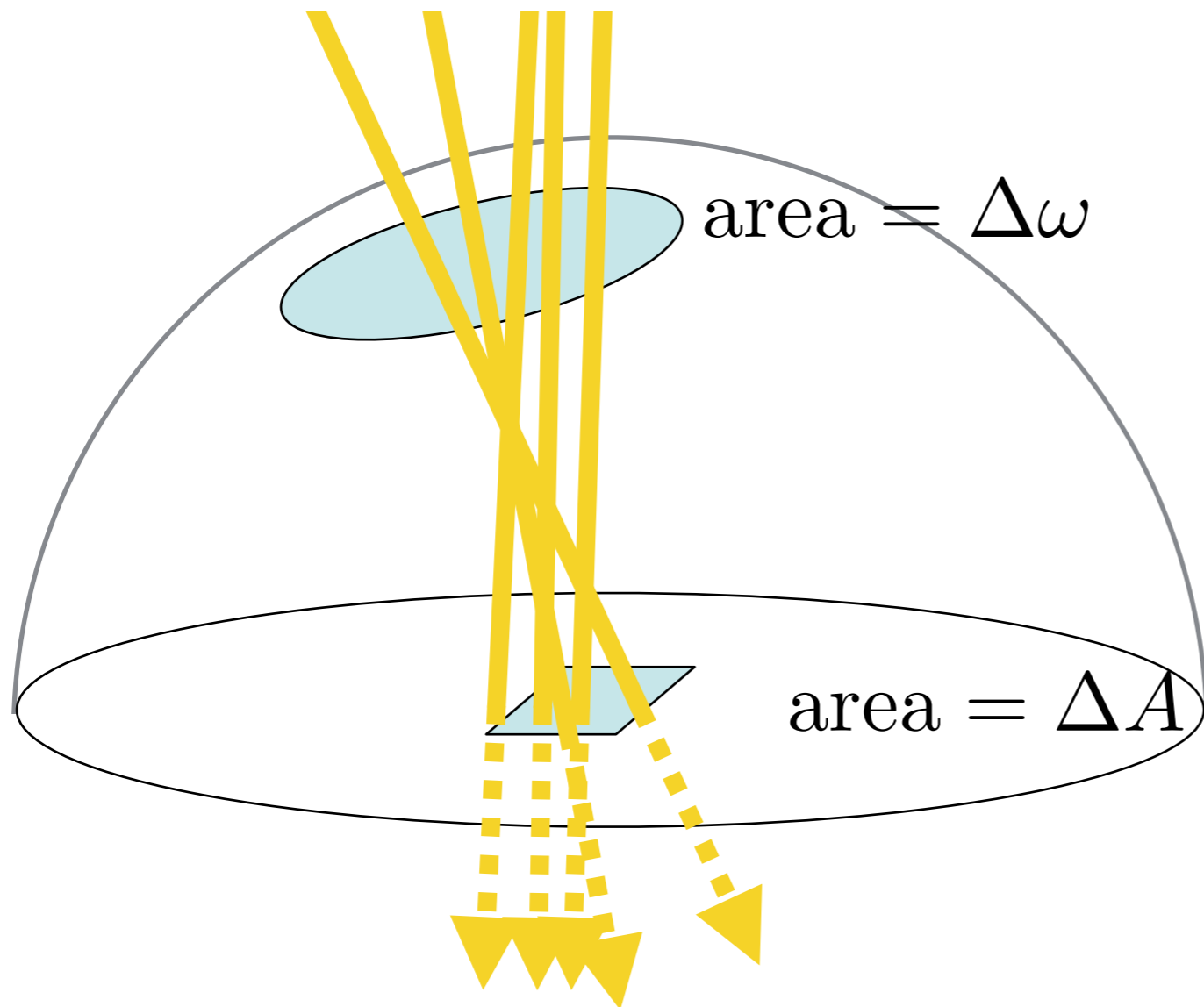


$$L = \frac{d\Phi}{dA^\perp d\omega}$$

$$[L] = \left[\frac{W}{m^2 sr} \right]$$

Radiance, intuitively

- Smaller projected surface area
=> fewer rays => less energy



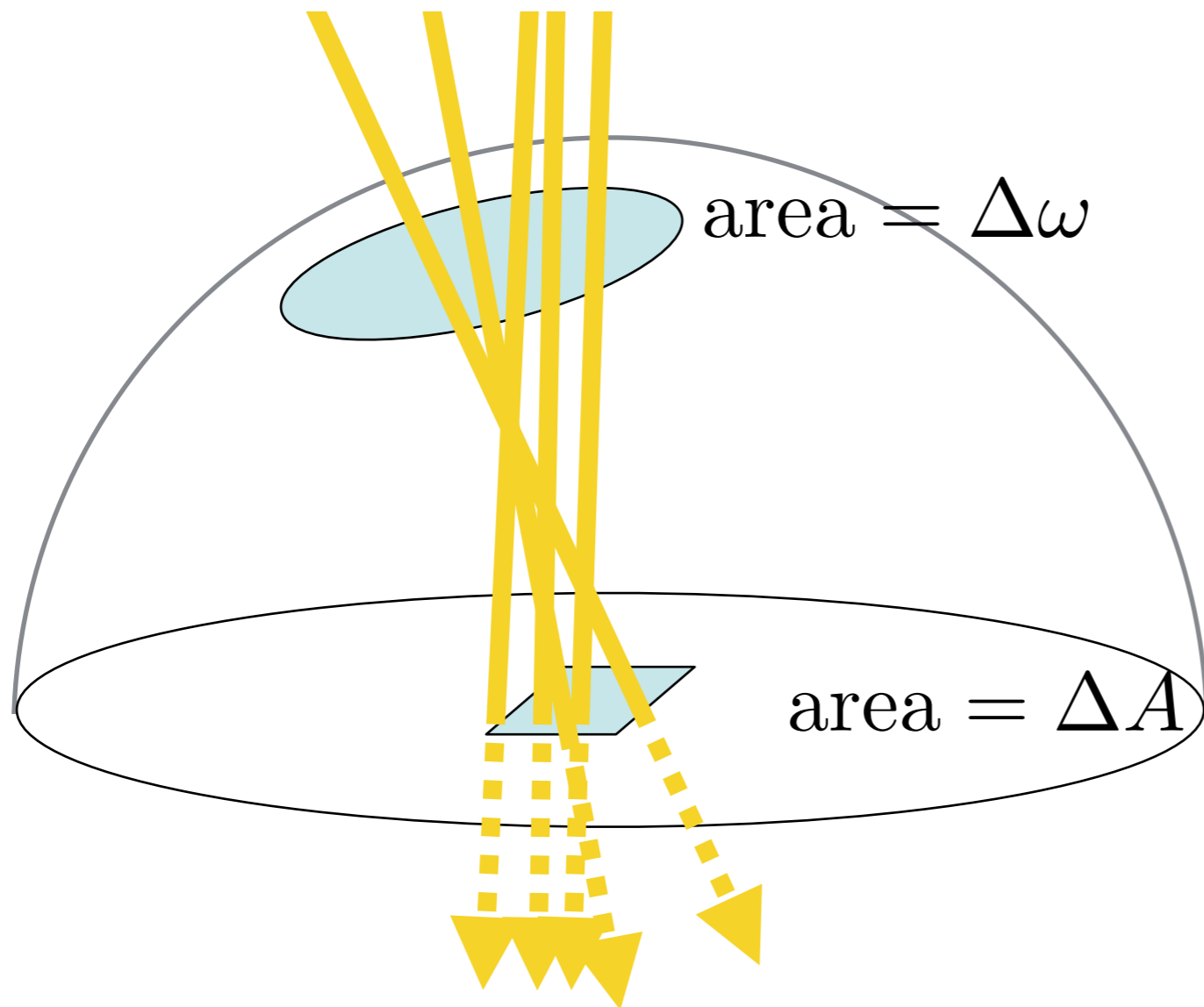
$$L = \frac{d\Phi}{dA^\perp d\omega}$$

$$[L] = \left[\frac{W}{m^2 sr} \right]$$

Radiance, intuitively

- I.e., *radiance is a density over both space and angle*

$$L = \frac{d\Phi}{dA^\perp d\omega}$$



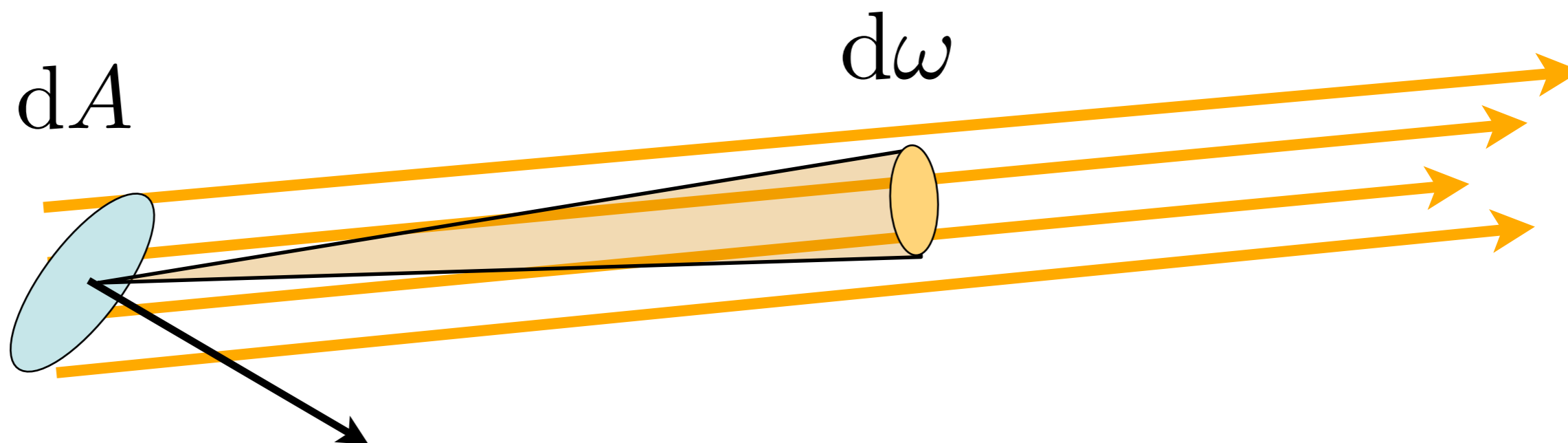
Radiance

- **Sensors are sensitive to radiance**
 - It's what you assign to pixels
 - The fundamental quantity in image synthesis
- “Intensity does not attenuate with distance”
<=> radiance stays constant along straight lines**
- **All relevant quantities (irradiance, etc.) can be derived from radiance**

**unless the medium is participating, e.g., smoke, fog

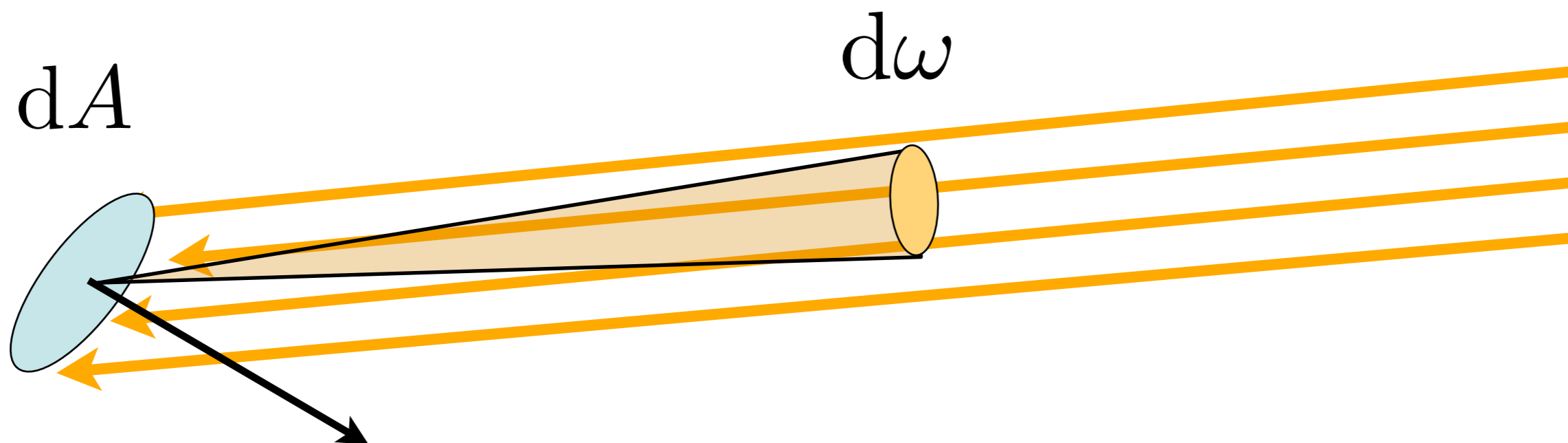
Radiance

- Characterizes
 - Lighting that leaves a surface patch dA to a given direction
 - Lighting that impinges dA from a given direction
 - Just flip direction



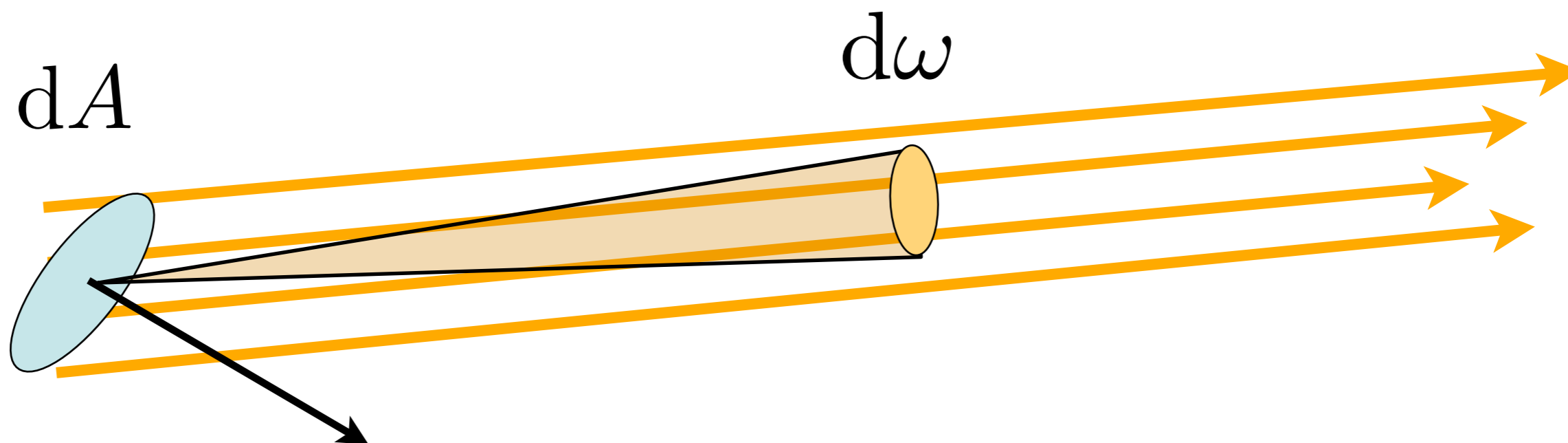
Radiance

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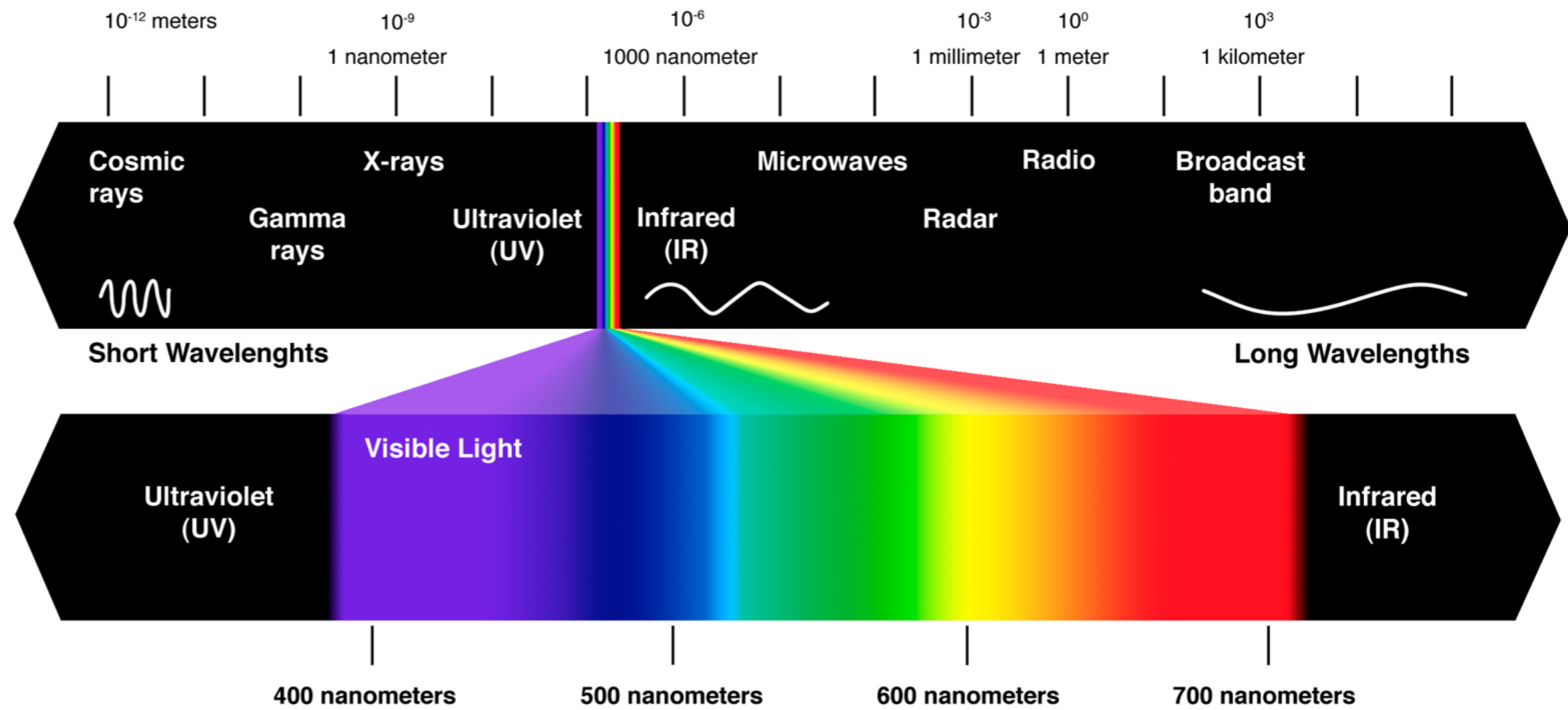
Radiance

- Also empty space, away from surfaces
 - Radiance $L(x, \omega)$, when taken as a 5D function of position (3D) and direction (2D) completely nails down the light flow in a scene
 - Sometimes called the “plenoptic function”



A Word on Color

- Spectral radiance $L(x, \omega, \lambda)$ is the radiance in a small band $d\lambda$ of wavelengths
- You get the total energy by integrating over the visible range



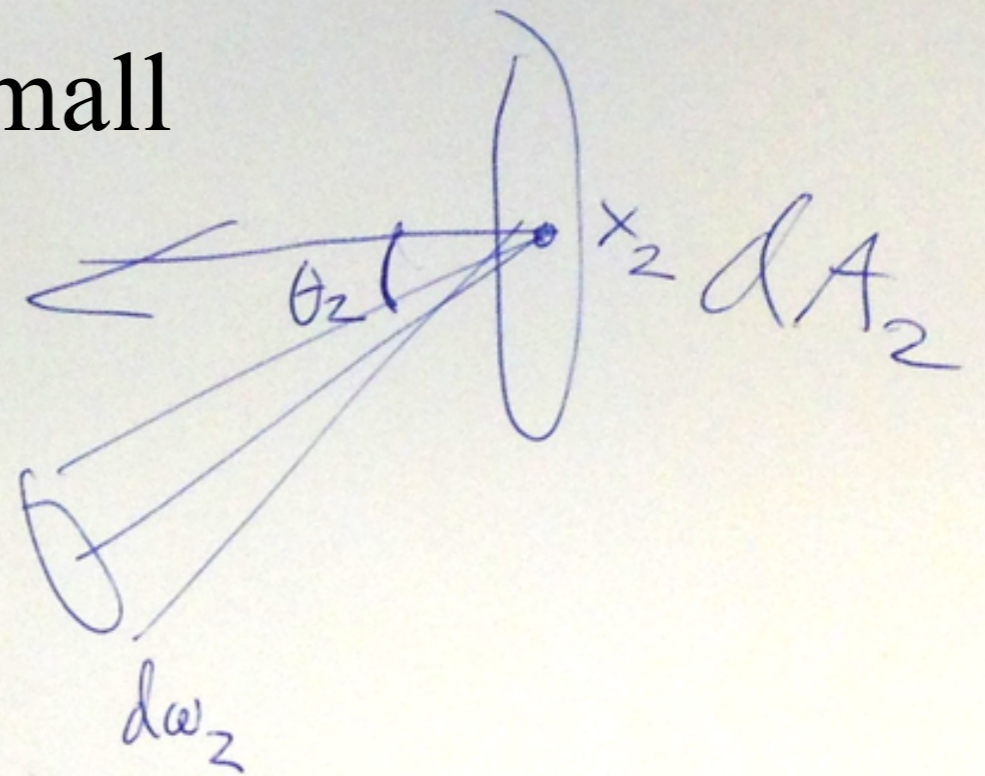
About Color

- We'll mostly not talk about it in this class
- But not difficult to do “right”
- See e.g. Chapter 5 in the excellent Physically Based Rendering: From Theory to Implementation, 3rd ed.



Constancy Along Straight Lines

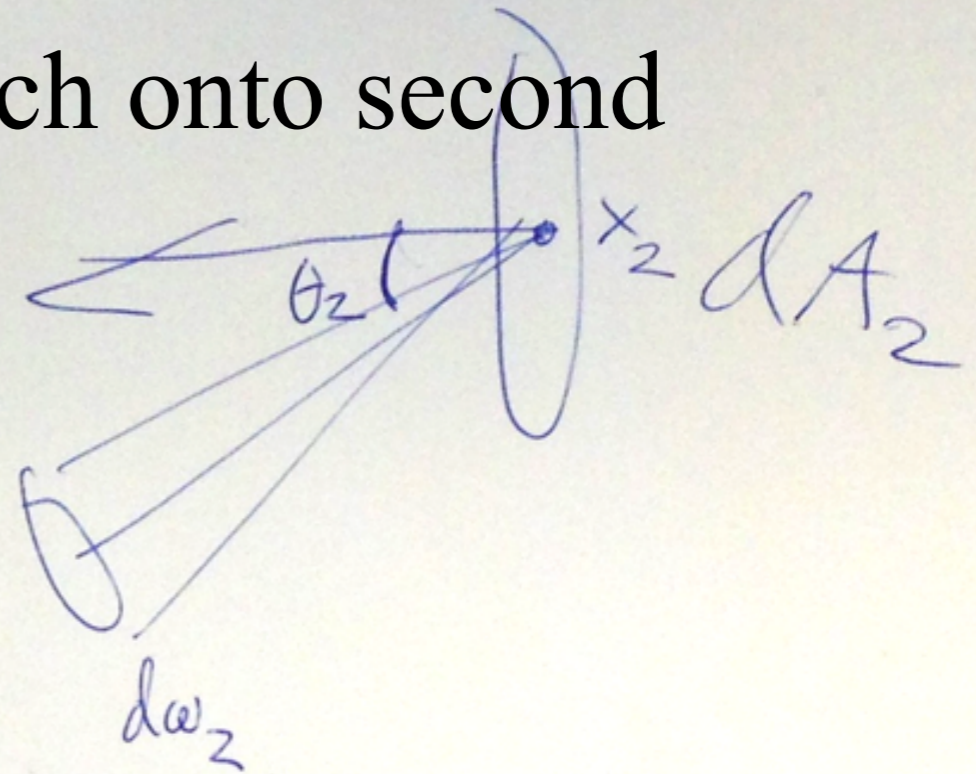
- Let's look at the flux sent by a small patch onto another small patch



Constancy Along Straight Lines

- Differential flux sent by first patch onto second

$$L = \frac{d\Phi}{dA^\perp d\omega}$$



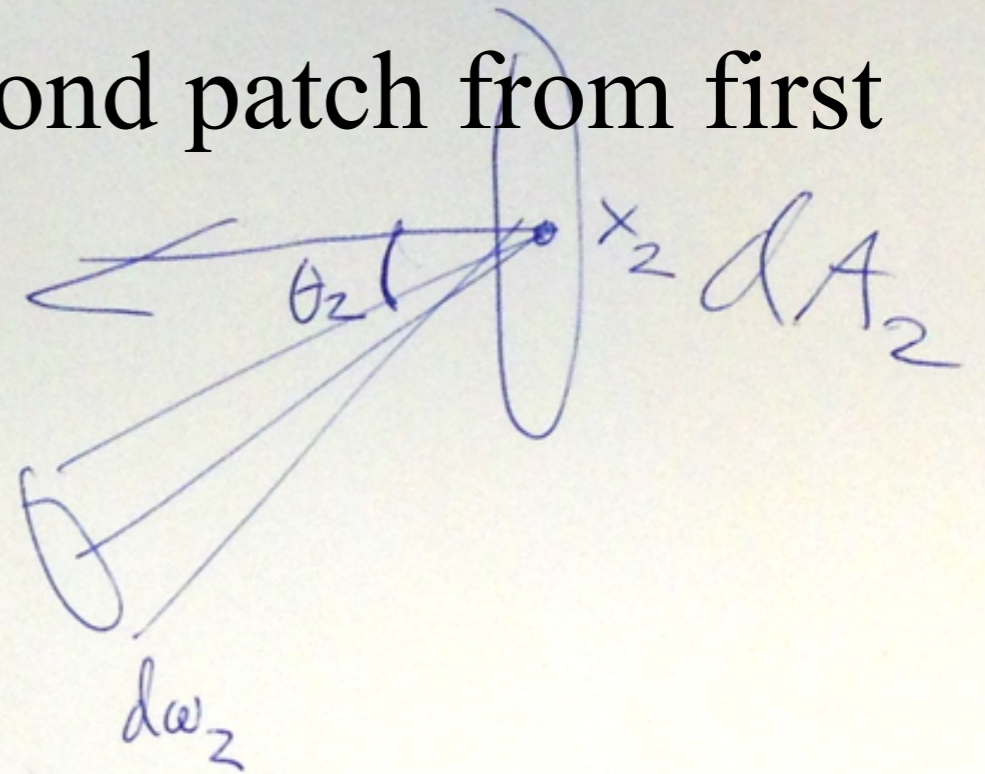
Solid angle $d\omega_1$ subtended by dA_2 as seen from dA_1

$$d\Phi = L(x_1 \rightarrow \omega_1) \overbrace{\cos \theta_1 dA_1}^{dA_1^\perp} \frac{dA_2 \cos \theta_2}{r^2}$$

Constancy Along Straight Lines

- Differential flux received by second patch from first

$$L = \frac{d\Phi}{dA^\perp d\omega}$$



Solid angle $d\omega_2$ subtended by dA_1 as seen from dA_2

$$d\Phi = L(x_2 \leftarrow \omega_2) \overbrace{\cos \theta_2 dA_2}^{dA_2^\perp} \frac{dA_1 \cos \theta_1}{r^2}$$

Eureka

$$d\Phi = L(x_2 \leftarrow \omega_2) \cos \theta_2 dA_2 \frac{dA_1 \cos \theta_1}{r^2}$$

$$d\Phi = L(x_1 \rightarrow \omega_1) \cos \theta_1 dA_1 \frac{dA_2 \cos \theta_2}{r^2}$$

Eureka

- Radiance is constant along straight lines
 - I.e. radiance sent by dA_1 into the direction of dA_2 is the same as radiance received by dA_2 from the direction of dA_1 .
- This is why the lamp appears “as bright” no matter how far you look at it from

$$\Rightarrow L(x_1 \rightarrow \omega_1) = L(x_2 \leftarrow \omega_2)$$

Rendering \Leftrightarrow

what is the radiance hitting my sensor?

Let's Look at Irradiance Again

- Remember, irradiance is radiant power landing on a surface per unit area (from all directions)
 - So far we only looked at tiny collimated beams

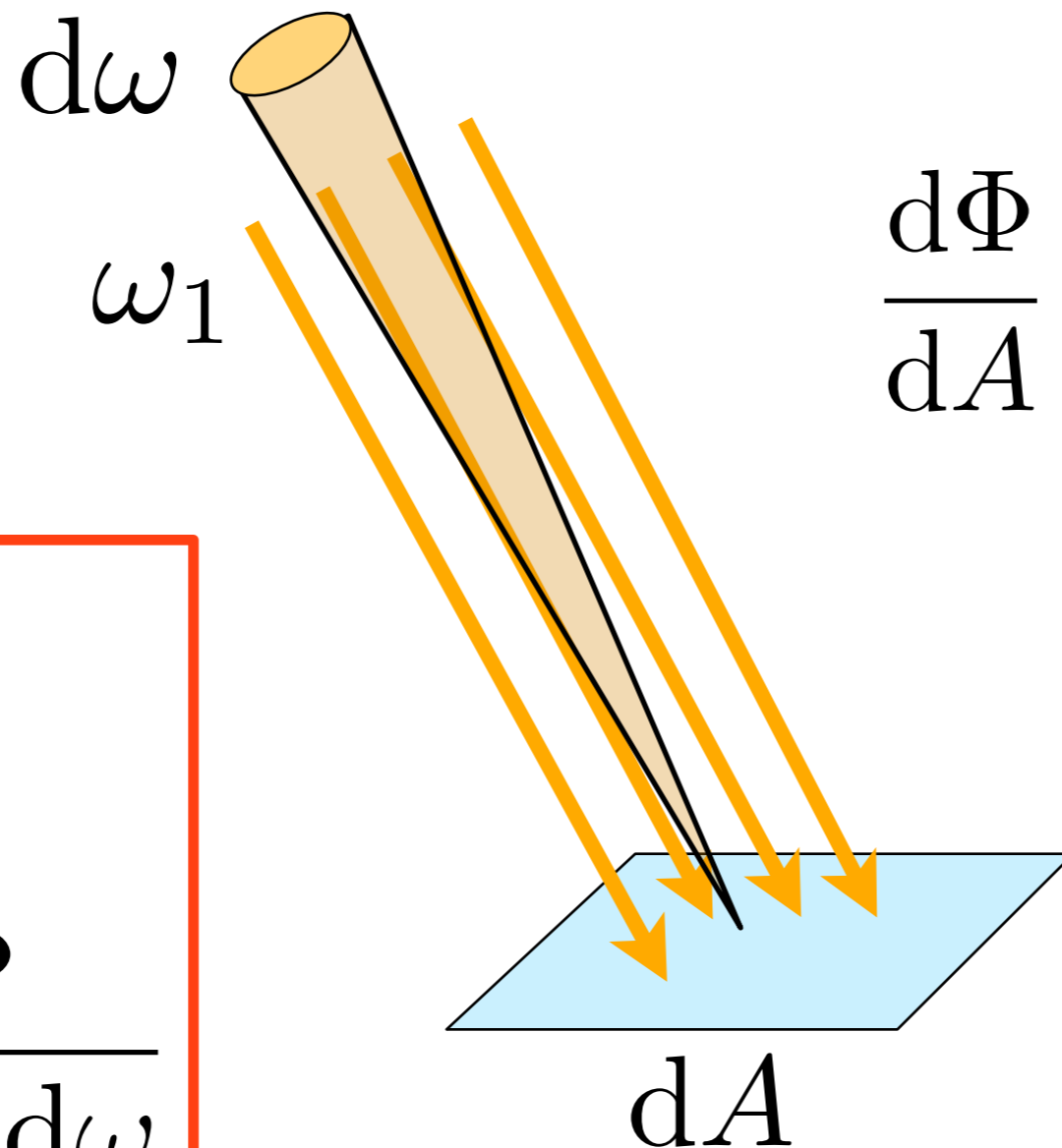
$$E = \frac{d\Phi}{dA} \quad \left[\frac{W}{m^2} \right]$$



dA

Let's Look at Irradiance Again

- Let's count irradiance, add up the radiance from all the differential beams from all directions



$$\frac{d\Phi}{dA} = L(\omega_1) \cos \theta d\omega$$

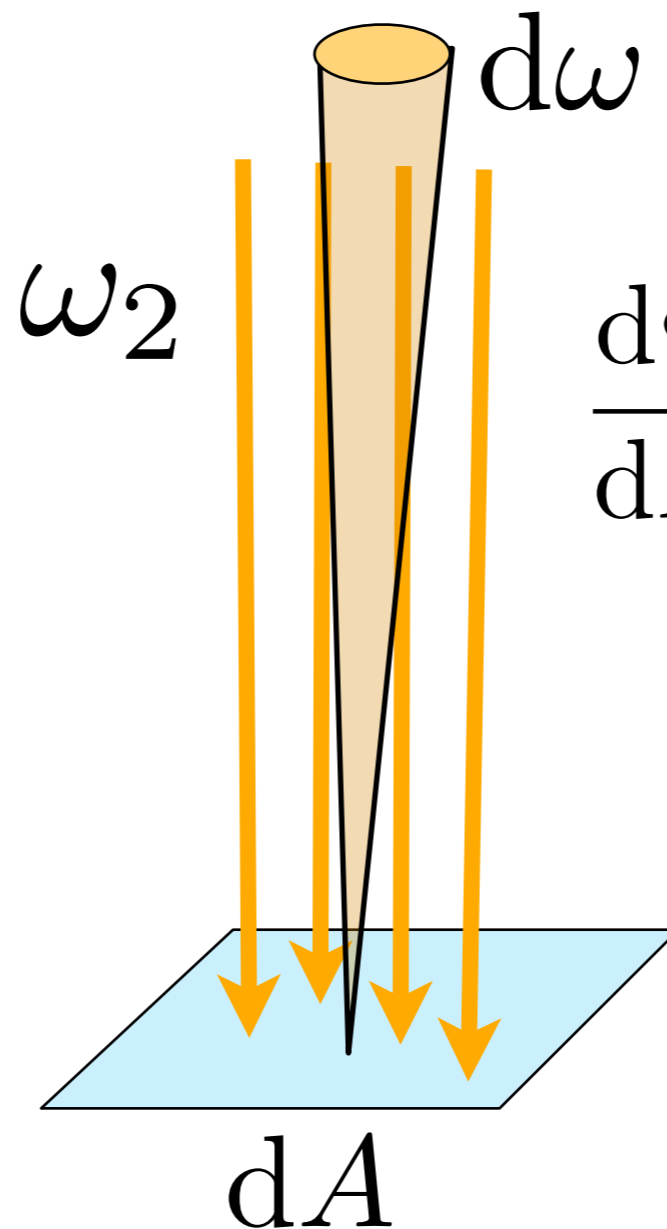
$$E = \frac{d\Phi}{dA}$$

$$L = \frac{d\Phi}{dA^\perp d\omega}$$

Remember: omega is a single direction, dw is the small solid angle around it

Let's Look at Irradiance Again

- Let's count irradiance, add up the radiance from all the differential beams from all directions



$$\frac{d\Phi}{dA} = L(\omega_2) \cos \theta d\omega$$

$$E = \frac{d\Phi}{dA}$$

$$L = \frac{d\Phi}{dA^\perp d\omega}$$

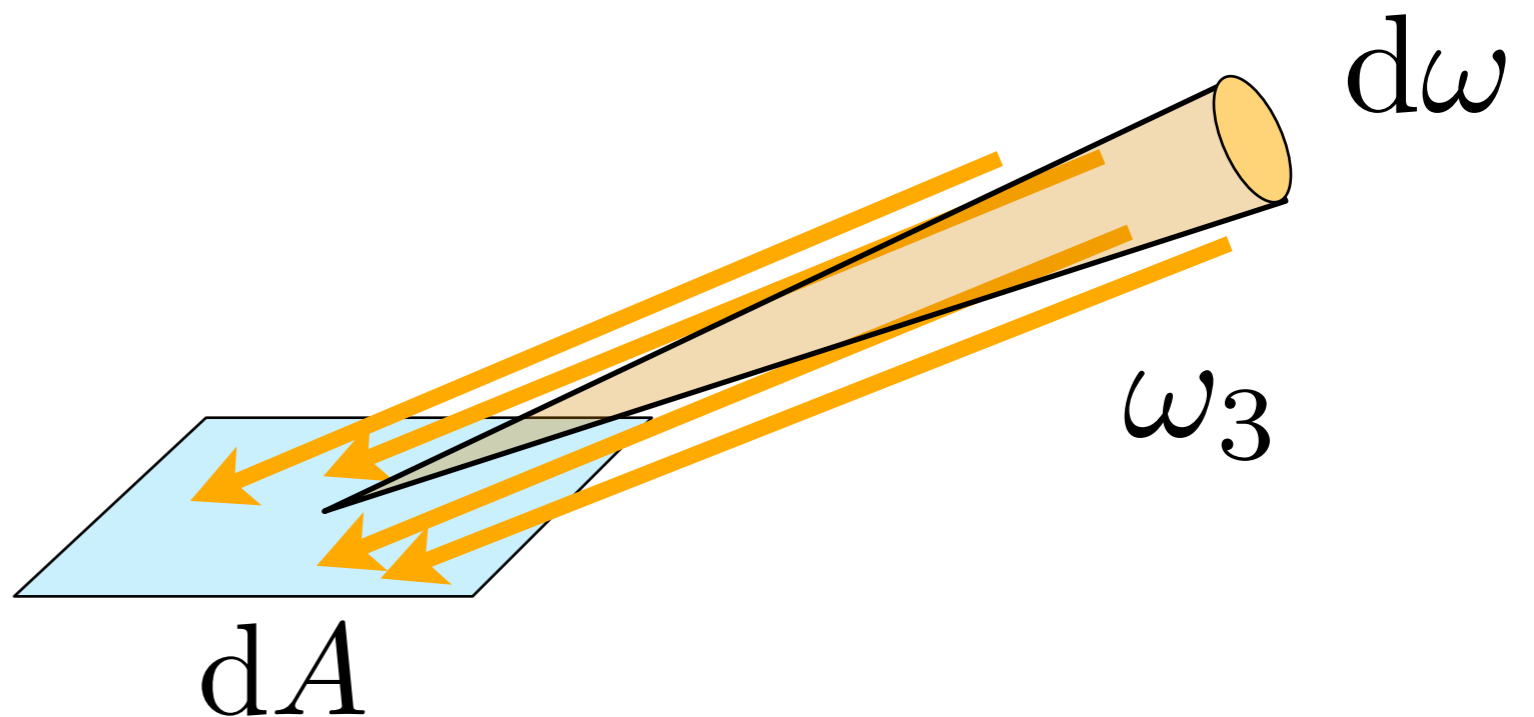
This Happens for All Directions

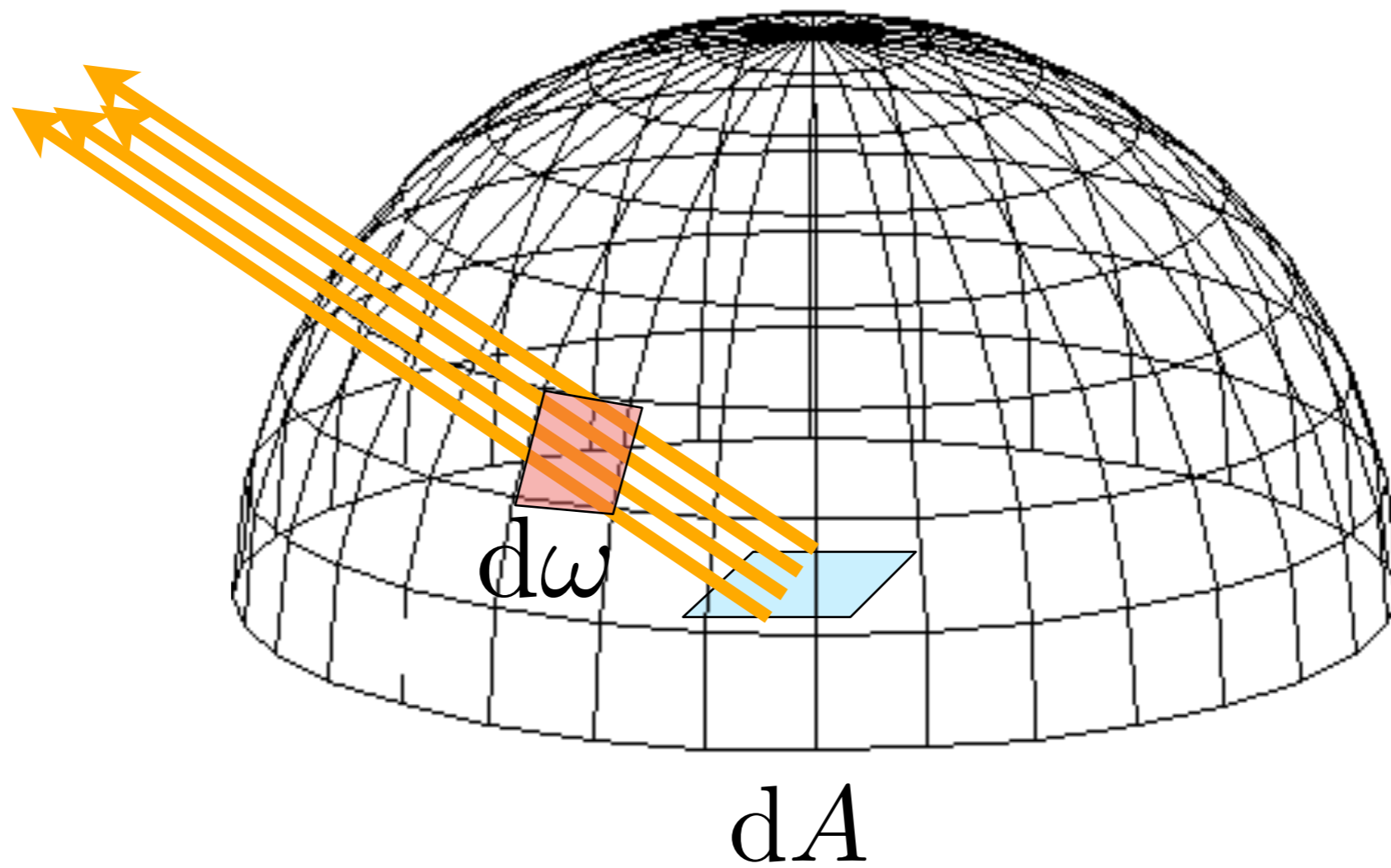
- Infinitely many of incident directions
 - Yes, you guessed it: integral over solid angle

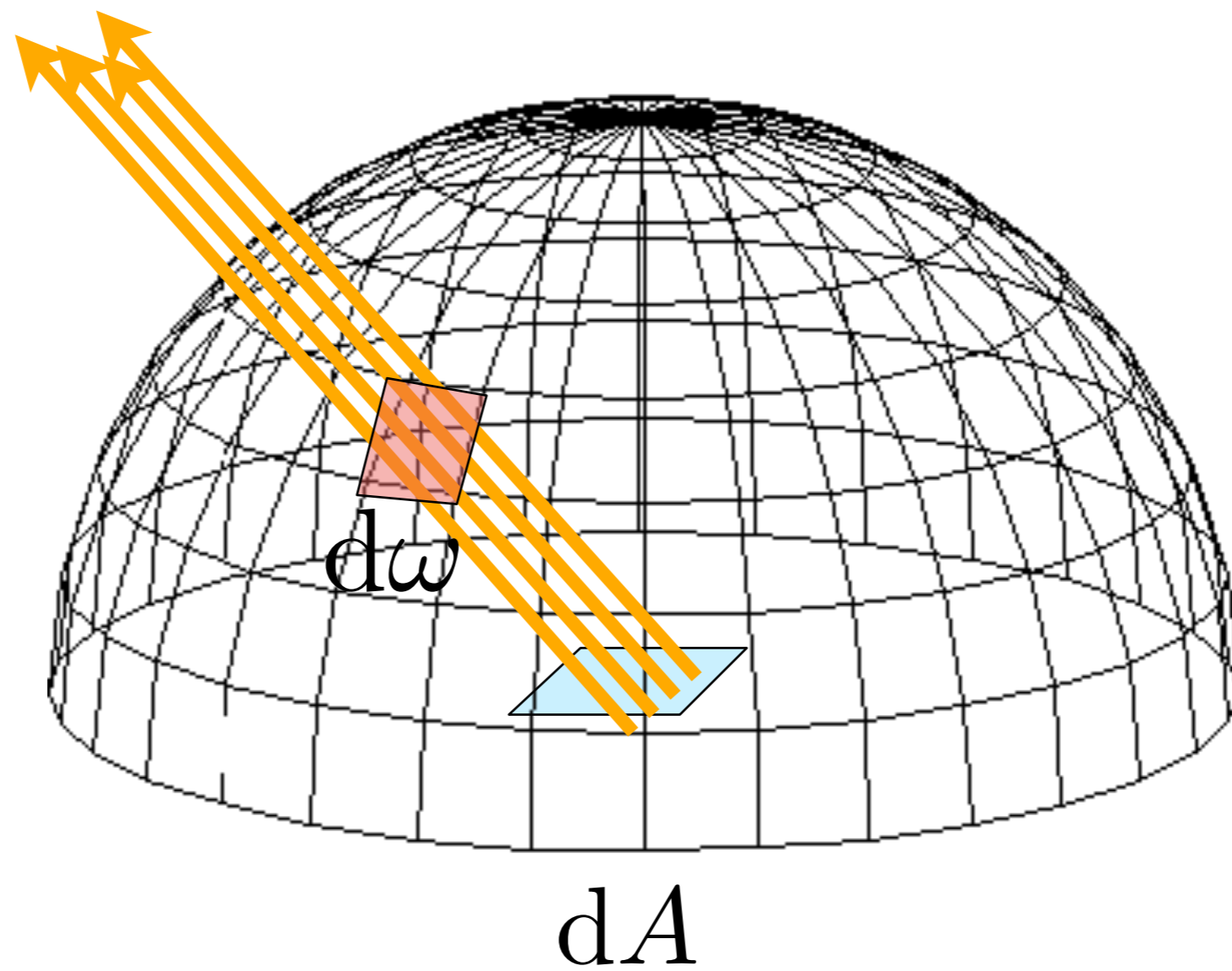
$$\frac{d\Phi}{dA} = L(\omega_3) \cos \theta \, d\omega$$

$$E = \frac{d\Phi}{dA}$$

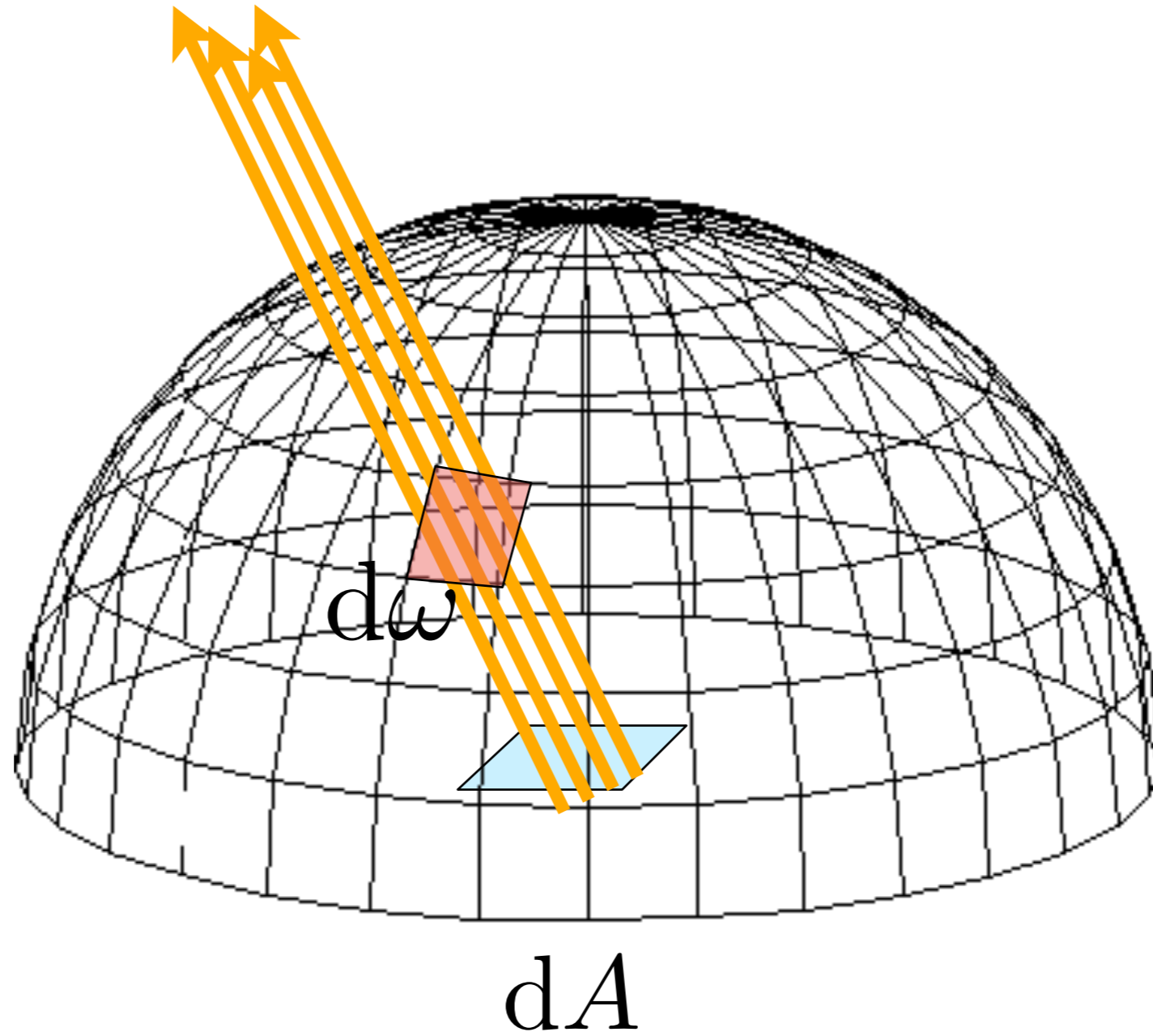
$$L = \frac{d\Phi}{dA^\perp \, d\omega}$$







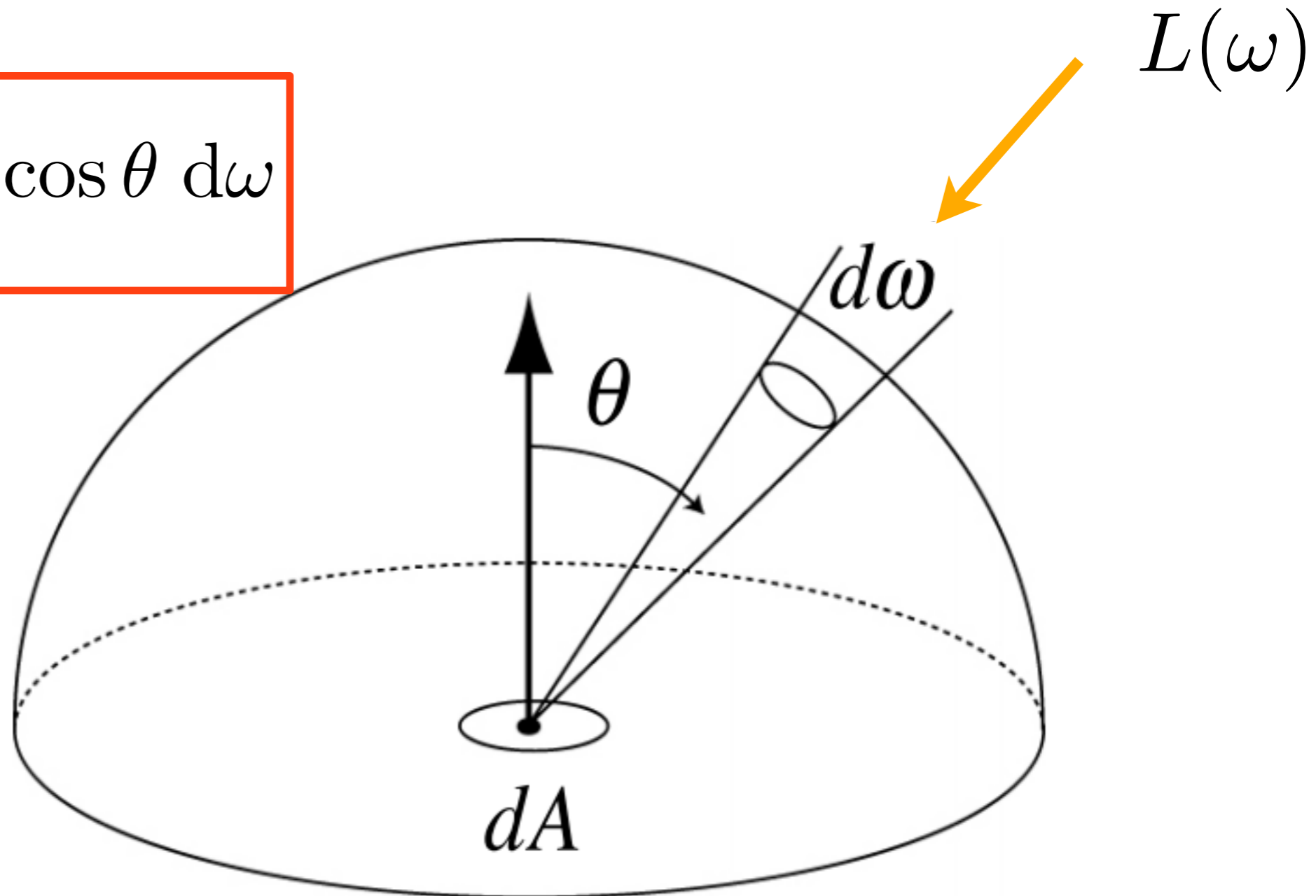
• ...



Irradiance

- Integrate incident radiance times cosine over the hemisphere Ω

$$E = \int_{\Omega} L(\omega) \cos \theta \, d\omega$$



Eureka, Part Deux

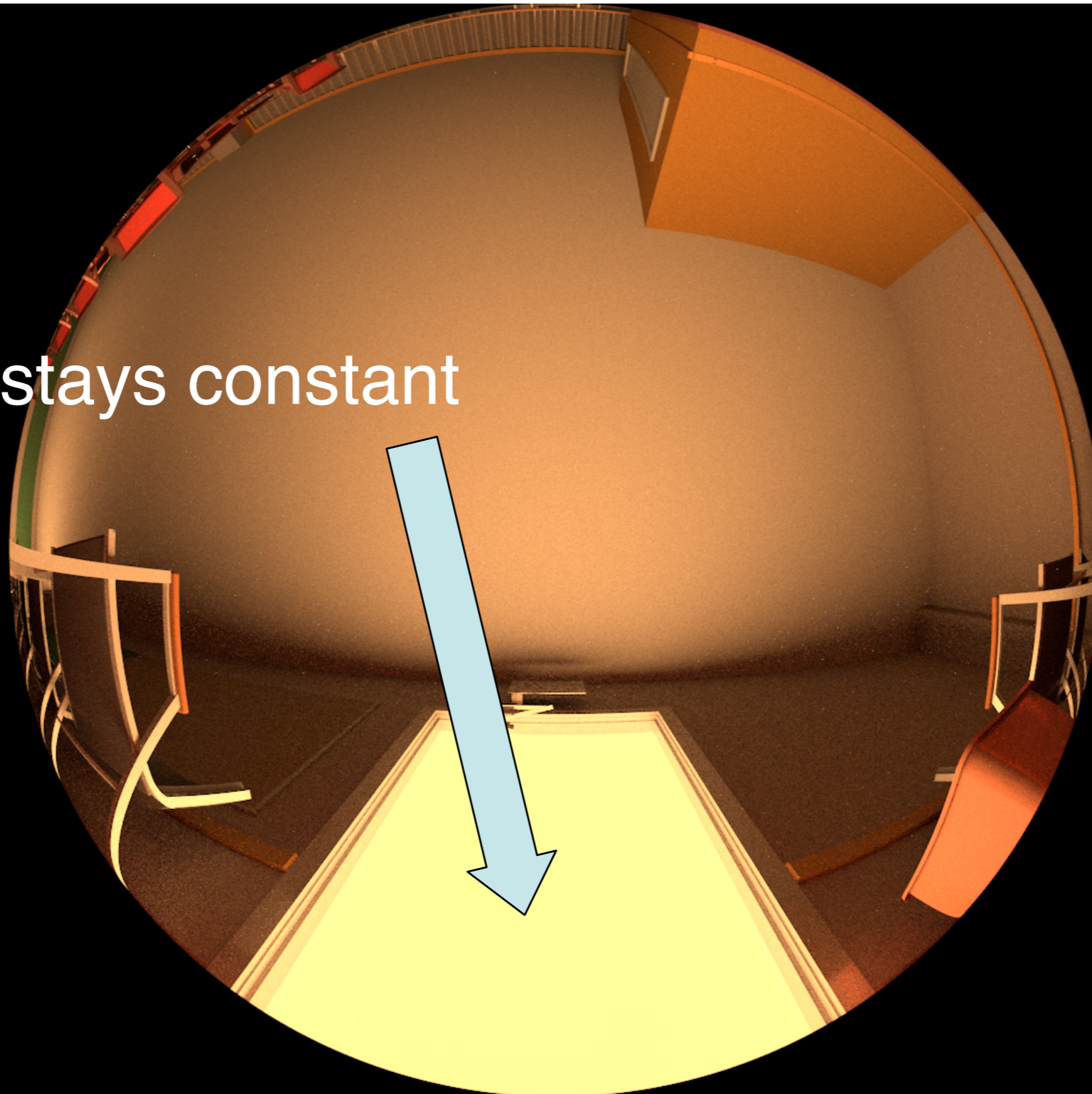
- Radiance is constant along straight lines ✓
 - I.e. radiance sent by dA_1 into the direction of dA_2 is the same as radiance received by dA_2 from the direction of dA_1 .
- This is why the lamp appears “as bright” no matter how far you look at it from ✓
 - BUT: The solid angle subtended by the lamp decreases with distance, so irradiance, which is the integral of radiance over solid angle, decreases => less light is reflected

$$E = \int_{\Omega} L(\omega) \cos \theta \, d\omega$$



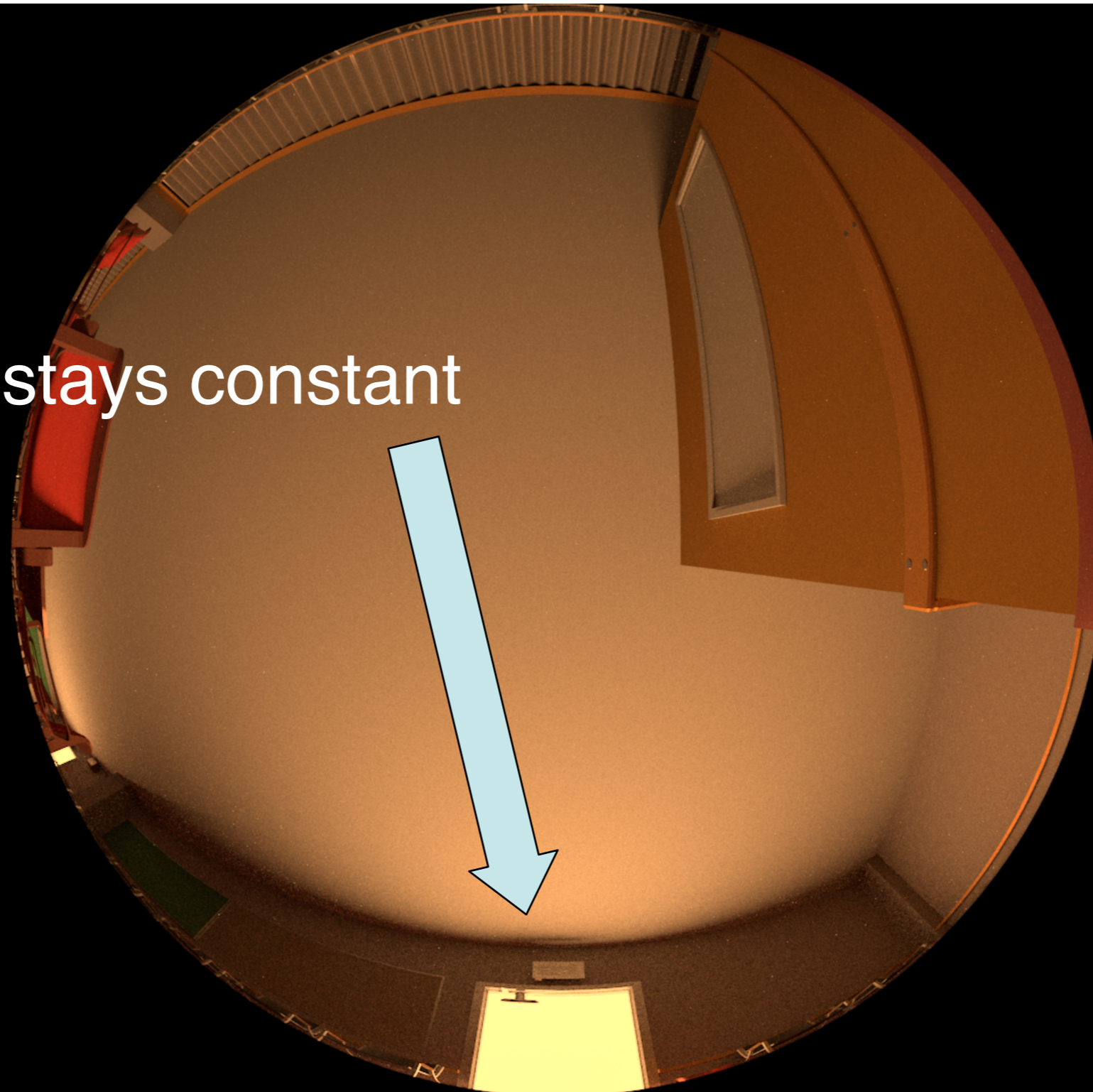
View from A

Brightness stays constant



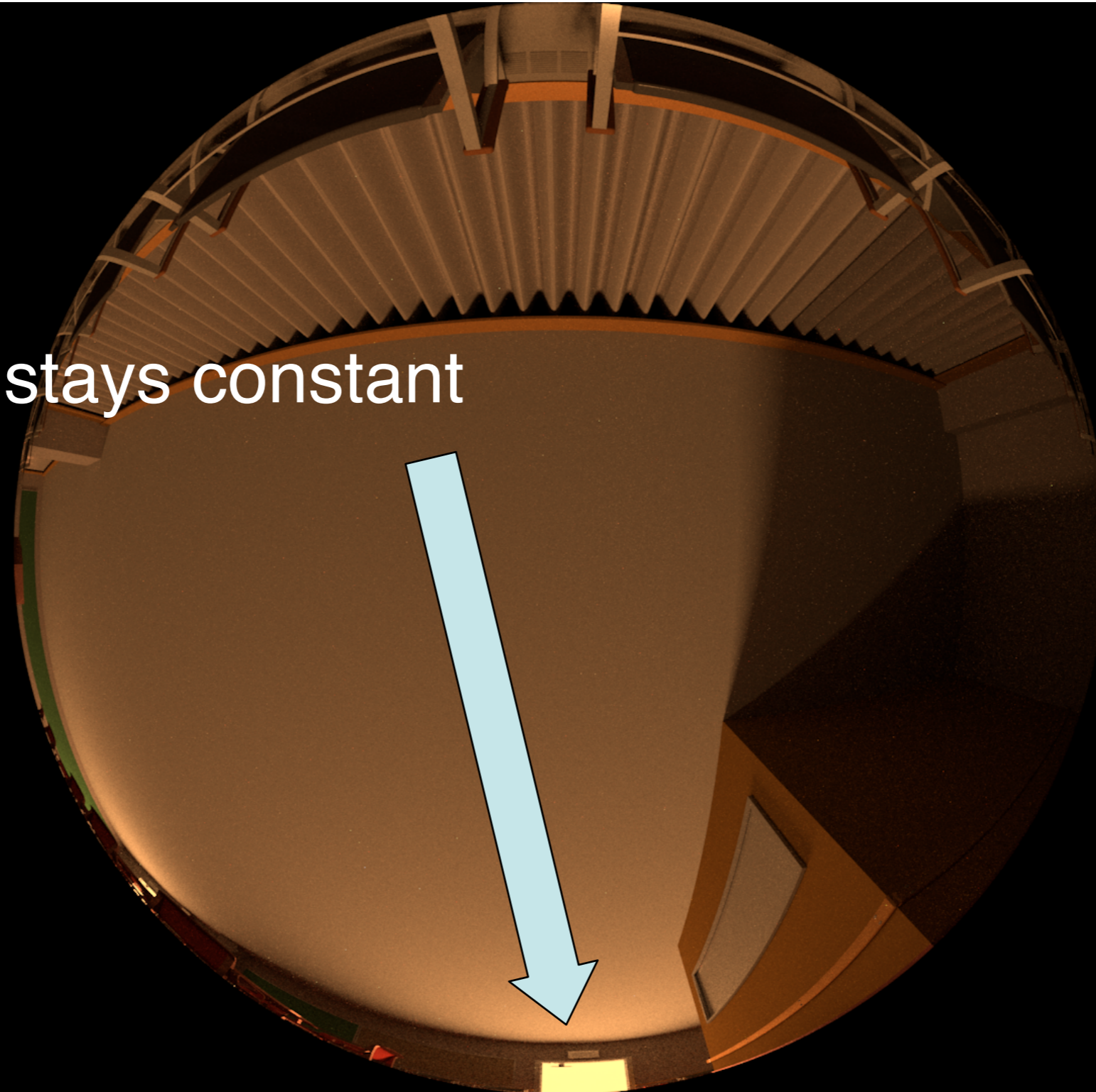
View from B

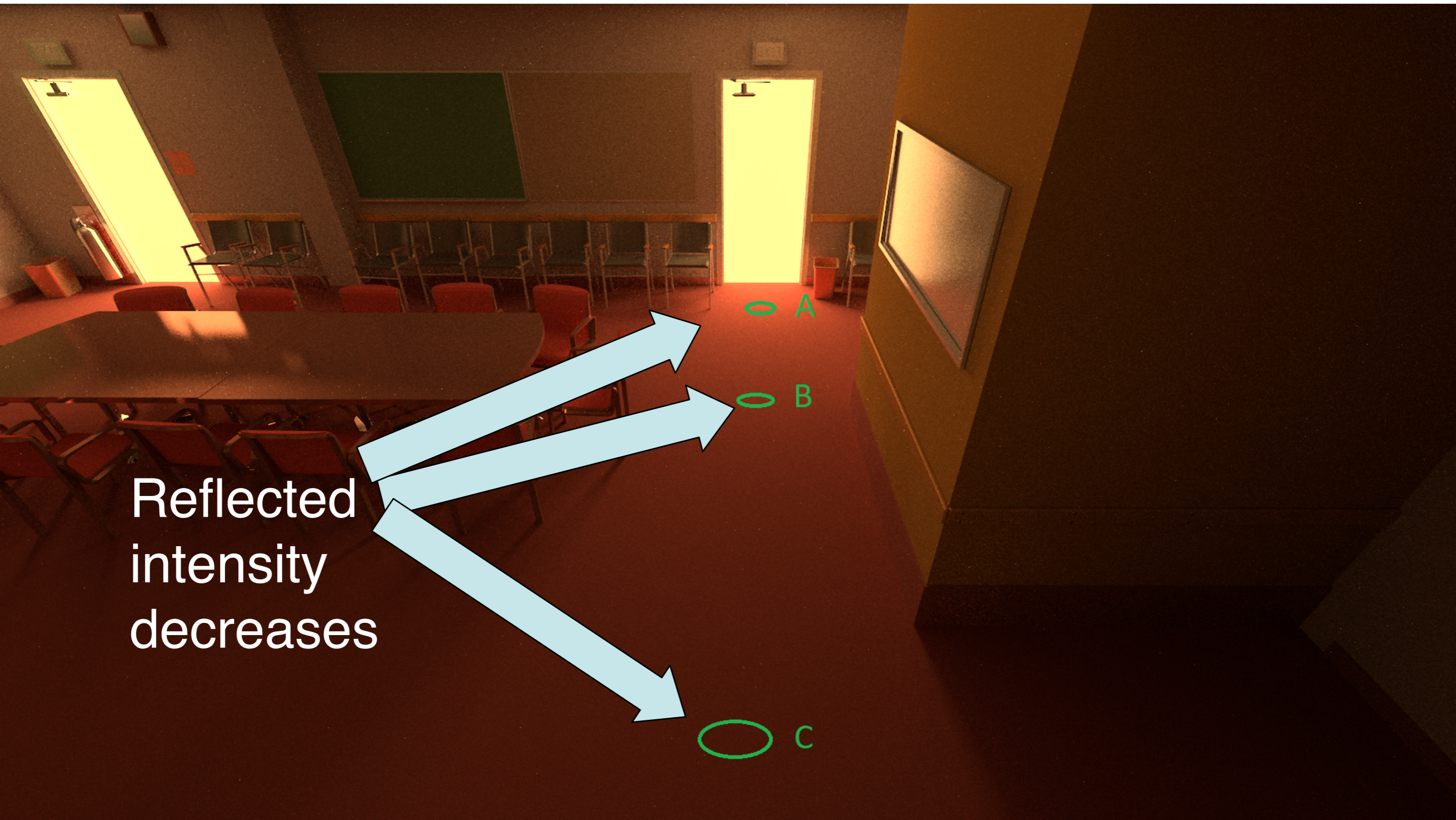
Brightness stays constant



View from C

Brightness stays constant

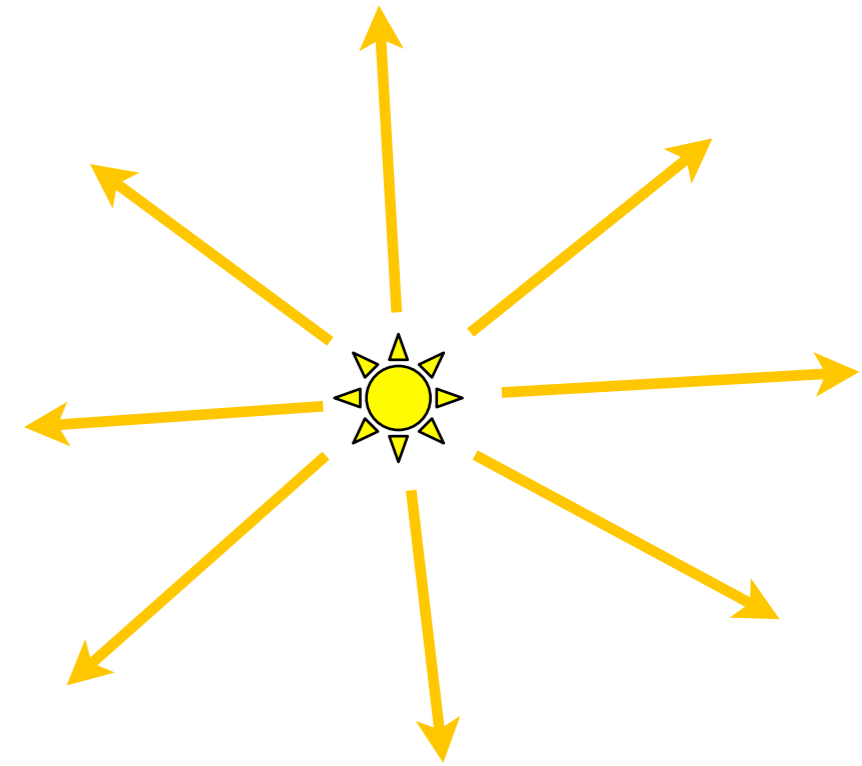




Reflected
intensity
decreases

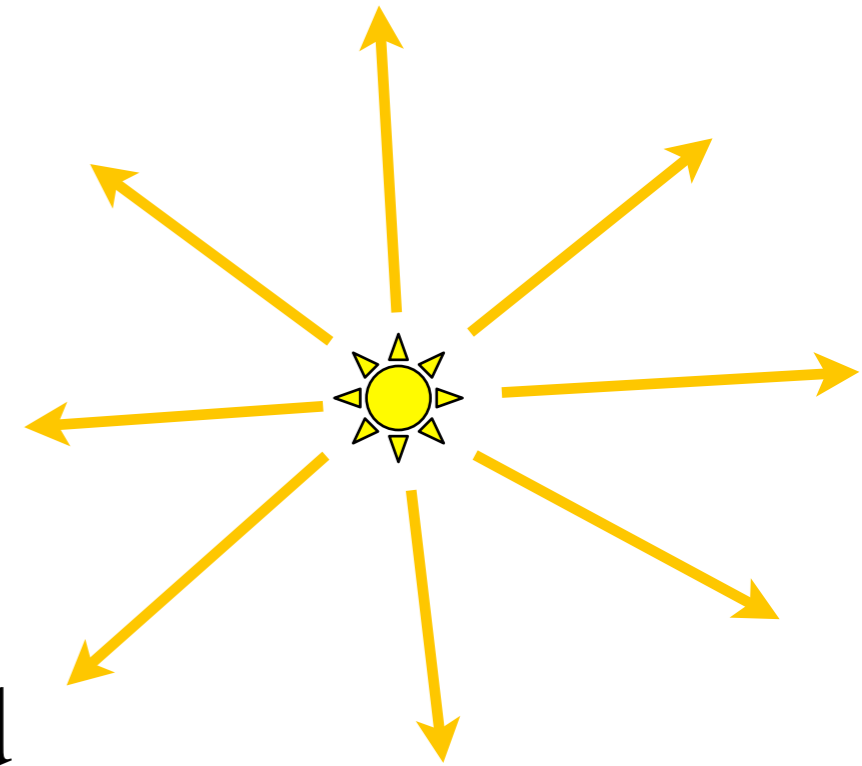
What About Pointlights?

- A pointlight has no area
 - Hence we can't define radiance easily
 - However, differential irradiance is easy



What About Pointlights?

- A pointlight has no area
 - Hence we can't define radiance easily
 - However, differential irradiance is easy
- The emission of a pointlight measured by *intensity* I , flux per solid angle



$$I = \frac{d\Phi}{d\omega}$$

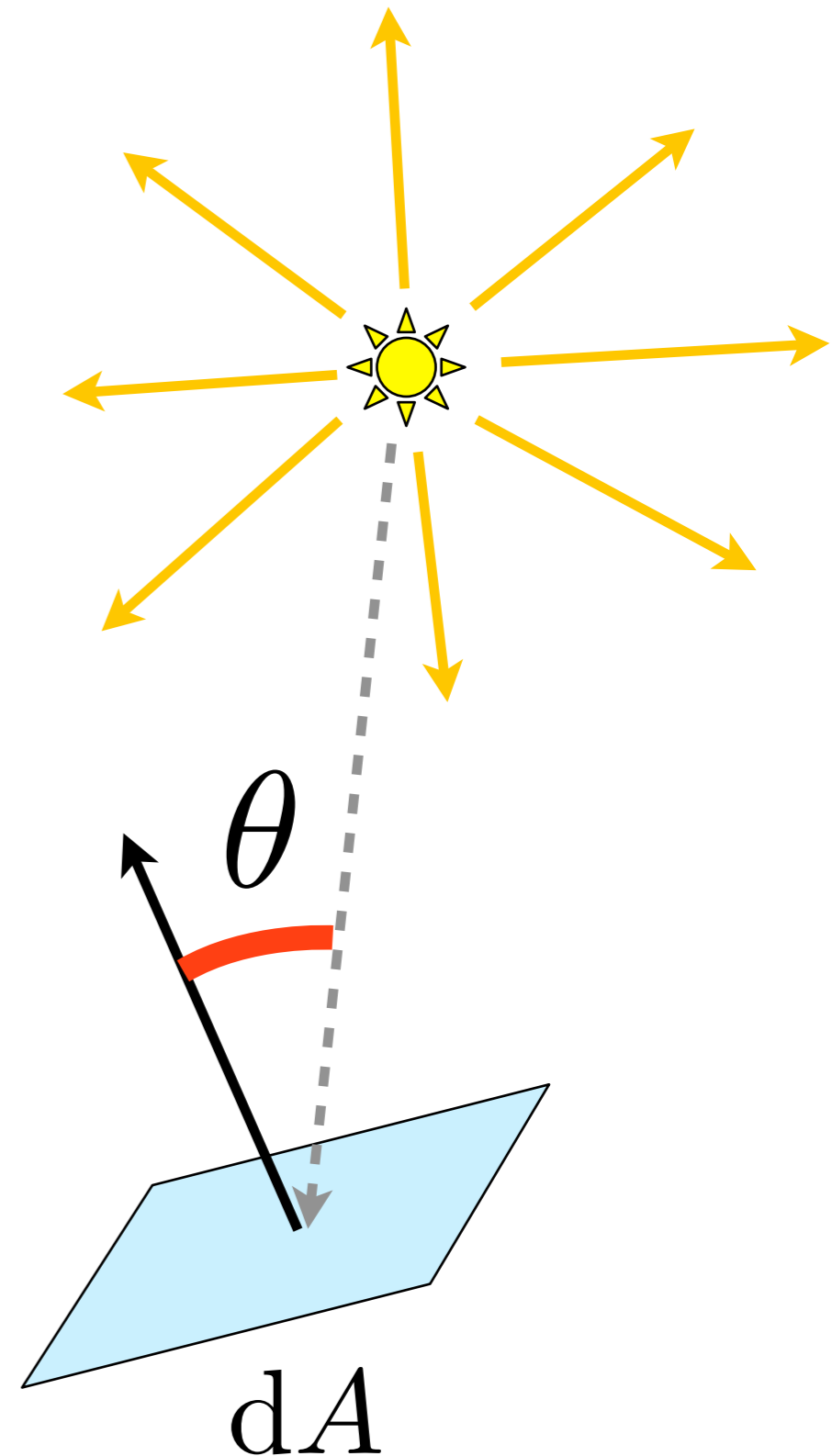
$$[I] = \left[\frac{W}{sr} \right]$$

Irradiance due to a Pointlight

- What's the irradiance received by dA from the light \Leftrightarrow
what's the solid angle subtended by dA as seen from the light?
 - We know the answer...

$$I = \frac{d\Phi}{d\omega}$$

$$[I] = \left[\frac{W}{sr} \right]$$

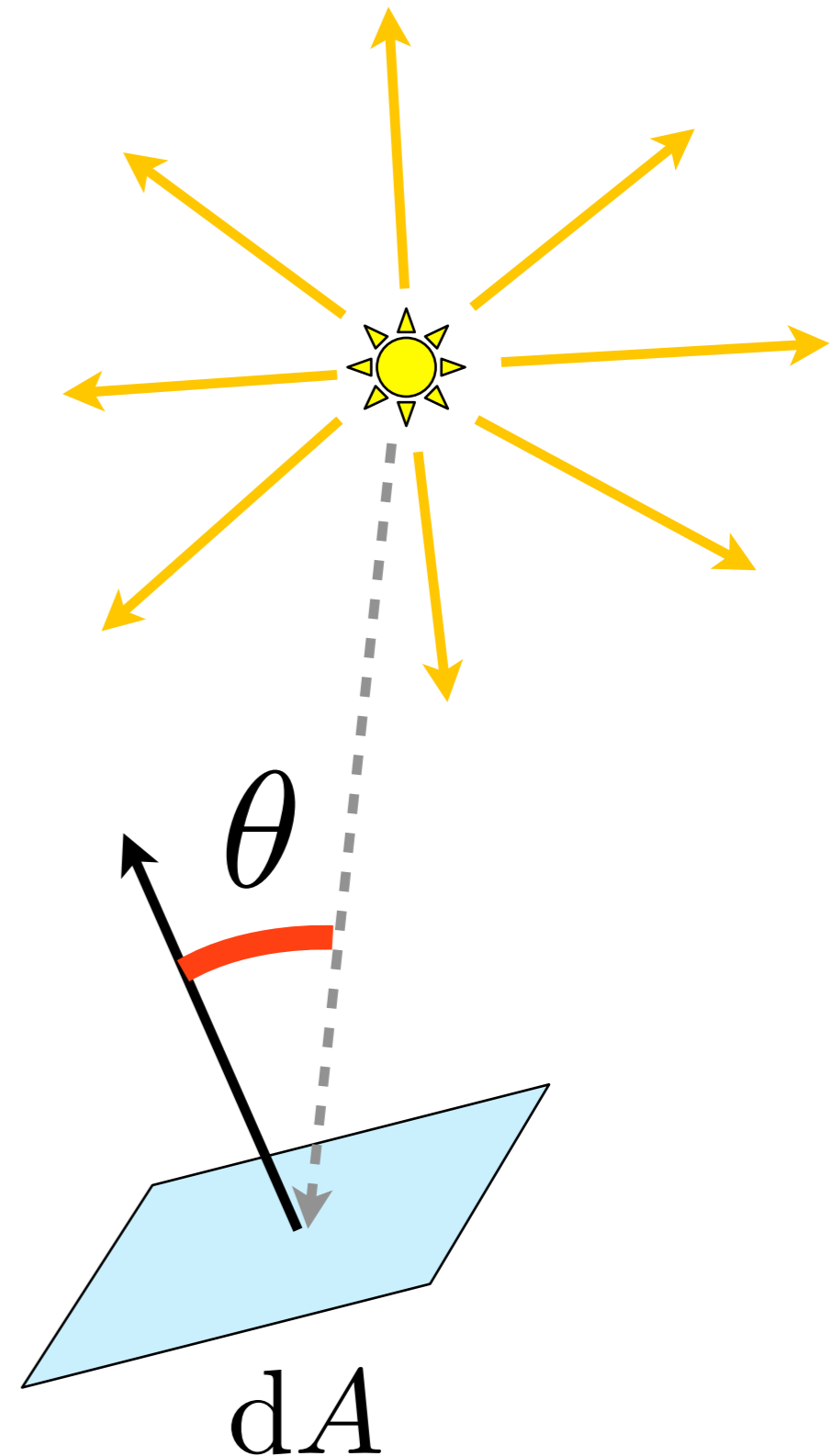


Irradiance due to a Pointlight

- What's the irradiance received by dA from the light \Leftrightarrow
what's the solid angle subtended by dA as seen from the light?
 - We know the answer...

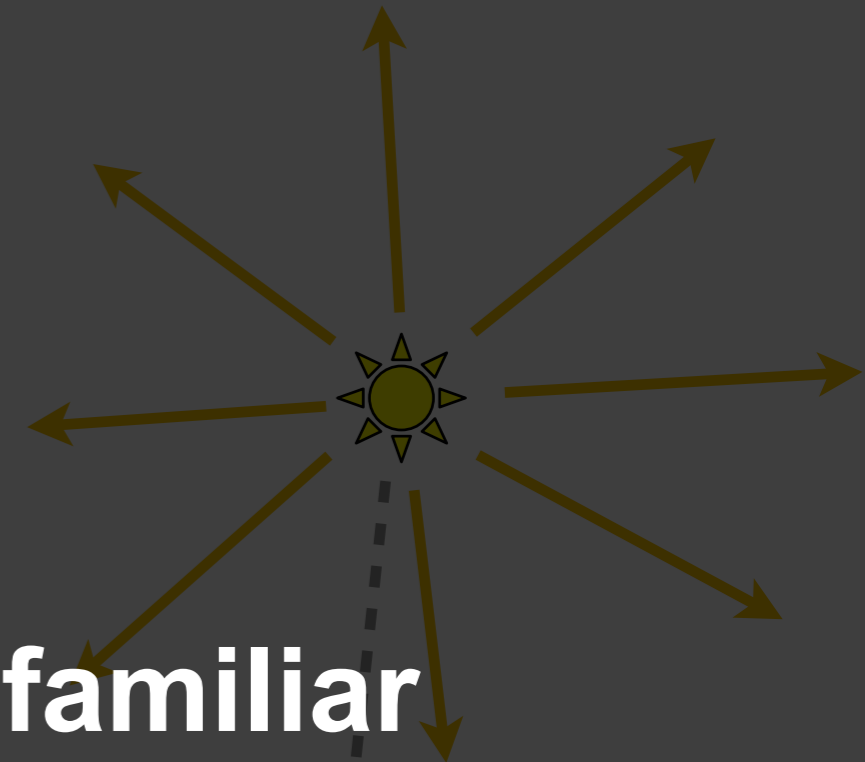
$$E = \frac{d\Phi}{dA} = I \frac{d\omega}{dA} = I \frac{\cos \theta}{r^2}$$

$$I = \frac{d\Phi}{d\omega} \quad [I] = \left[\frac{W}{sr} \right]$$



Irradiance due to a Pointlight

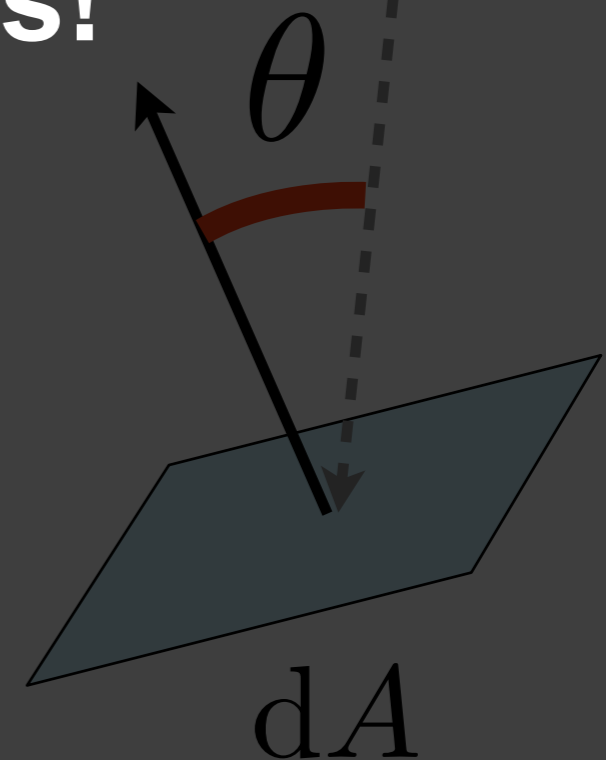
- What's the irradiance received by dA from the light \Leftrightarrow
what's the solid angle subtended by dA as seen from the light?



– We know the answer!
This formula should look familiar from the intro class!

$$E = \frac{d\Phi}{dA} = I \frac{d\omega}{dA} = I \frac{\cos \theta}{r^2}$$

$$I = \frac{d\Phi}{d\omega} \quad [I] = \left[\frac{W}{sr} \right]$$



“White Furnace Test”

- Integrate incident radiance times cosine over the hemisphere Ω above surface normal

$$E = \int_{\Omega} L(\omega) \cos \theta \, d\omega$$

- Sanity check: What if we get unit intensity in, i.e., $L=1$ for all incident directions?
 - The so-called “white furnace test”
 - We’d expect the surface not to emit more than 1 unit of radiance.. Conservation of energy!
 - *Good idea to perform this in code for validation!*

“White Furnace Test”

$$E = \int_{\Omega} L(\omega) \cos \theta \, d\omega$$

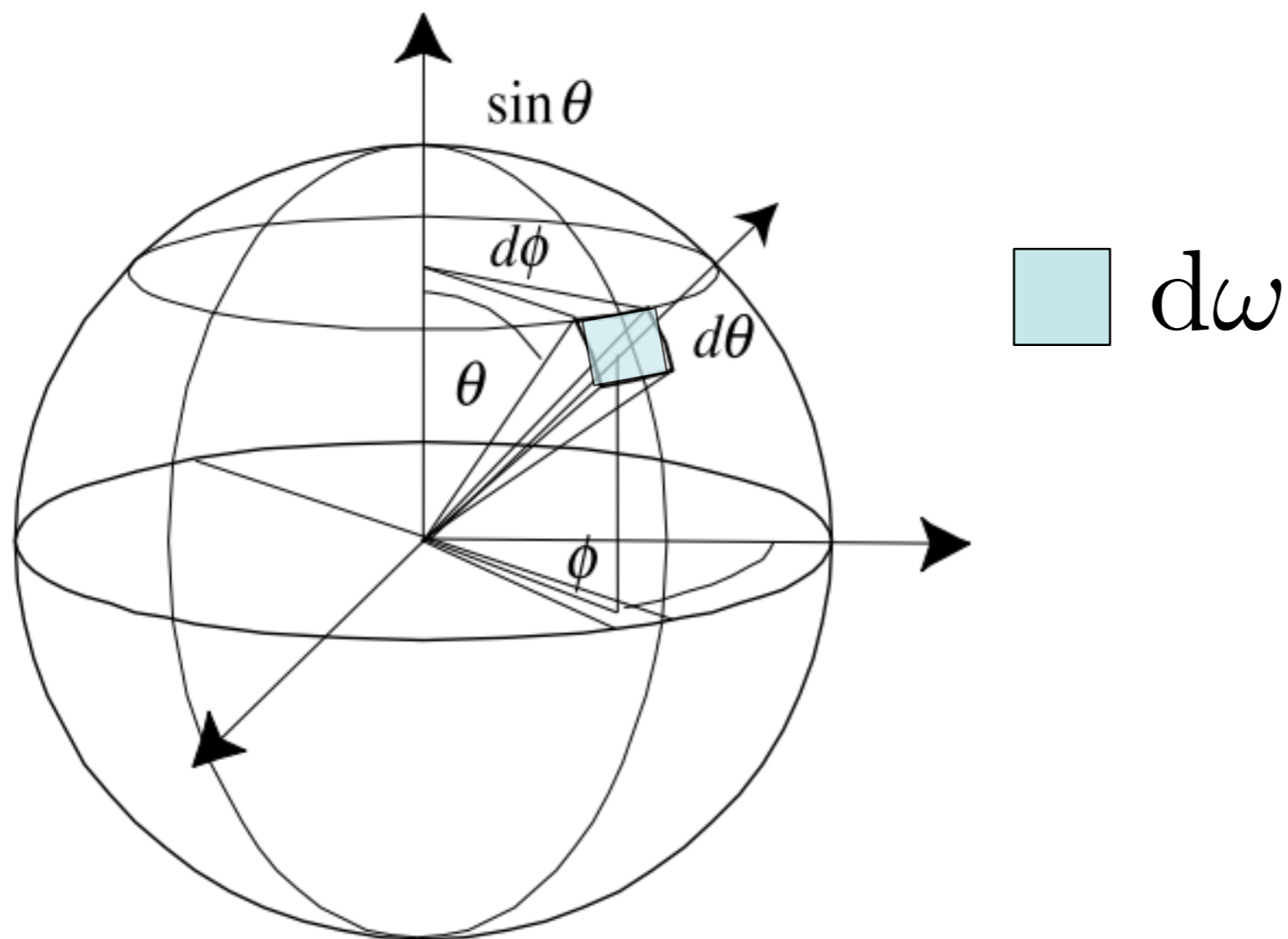
Remember! The cosine in these hemisphere formulas is pretty much always assumed to be clamped to zero from below, so that we don't count anything from below the horizon...

$$\cos \theta = \max(0, \cos \theta)$$

..but we don't want to clutter the notation.

Interlude

- Remember polar coordinates? $d\omega = \sin \theta d\theta d\phi$

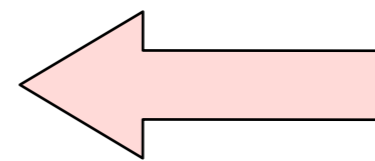


White Furnace, cont'd

- Sanity check: What if we get unit intensity in, i.e., $L=1$ for all incident directions?

$$E = \int_{\Omega} L(\omega) \cos \theta \, d\omega$$

$$= \int 1 \cos \theta \sin \theta \, d\theta \, d\phi$$



integral over
hemisphere in polar
coordinates

$$\phi \in \{0, 2\pi\}$$

$$\theta \in \{0, \pi/2\}$$

White Furnace, cont'd

- Sanity check: What if we get unit intensity in, i.e., $L=1$ for all incident directions?

$$E = \int_{\Omega} L(\omega) \cos \theta \, d\omega$$

See it for yourself in
Wolfram Alpha (click here)

$$= \int 1 \cos \theta \sin \theta \, d\theta \, d\phi \quad \boxed{= \pi}$$

$$\phi \in \{0, 2\pi\}$$

$$\theta \in \{0, \pi/2\}$$

Hmm, intuition says: if you light a perfectly reflecting diffuse surface with uniform lighting, you should get the same “intensity” out

From Irradiance to Radiosity

- The reflectivity of a diffuse surface is determined by its *albedo* ρ
 - This is the “diffuse color k_d ” from your ray tracer in C3100
- The flux emitted by a diffuse surface per unit area is called *radiosity* B
 - Same units as irradiance, $[B] = [W/m^2]$
 - Hence

$$B = \frac{\rho E}{\pi}$$

(Danger spot!
What if you forget
to divide your
albedo by pi?)

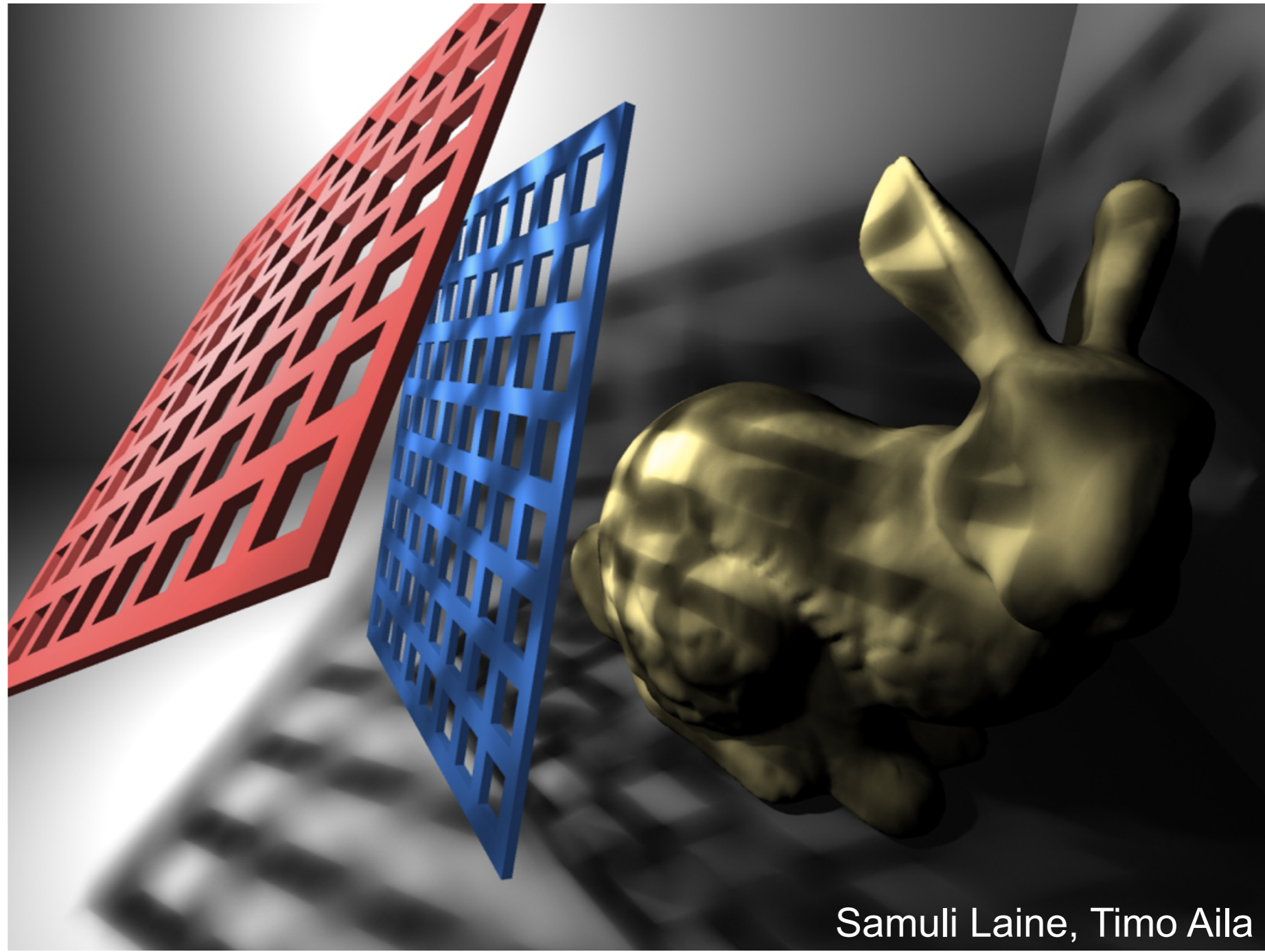
Radiosity cont'd

- For a diffuse surface, the outgoing radiance is constant over all directions, and $L = B$
- Diffuseness is a pretty strict approximation (not many surfaces are really like that) but diffuse GI can look very good when done right
 - We did this for Max Payne 1 & 2
 - Easy to combine diffuse GI solution with “fake” glossy/specular reflections computed on top of it



Enough Theory, Let's Apply This

- How to compute soft shadows from an area light source on a diffuse receiver?



Lambertian Soft Shadows

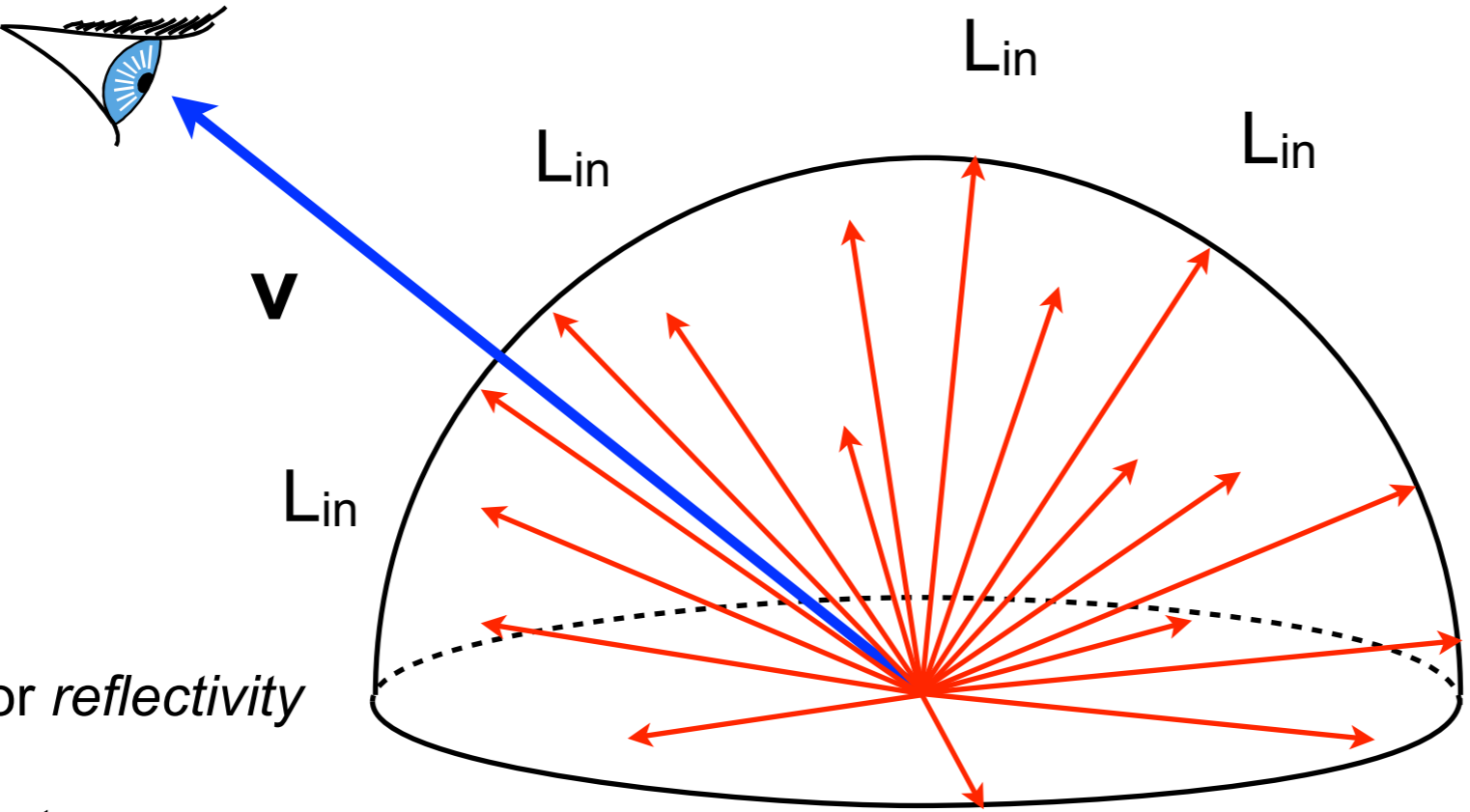
differential
solid angle

$$L_{\text{out}}(x) = \frac{\rho(x)}{\pi} \int_{\Omega} L_{\text{in}}(x, \omega) \cos \theta \, d\omega$$

outgoing light
(diffuse =>
independent of
direction v)

albedo/pi

incident radiance cosine
term



Sum (integrate)
over every
direction on the
hemisphere,
modulate incident
illumination by
cosine, albedo/pi

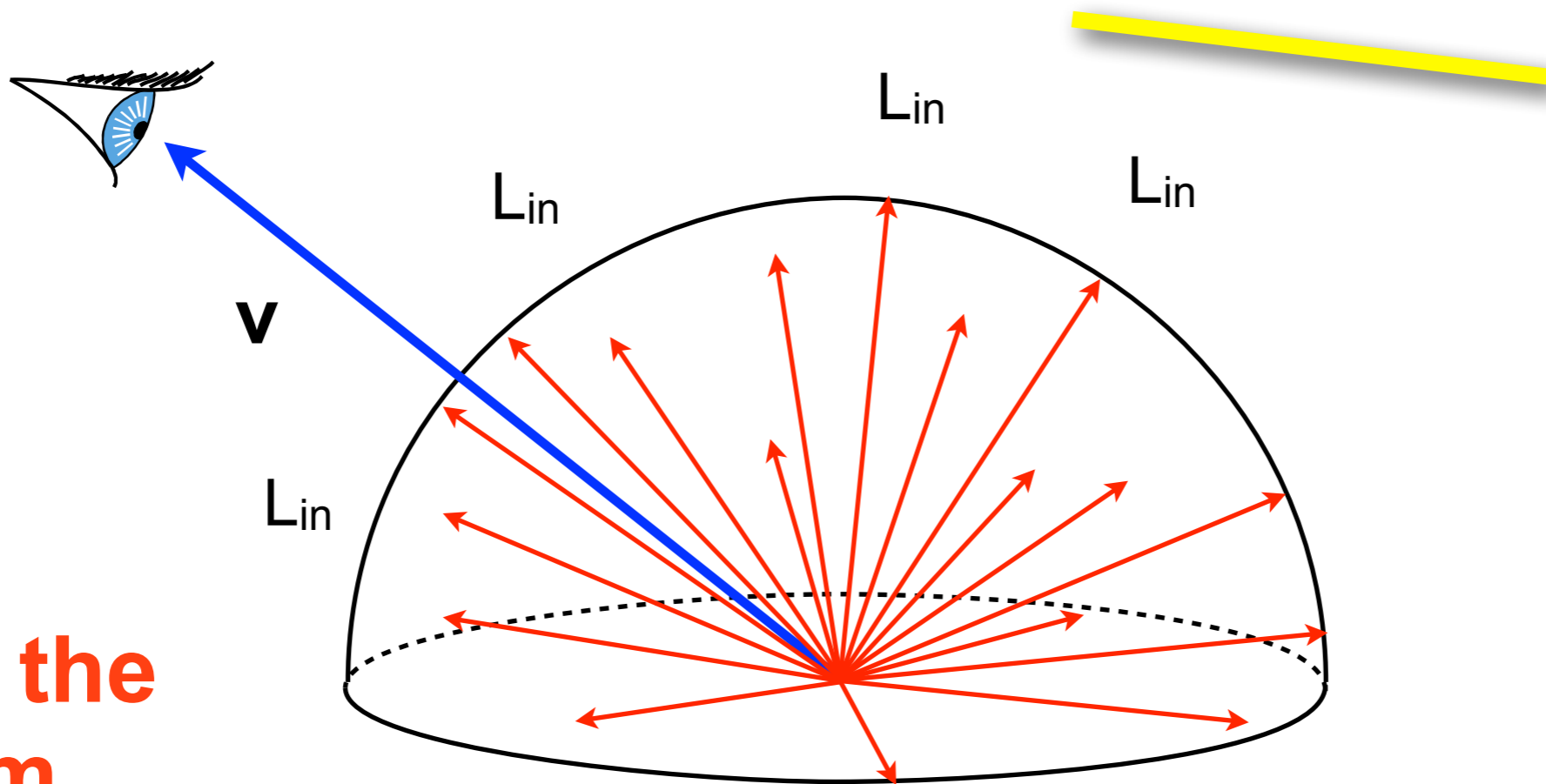
$\rho(x)$

is the albedo or *reflectivity*
(between 0,1)
of the surface at x

Incident Light: Area Light Source

$$L_{\text{out}}(x) = \frac{\rho(x)}{\pi} \int_{\Omega} L_{\text{in}}(x, \omega) \cos \theta \, d\omega$$

incident light
from direction ω

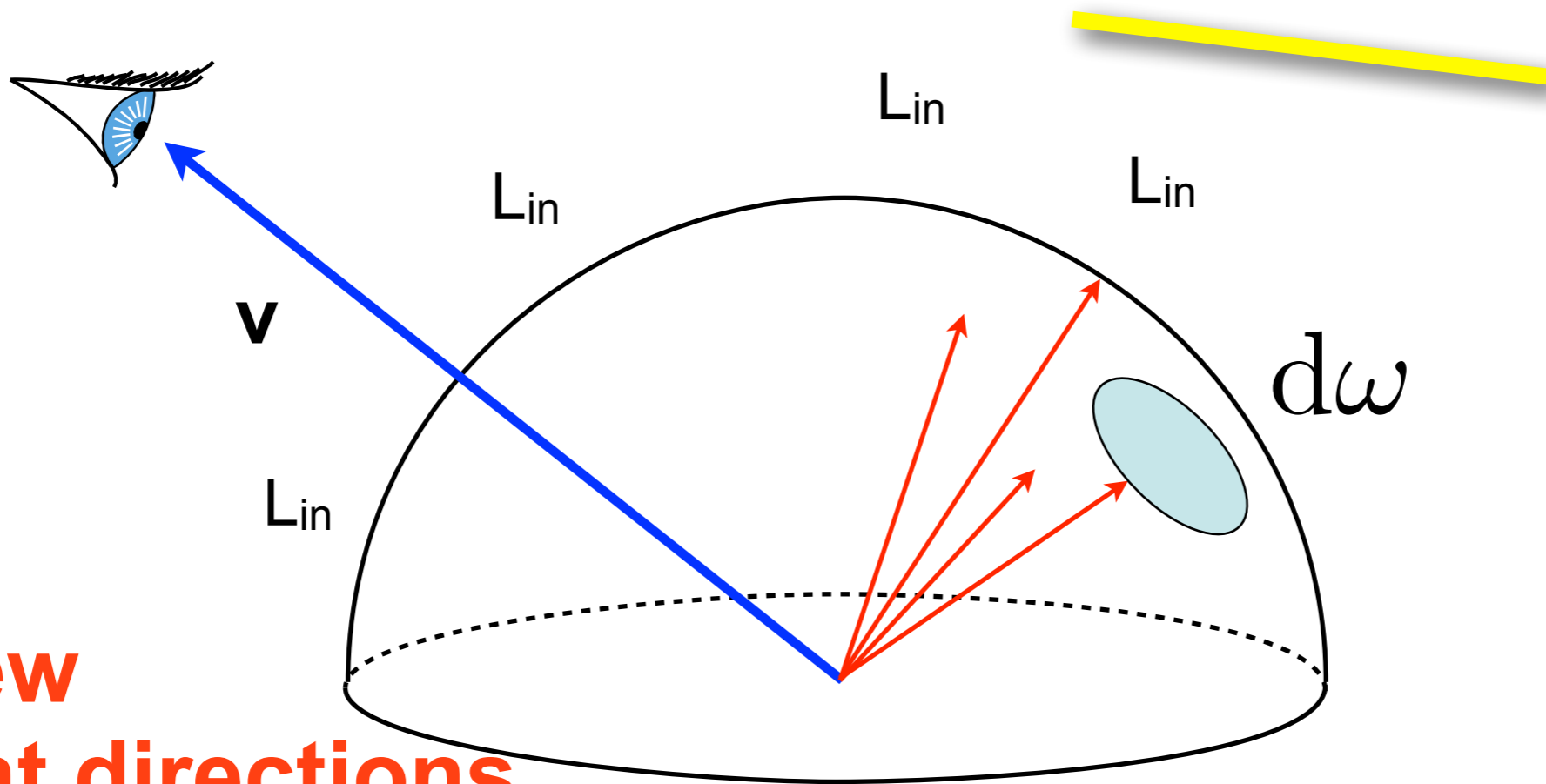


What's the
problem
here?

Incident Light: Area Light Source

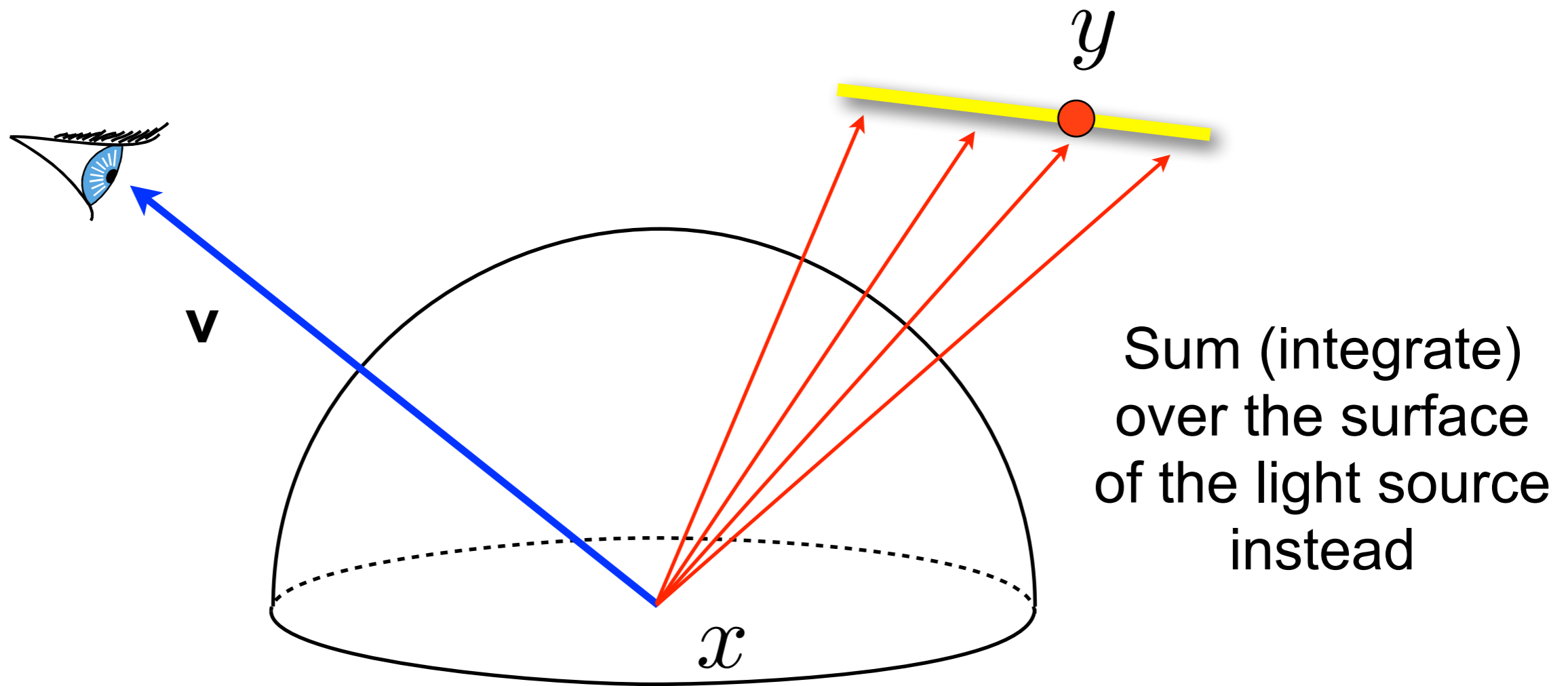
$$L_{\text{out}}(x) = \frac{\rho(x)}{\pi} \int_{\Omega} L_{\text{in}}(x, \omega) \cos \theta \, d\omega$$

incident light
from direction ω



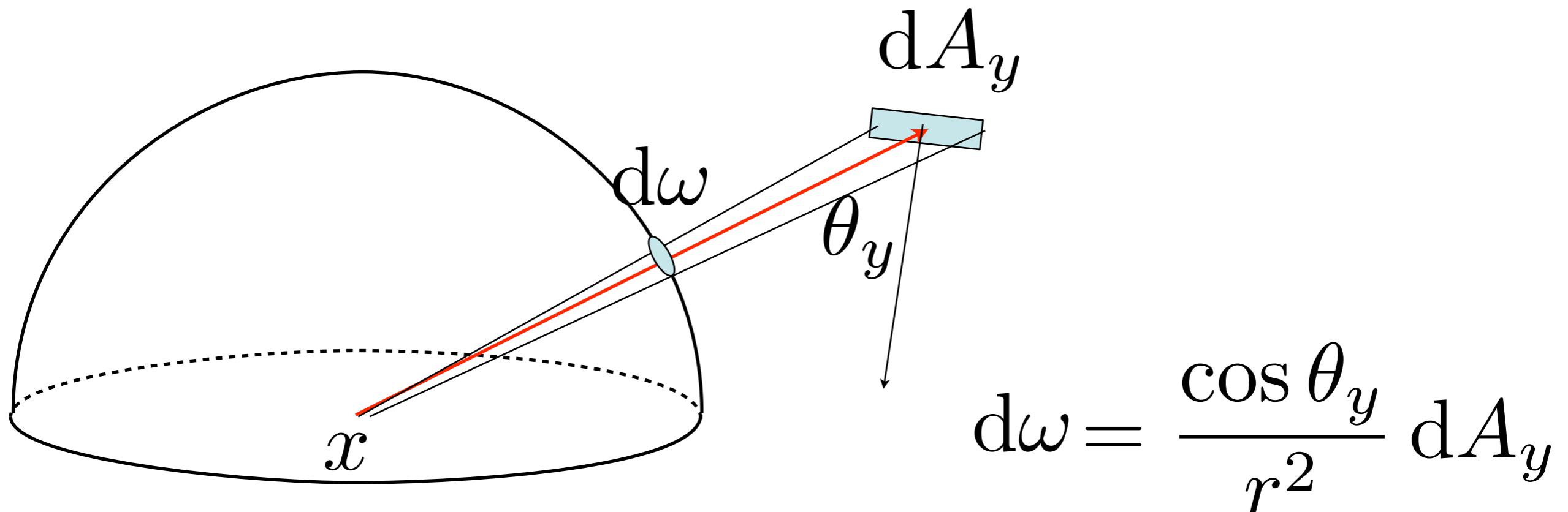
**Only few
incident directions
contribute!**

Fortunately, We Know What To Do!



Looks Hairy, But Isn't

- We started today by looking at the solid angle, and how it relates to infinitesimal surface patches
- This really is just a change of integration variables
 - With proper normalization factors (you know this from math), integral over surface \Leftrightarrow integral over solid angle

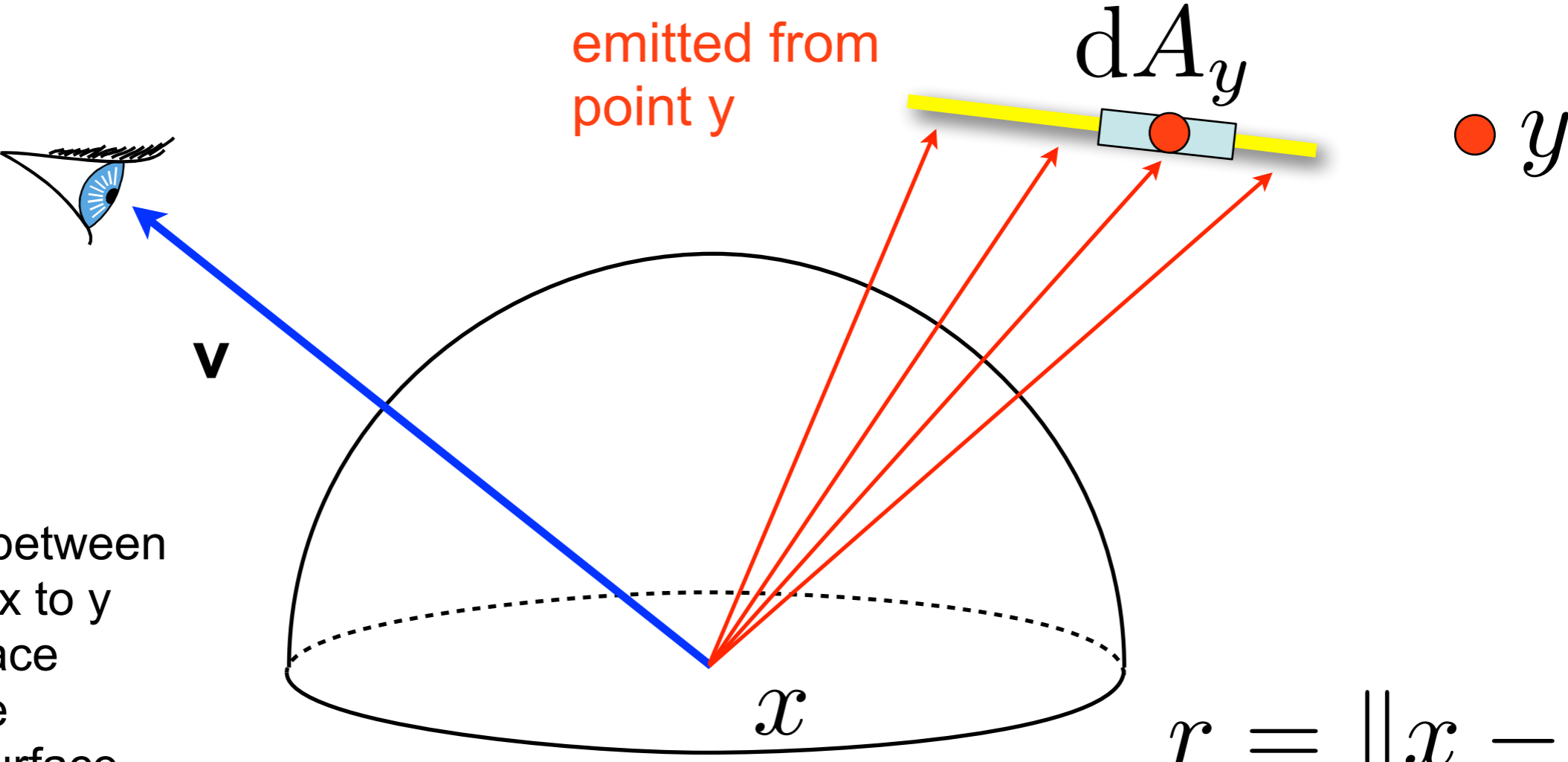


Change variables and integrate over light

Area \Leftrightarrow solid angle conversion

$$L_{\text{out}} = \frac{\rho(x)}{\pi} \int_{\text{light}} E(y) \frac{\cos \theta_y}{r^2} \cos \theta \, dA_y$$

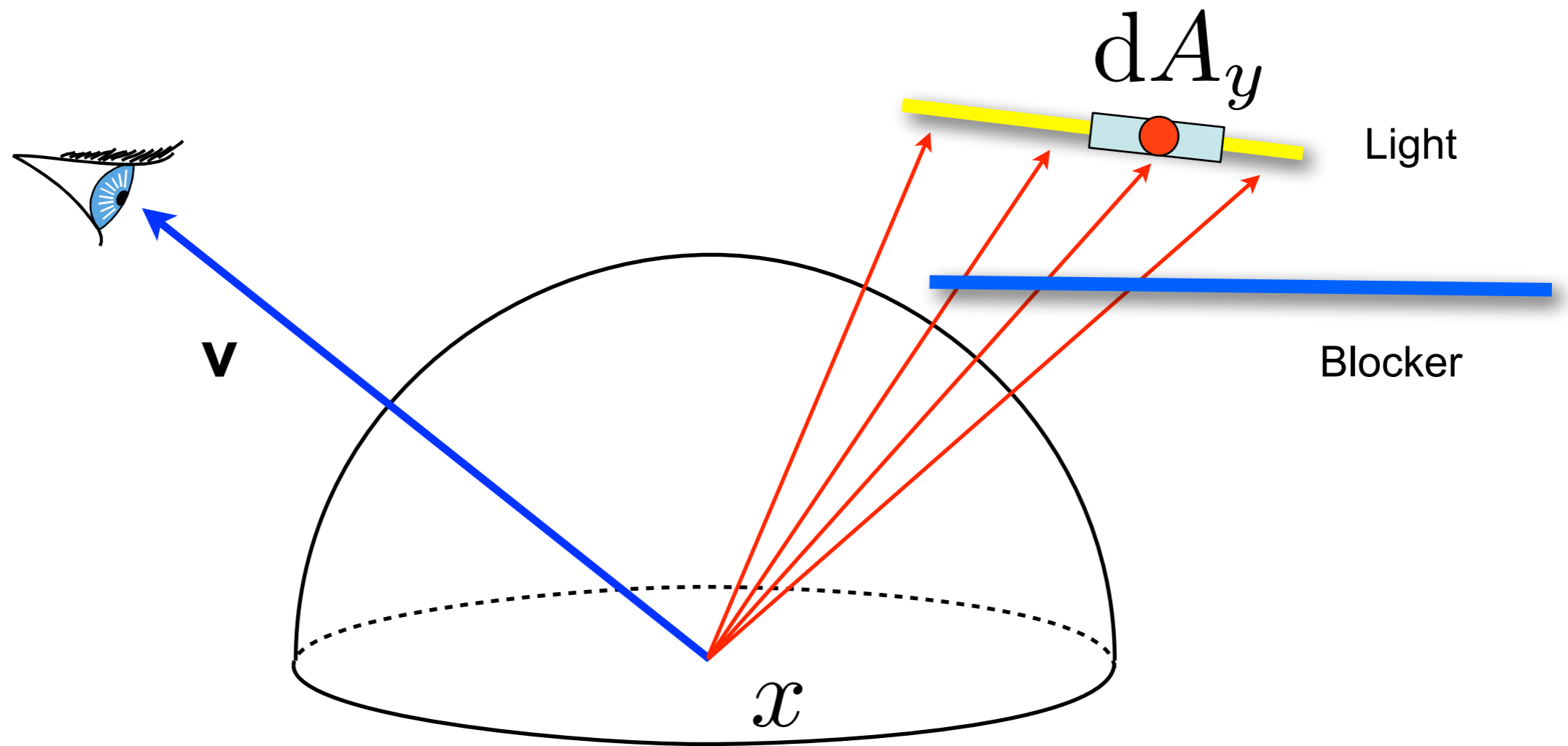
Radiance emitted from point y



θ_y is the angle between the ray from x to y and the surface normal of the differential surface patch dA_y .

$$r = \|x - y\|$$

Still Not Quite There Yet



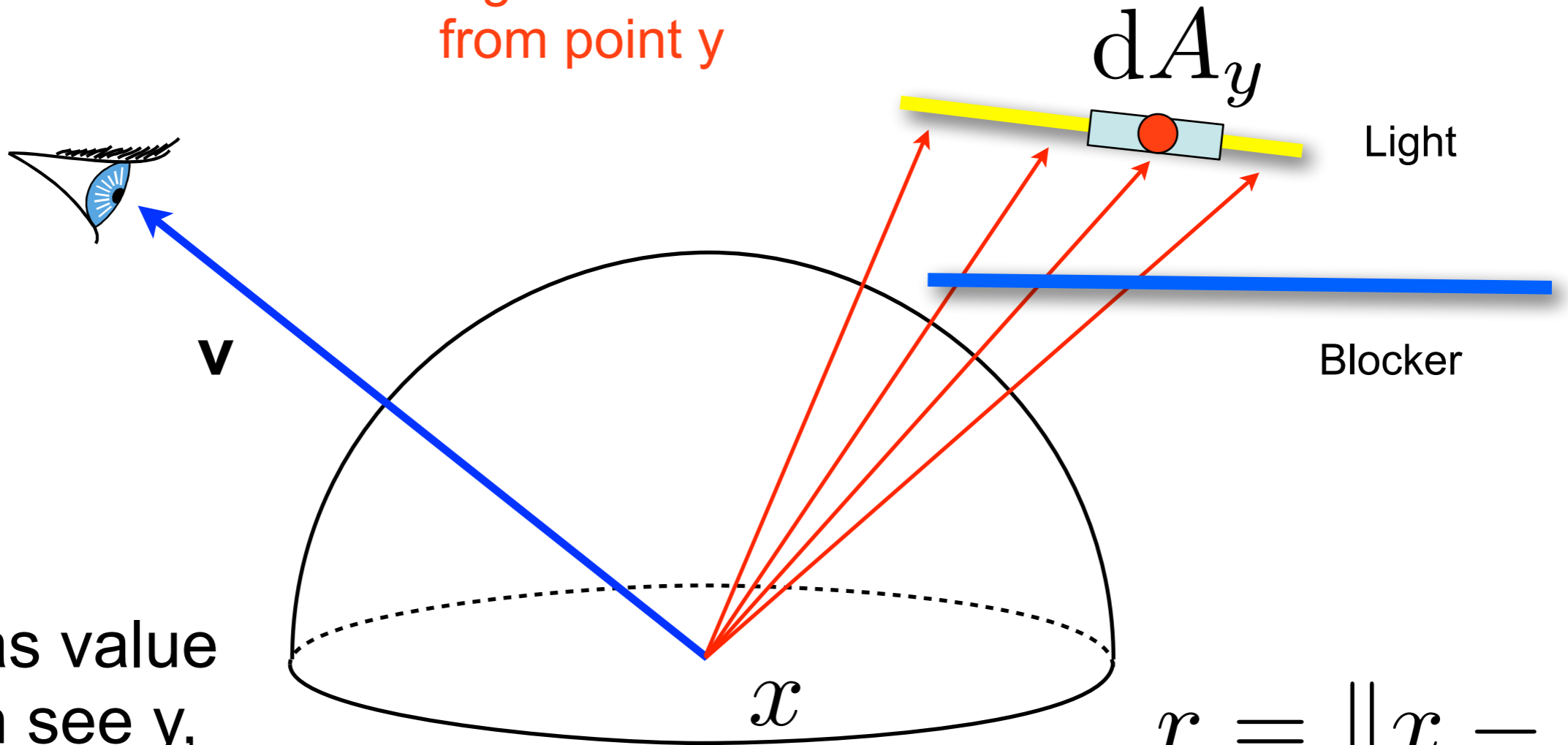
Visibility Causes Soft Shadows

Area \Leftrightarrow solid angle conversion

Visibility function

$$L_{\text{out}} = \frac{\rho(x)}{\pi} \int_{\text{light}} E(y) V(x, y) \frac{\cos \theta_y}{r^2} \cos \theta \, dA_y$$

Light emitted from point y



Light

Blocker

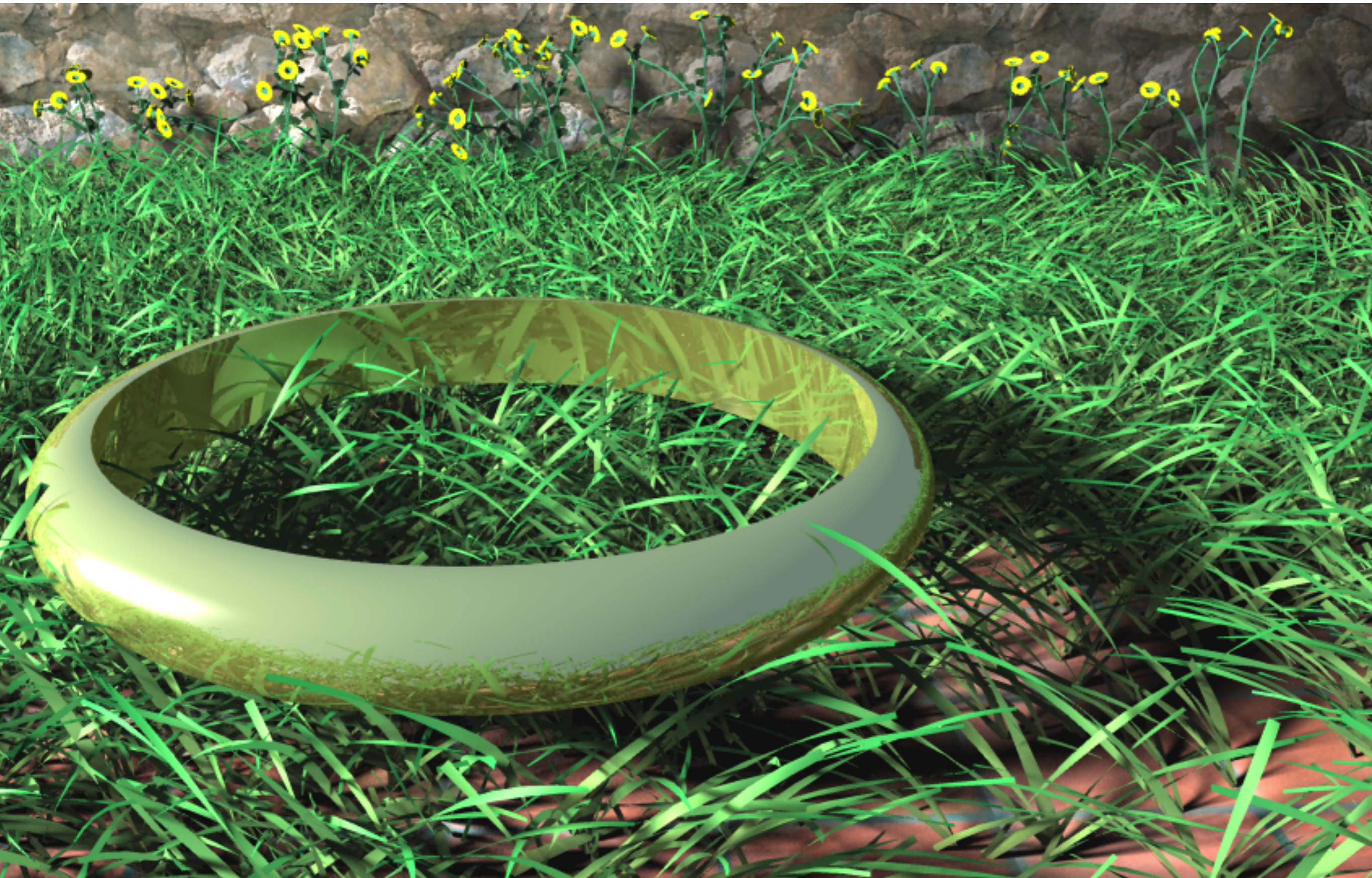
x

$$r = \|x - y\|$$

$V(x,y)$ has value 1 if x can see y , 0 if not

Questions?

Laine et al., cover of SIGGRAPH 2005 proceedings

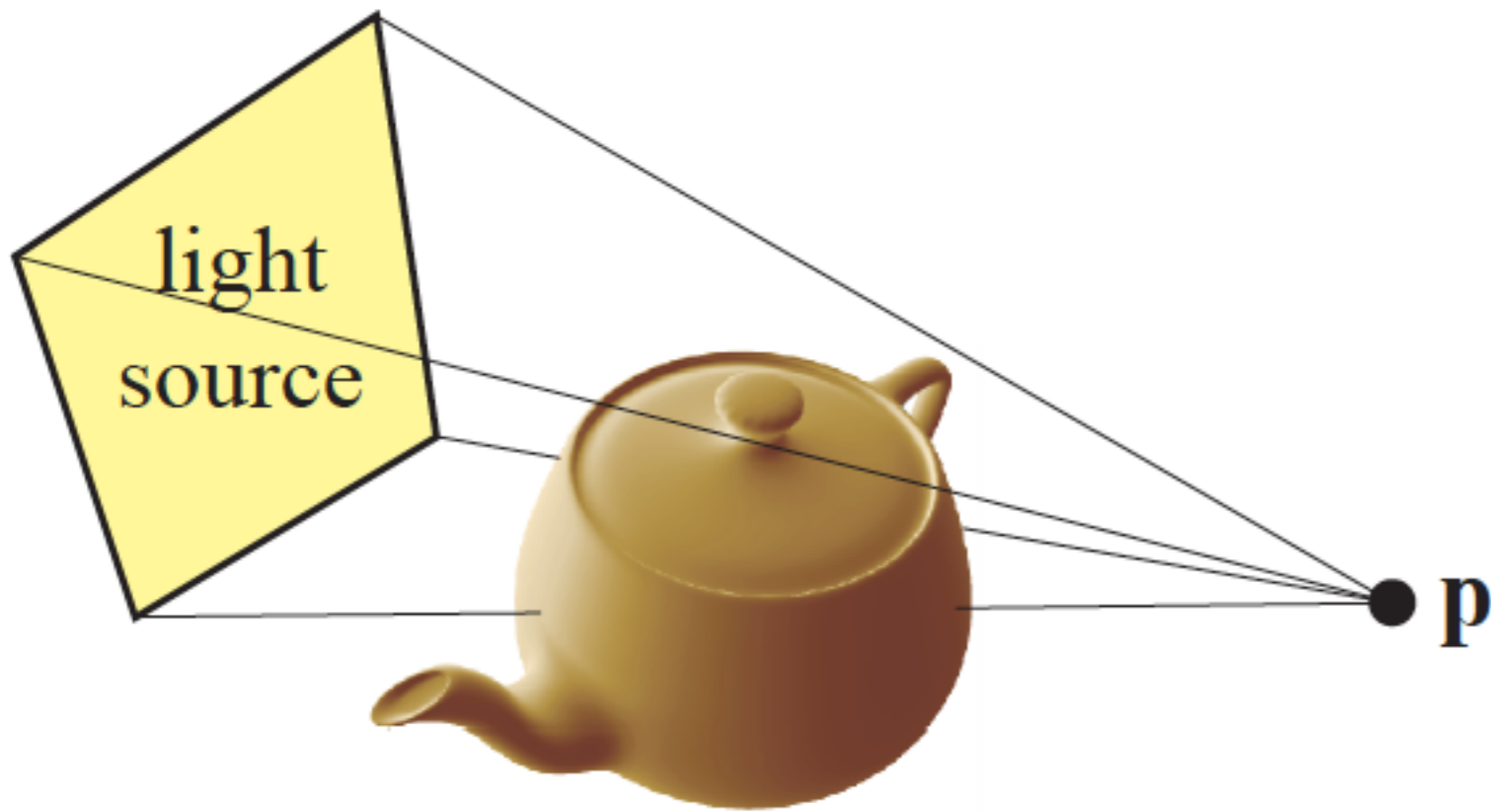


Algorithm for Diffuse Soft Shadows

$$L_{\text{out}} = \frac{\rho(x)}{\pi} \int_{\text{light}} E(y) V(x, y) \frac{\cos \theta_y}{r^2} \cos \theta \, dA_y$$

```
for each visible point x
  Generate N random points  $y_i$  on light source, store
  probabilities  $p_i$  as well (uniform:  $p_i == 1/A$ )
  est = 0
  for each  $y_i, i=1, \dots, N$ 
    Cast shadow ray to evaluate  $V(x, y_i)$ 
    if visible
      est = est +  $E(y_i) \cos(\theta_{y_i}) \cos(\theta) / r^2 / p_i$ 
    endif
  endfor
   $L_{\text{out}}(x) = 1/N * \text{est} * \rho(x) / \pi$ 
endfor
```

Intuitive Picture



(a)



(b)

I've Skipped Ahead of Myself

- Note the use of random numbers
 - We are performing Monte Carlo integration
 - We'll come to that
- **BUT:** Why not write an area light renderer as extra credit for your first programming assignment?
 - After writing code to place the light where you want, you can pretty much translate the pseudocode into actual C++
- Also, note that we haven't talked about non-diffuse surfaces or indirect illumination, yet.

That's It for Today

- Next week: reflectance equation, rendering equation
- Useful reading
 - Pat Hanrahan's slides on radiometry
 - More detail than what we've covered today, **highly recommended**
 - Monte Carlo integration
 - Phil Dutré's Global Illumination Compendium
 - A handy collection of most math that relates to GI
 - Dutré, Bala, Bekaert: Advanced Global Illumination
 - Cohen, Wallace: Radiosity and Realistic Image Synthesis
 - Pharr, Humphreys: Physically Based Rendering