The role of nitrogen-related defects in high-$k$ dielectric oxides: Density-functional studies

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Using ab initio density-functional total energy and molecular-dynamics simulations, we study the effects of various forms of nitrogen postdeposition anneal (PDA) on the electric properties of hafnia in the context of its application as a gate dielectric in field-effect transistors. We consider the atomic structure and energetics of nitrogen-containing defects which can be formed during PDA in various N-based ambients: $N_2$, $N_2^+$, N, NH$_3$, NO, and N$_2$O. We analyze the role of such defects in fixed charge accumulation, electron trapping, and in the growth of the interface SiO$_2$ layer. We find that nitrogen anneal of the oxides leads to an effective immobilization of native defects such as oxygen vacancies and interstitial oxygen ions, which may inhibit the growth of a silica layer. However, nitrogen in any form is unlikely to significantly reduce the fixed charge in the dielectric. © 2005 American Institute of Physics. [DOI: 10.1063/1.1854210]

I. INTRODUCTION

Transistor scaling, which enables continuous increase of performance of integrated circuits, has been generally facilitated by a reduction in the thickness of the gate dielectric in typical metal-oxide-semiconductor field-effect transistors (MOSFETs). However, a further decrease of the thickness of conventional silicon dioxide (SiO$_2$)-type dielectrics leads to an unacceptable rise in the gate leakage current, and hence, power consumption. Several possible solutions are under consideration, but one of the most attractive, which retains a standard MOSFET design, is to replace SiO$_2$ with a material of higher dielectric constant (high $k$). The resulting increase in effective capacitance means that a thicker gate dielectric layer can be used, reducing gate leakage current, while providing comparable performance to a much thinner SiO$_2$ layer. The choice of a specific high-$k$ material is subject to rather strict electrical and process integration requirements eliminating most of the potential candidates, and presently hafnium oxide based dielectrics are considered to be the most promising from a practical standpoint.

In spite of recently reported successes, the performance of high-$k$ transistors requires further improvement to meet the industry needs for most of the potential applications. Most critically, high-$k$ devices suffer from poor channel mobility and instabilities of the threshold potential ($V_T$). It is understood that these drawbacks result from the high density of structural defects in the high-$k$ films, in particular, defects acting as electron traps. These defects were shown to form localized states in the band gap, whose occupancy may vary with the external chemical potential. It was generally expected that a postdeposition anneal (PDA) would reduce the density of intrinsic defects. However, for high-$k$ films deposited on silicon, PDA usually results in a decrease of the effective capacitance of the gate stack. This decrease was attributed to a spontaneous growth of the SiO$_2$ buffer layer between high-$k$ and silicon substrate during the high-$k$ film deposition and subsequent anneals (600–1000 °C), facilitated by the oxygen excess. The low quality of the resulting interfacial SiO$_2$ layer negatively impacts transistor characteristics. In order to suppress the suboxide growth, nitrogen-rich ambients are preferable in PDA. In general, nitrogen incorporation into the Hf-based dielectrics was shown to provide several advantages, such as reducing boron penetration from the $p$-type polysilicon gate electrodes, improving electrical performance, and increasing stability of high-$k$ devices. Besides $N_2$ PDA, several other options were used to increase nitrogen incorporation in Hf-based oxides, including remote nitrogen plasma ($N_2^+$), ammonia (NH$_3$), nitrogen monoxide (NO), and N$_2$O, as well as nitrate- chemical-vapor-deposition processes. However, the lack of understanding of the forms of nitrogen incorporation and its effect on the electronic properties of the dielectric hampers further progress.

In this paper we theoretically investigate the incorporation of $N_2$, N, NO, and NH$_3$ species in different charge states into the ideal and defective HfO$_2$ crystal. Specifics of the structural and chemical composition of real films depend strongly on the deposition and PDA conditions. In particular, a thin film deposited at relatively low temperatures (typically below 500 K) is in a metastable porous low-density state, often characterized by substantial nonstoichiometry. Significant efforts have been recently made to resolve the atomic structure of the deposited films. After PDA in oxygen

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(T > 770 K), hafnia films on Si adopt the monoclinic structure. This is in contrast to zirconia which may crystallize into either a monoclinic or a tetragonal structure depending on the film thickness and stoichiometry. In this paper we leave the problem of polymorphism aside and focus on monoclinic hafnia.

In broad terms, an optimal postdeposition anneal should stipulate

- formation of dense (preferably amorphous) oxide films with controlled thickness, high dielectric constant, and high thermal stability;
- reduction of fixed charge and electron traps in the bulk of the film and at the interface with Si (high electrical stability);
- an effective control over the growth of the SiO₂ buffer layer; and
- inhibition of the diffusion of charged species towards the interface and into the channel region.

In order to assess the effectiveness of different anneals, we assume the following physical picture. After deposition and PDA, a hafnia film is crystallized into the monoclinic structure. After deposition and PDA, a hafnia film is crystallized into the monoclinic or a tetragonal structure depending on the film thickness and stoichiometry. In this paper we leave the problem of polymorphism aside and focus on monoclinic hafnia.

All the electrically active defects in the oxide layer can be qualitatively classified by the position of their levels with respect to the silicon band edges.

(A) Defects whose levels are resonant with the Si conduction band. Under zero electric field and in the thermodynamic equilibrium, these levels are empty. However, such states are available for resonant tunneling at nonzero gate voltage, and thus may serve as electron traps.

(B) Defects whose levels fall into the silicon band gap. The electron occupancy of such defects depends on the position of the Fermi level. These deep defects are responsible for the Fermi-level pinning, and thus, for the high threshold voltages. Also they may contribute into the threshold potential instability and, to some extent, to a fixed charge problem, since the charge relaxation time on such defects may be macroscopically slow.

(C) Defect states resonant with the silicon valence band are expected to be occupied, and, depending on their charge with respect to the lattice, they may become a major source of the fixed charge.

Therefore, the efficiency of a specific PDA could be judged by the integral effect of the resultant nitrogen-containing species on the bulk charge trap density and on the mobility of oxygen, which may occur via the vacancy or interstitial mechanisms.

Although the model outlined above is certainly simplified, it will form a framework for systematizing the effect of various nitrogenous species on the properties of monoclinic hafnia. It can be then refined to include other important effects, e.g., interface diffusion and segregation, impurity clustering, etc.

In Sec. II we give the details of the calculations. The results of the modeling of the effect of different anneal gases are presented in Sec. III and discussion is given in Sec. III.
standard pseudopotentials, as supplied by Kresse and Hafner, were employed for hydrogen, hafnium, nitrogen, and oxygen with the valence charges of 1, 4, 5, and 6, respectively.

The calculations were made in a 96-atom unit cell, which is a $2 \times 2 \times 2$ extension of the 12-atom monoclinic primitive unit cell. We used two $k$ points in the irreducible part of the Brillouin zone, a cutoff energy of 400 eV and the cutoff for augmented charges of 928 eV for atomic relaxation and total-energy calculations. The total energies of the charged systems were corrected for the spurious electrostatic interaction arising from the periodic boundary conditions using the compensating background approach as described in the Appendix. The atomic positions were optimized to the accuracy in atomic forces typically below 0.03 eV Å$^{-1}$, which corresponds to the nominal accuracy of the total energy to within 0.002 eV.

To test the stability of atomic configurations optimized in static calculations and to extract dynamical information, such as diffusion paths and vibrational frequencies, we carried out an extensive set of Born–Oppenheimer molecular-dynamics (MD) simulations using VASP. In these simulations we used $k=0$, a 300-eV energy cutoff, a constant volume, energy, and a number of particles (NVE) algorithm with a time step of 1 fs. This assured a total-energy drift of less than 0.05 eV at $T=600$ K for a typical MD run of 5 ps. The supercell volume in all calculations was fixed to its 0 K theoretical value.

For each charge state $q$ of a candidate defect ($D$) we first determine its geometric structure and formation or incorporation energy $[G(D^q)]$ using the static DFT calculations. Given the macroscopically long defect diffusion and charge relaxation times, we believe that the defect equilibrium free energies do not necessarily reflect relative concentrations of various defects (even if the Fermi level and atomic chemical potentials were well defined). Thus, we do not discuss free energies, but rather assume initially that all energetically stable charge states are possible, and then discuss most probable charge states considering various defects at equilibrium.

The position of defect electrical levels with respect to the band edges of hafnia and silicon determines the stability of a defect in a particular charge state as well as its ability to trap or release an electron. First, we calculate the vertical and relaxed defect ionization energies $[I(D^q)]$ and vertical electron $[\chi_e(D^q)]$ and hole $[\chi_h(D^q)]$ affinities defined as the excitation energies between the defect states and the corresponding band edges of HfO$_2$. These quantities explicitly depend on the defect’s charge state, and their calculation involves combination of the total energies of the system in different charge states, as proposed in Ref. 14 and outlined in the Appendix. Next, we align the calculated electrical levels of defects with the silicon bands using experimental band offsets between bulk HfO$_2$ and silicon measured using internal photoemission. In this approach we neglect the effect of band bending near the interface on the position of the electrical levels of defects and their trapping capability.

Towards the full picture of possible products of incorporation of nitrogen, we examine all possible dissociation channels for nitrogenous molecular species in hafnia matrix. To quantify this, we consider the energetics of solid-state reactions of the type $AB \rightarrow A + B$, as described in the Appendix [Eq. (A2)]. In further discussion we treat a molecular defect $AB$ as thermodynamically unstable if its dissociation into the products $A$ and $B$ is exothermic.

III. RESULTS OF CALCULATIONS

As discussed previously, nitrogen-based PDA can be performed using a variety of gas sources (ambients), and depending on the chemical composition, pressure, and temperature, different products may occur in the bulk film. Here we consider each PDA ambient in turn, and predict the likely resultant defects and their effects on the properties of the oxide.

A. Molecular nitrogen

1. $N_2$ incorporation

The experimental dissociation energy of a $N_2$ molecule in the gas phase is $\sim 9.9$ eV (Ref. 36) (10.0 eV in our DFT calculations). Thus, no $N_2$ dissociation is likely to occur at the surface, and molecular nitrogen is expected to diffuse inside the bulk oxide. Indeed, as we show below, even trapping of extra electrons or interaction with oxygen vacancies does not lead to a spontaneous dissociation of $N_2$ molecular species inside the oxide.

The equilibrium configuration of the neutral interstitial nitrogen molecule is shown in Fig. 2. The incorporation energy for this configuration with respect to $N_2$ in the gas phase is $\sim 3.0$ eV per nitrogen atom. It is seen in Figs. 2 and 3(a) that the interstitial $N_2$ does not form a bond with the lattice oxygen but rather incorporates in the interstitial space near the threefold-coordinated oxygen site. This is in contrast with the $O_2$ molecule, which makes a covalent bond with the lattice anion.

The interstitial $N_2$ molecule has a positive affinity to two electrons (defect electron affinities are given in Table I). The localization of the first extra electron on the $N_2$ interstitial ($N_2^-$ radical) results in the outward relaxation of the nearest-neighbor oxygen ions (cf. O–N distance of 1.96 Å in $N_2^-$.)

![Fig. 2. Structure of neutral nitrogen interstitial molecule in hafnia. The ions are color coded as follows: white—Hf, grey—O, black—N.](image-url)
and \( \sim 2.20 \, \text{Å} \) in \( \text{N}_2^- \)). The corresponding relaxation energy is \( \sim 1.2 \, \text{eV} \). The second extra electron is also strongly localized on the \( \text{N}_2^- \) molecular ion. This further increases the \( \text{O}--\text{N} \) distance to 2.34 Å with a relaxation energy of 0.6 eV with respect to the \( \text{N}_2^- \) geometry. Interestingly, a hole (an absence of the electron) in \( \text{HfO}_2 \) will not localize on the \( \text{N}_2 \) interstitial, owing to the fact that the last occupied orbital of the molecule is well below the valence-band maximum (VBM).

2. Thermodynamic considerations on the likely charge states

We have established that interstitial nitrogen molecules may have multiple charge states, whose occurrence at thermodynamic equilibrium is defined explicitly by the electron chemical potential. The latter depends not only on the external potential but also on the concentrations and electrical levels of all other defects present in the lattice. In this case, the problem of the possible defect charge states may be evaluated by considering the relative electron affinities of various defects, and answering the question: given the fixed number of electrons, on which of the defects they are more likely to reside? This question can be resolved by considering the electron exchange reactions between the pairs of infinitely separated defects, as presented in Table II.

Consider for example the oxygen Frenkel pair (an interstitial atom and the vacancy). It is evident from reactions 1 and 2 (Table II) that in the overall neutral \( \text{m-HfO}_2 \) the zero-temperature equilibrium state corresponds to the doubly positively charged vacancies and doubly negatively charged interstitial oxygen atoms. Next, consider \( \text{N}_2 \) interstitial molecules. Reactions 3–6 (Table II) suggest that they are more electronegative than anion vacancies. Therefore, in oxygen-deficient films (high concentration of vacancies) nitrogen molecules will be predominantly doubly negative, while the vacancies remain doubly positive.

In the case of oxygen excess (large concentrations of interstitials), the relative charge state is defined by the energy balance in the reactions 11–13 (Table II). It follows that interstitial oxygen ions are more electronegative than nitrogen molecules. However, as discussed above, \( \text{N}_2^+ \) is not stable, so nitrogen interstitial molecules will remain largely neutral in this case.

Finally, reaction 21 (Table II) suggests that neutral and doubly negative \( \text{N}_2 \) interstitials are only marginally preferable over the \( \text{N}_2^- \).

The energetics of the electron exchange reactions considered in Table II allows us to narrow down the range of relevant association/dissociation reactions between various pairs of defects considered below.

3. \text{N}_2 reactions with interstitial oxygen species

First, we observe that the interstitial oxygen molecules (\( \text{O}_2 \)) are either marginally stable or unstable in any charge state (reactions 1–4, Table III). Therefore, we conclude that excess oxygen is present only in the form of atomic intersti-
interstitials. As demonstrated in Refs. 14 and 37–39, an interstitial oxygen atom forms a dumbell-type configuration in silica, zircon, zirconia, and hafnia where an oxygen atom effectively incorporates into the Me–O–Me bond (Me is Si, Zr, or Hf ion) forming a Me–O–O–Me configuration with an O–O covalent bond (1.5 Å in HfO2).

Second, it follows from the calculations that both N2 and oxygen interstitials may accept charge states 0, −1, and −2 with respect to the lattice (Table I). Their likely association product, the N2O interstitial, is stable only in charge states (+2, +1, and 0). Next, it follows from the electron exchange reactions shown in Table II (11–13) that oxygen interstitials are more electronegative than nitrogen molecules. Therefore, relevant reactions involving N2 and O must have nitrogen molecules in the charge state that are not more negative than that of the oxygen. Disregarding also reactions involving unstable initial or final charge states leaves only one possible association reaction (reaction 5, Table III), which is endothermic. Therefore, the formation of neutral N2O interstitials is unfavorable. Similarly, it is kinetically unlikely that interstitial NO is formed from N2 molecules, since all reactions involving N2 dissociation (e.g., reaction 6, Table III) are strongly endothermic. The fact that the N2 molecules do not bond to the interstitial oxygen atoms suggests that molecular nitrogen is ineffective in inhibiting diffusion of highly mobile oxygen interstitials15 and in preventing them from migration towards the interface. This finding is consistent with the experimental evidence that oxygen-abundant deposition techniques lead to the formation of the SiO2 buffer layer at the HfO2/Si interface, and that the N2 PDA does not significantly affect its thickness.8,9

**4. N2 reactions with oxygen vacancies**

In the case of substantial oxygen vacancies concentration in the film, the N2 interstitial species can interact with the vacant oxygen sites and passivate them. Based on the previous calculations,14,16 we assume three-coordinated oxygen vacancies to dominate. We consider the stability of nitrogenous species in the three-coordinated anion lattice sites with respect to the infinitely separated interstitial species and the oxygen vacancy. Furthermore, we recall that nitrogen interstitial molecule is more electronegative than the oxygen vacancy (see Table II) and discuss reactions involving doubly charged vacancies (V++2) as the most thermodynamically probable. The corresponding reaction energies are summa-

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**TABLE II.** Electron exchange reactions for defects in m-HfO2. The energies are calculated in the assumption of infinitely separated defects. E > 0 indicates exothermic reaction along the arrow.

<table>
<thead>
<tr>
<th>No.</th>
<th>Reaction</th>
<th>Energy (eV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>O0+V0 ⇒ O0 + V0</td>
<td>1.1</td>
</tr>
<tr>
<td>2</td>
<td>O0+V0 ⇒ O+0 + V0+</td>
<td>2.4</td>
</tr>
<tr>
<td>3</td>
<td>N02+V0 ⇒ N02− + V2+</td>
<td>0.5</td>
</tr>
<tr>
<td>4</td>
<td>N02+V0 ⇒ N02− + V2+</td>
<td>0.7</td>
</tr>
<tr>
<td>5</td>
<td>N02+V0 ⇒ N02− + V2+</td>
<td>0.1</td>
</tr>
<tr>
<td>6</td>
<td>N0−+V0 ⇒ N0− + V0+</td>
<td>0.6</td>
</tr>
<tr>
<td>7</td>
<td>N+0 + V0 ⇒ N0 + V0+</td>
<td>1.3</td>
</tr>
<tr>
<td>8</td>
<td>N0+V0 ⇒ N0 + V0+</td>
<td>1.4</td>
</tr>
<tr>
<td>9</td>
<td>NH2+ + V0 ⇒ NH2+ + V0+</td>
<td>1.5</td>
</tr>
<tr>
<td>10</td>
<td>H+ + V0 ⇒ H+ + V0+</td>
<td>−0.4</td>
</tr>
<tr>
<td>11</td>
<td>N2− + V0 ⇒ N1− + O0</td>
<td>−0.5</td>
</tr>
<tr>
<td>12</td>
<td>N2− + O0 ⇒ N2+ + O−</td>
<td>1.2</td>
</tr>
<tr>
<td>13</td>
<td>N2− + O0 ⇒ N2+ + O−</td>
<td>1.7</td>
</tr>
<tr>
<td>14</td>
<td>N0+O0 ⇒ N0 + O0</td>
<td>−0.2</td>
</tr>
<tr>
<td>15</td>
<td>N0+O0 ⇒ N0 + O0</td>
<td>0.3</td>
</tr>
<tr>
<td>16</td>
<td>N+O0 ⇒ N0 + O0</td>
<td>0.3</td>
</tr>
<tr>
<td>17</td>
<td>N+O0 ⇒ N+ + O0</td>
<td>0.6</td>
</tr>
<tr>
<td>18</td>
<td>N+O0 ⇒ N+ + O0</td>
<td>1.2</td>
</tr>
<tr>
<td>19</td>
<td>2V0 ⇒ V0 + V0</td>
<td>0.3</td>
</tr>
<tr>
<td>20</td>
<td>2O0 ⇒ O0 + O0</td>
<td>0.6</td>
</tr>
<tr>
<td>21</td>
<td>2N0+ ⇒ N0+ + N0+</td>
<td>0.1</td>
</tr>
<tr>
<td>22</td>
<td>2N0+ ⇒ N+ + N0</td>
<td>0.1</td>
</tr>
<tr>
<td>23</td>
<td>2NH2+ ⇒ NH2+ + NH2</td>
<td>2.8</td>
</tr>
<tr>
<td>24</td>
<td>2H+ ⇒ H+ + H+</td>
<td>2.7</td>
</tr>
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</table>

**TABLE III.** Energetics of the association reactions of nitrogen and the interstitial oxygen in m-HfO2. E > 0 denotes an exothermic reaction along the arrow.

<table>
<thead>
<tr>
<th>No.</th>
<th>Reaction</th>
<th>Energy (eV)</th>
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<tr>
<td>1</td>
<td>2O0 ⇒ O2</td>
<td>−1.0</td>
</tr>
<tr>
<td>2</td>
<td>O4− + O− ⇒ O3−</td>
<td>−0.3</td>
</tr>
<tr>
<td>3</td>
<td>2O− ⇒ O2−</td>
<td>0.7</td>
</tr>
<tr>
<td>4</td>
<td>O4− + O− ⇒ O2−</td>
<td>0.0</td>
</tr>
<tr>
<td>5</td>
<td>(N2)+02− ⇒ (N2)02-</td>
<td>−0.9</td>
</tr>
<tr>
<td>6</td>
<td>(N2)+02− ⇒ (NO)+N</td>
<td>−2.1</td>
</tr>
<tr>
<td>7</td>
<td>N02+O0 ⇒ (NO)</td>
<td>1.0</td>
</tr>
<tr>
<td>8</td>
<td>N0+O0 ⇒ (NO)</td>
<td>1.2</td>
</tr>
<tr>
<td>9</td>
<td>N0+O0 ⇒ (NO)</td>
<td>1.6</td>
</tr>
<tr>
<td>10</td>
<td>N0+O0 ⇒ (NO)</td>
<td>1.5</td>
</tr>
</tbody>
</table>
TABLE IV. Energetics of the reactions of some interstitials with a neutral threefold-coordinated oxygen vacancy. The subscript $O$ denotes the species incorporated into the oxygen vacancy. Energies are calculated in the assumption of the infinitely separated vacancy and interstitial in the initial (left-hand side) state. $E > 0$ denotes an exothermic reaction along the arrow. Energies are calculated in the assumption of the infinitely separated products. $E > 0$ denotes an exothermic reaction along the arrow.

<table>
<thead>
<tr>
<th>No.</th>
<th>Reaction</th>
<th>Energy (eV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$N_2^0 + V^+ \rightarrow (N_2)_0^+$</td>
<td>5.1</td>
</tr>
<tr>
<td>2</td>
<td>$N_2^0 + V^{++} \rightarrow (N_2)_0^{++}$</td>
<td>4.7</td>
</tr>
<tr>
<td>3</td>
<td>$N_2^0 + V^+ \rightarrow (N_2)_0^+$</td>
<td>5.4</td>
</tr>
<tr>
<td>4</td>
<td>$N^+ + V^+ \rightarrow N_0^+$</td>
<td>2.2</td>
</tr>
<tr>
<td>5</td>
<td>$N^+ + V^+ \rightarrow N_0^+$</td>
<td>4.3</td>
</tr>
<tr>
<td>6</td>
<td>$N^0 + V^+ \rightarrow N_0^+$</td>
<td>3.3</td>
</tr>
<tr>
<td>7</td>
<td>$N^0 + V^+ \rightarrow N_0^+$</td>
<td>5.7</td>
</tr>
<tr>
<td>8</td>
<td>$N^0 + V^+ \rightarrow N_0^+$</td>
<td>6.1</td>
</tr>
<tr>
<td>9</td>
<td>$(NH_3)^+ + V^0 \rightarrow (NH_3)_0^+$</td>
<td>6.9</td>
</tr>
<tr>
<td>10</td>
<td>$(NH_3)^0 + V^0 \rightarrow (NH_3)_0^+$</td>
<td>6.6</td>
</tr>
<tr>
<td>11</td>
<td>$(H)_0^0 + V^0 \rightarrow H_0^0$</td>
<td>2.7</td>
</tr>
</tbody>
</table>

We note that the reactions involving different charge states of the vacancy can be readily calculated but they are likely to be even more exothermic due to a less stable left-hand side (e.g., reaction 3, Table IV).

B. Atomic nitrogen

As already mentioned, a dissociation of the $N_2$ molecule in the gas phase costs about 10 eV. However, this energy is greatly reduced in the bulk of hafnia crystal. Table V summarizes all possible reactions which would lead to the dissociation of $N_2$. In reactions 1 and 2 (Table V) we see that dissociation of the neutral molecule within the crystal is still endothermic, requiring about 3 eV for both neutral and charged products. The dissociation energy of the $N_2^+_2$ molecular ion, although smaller, is still $\sim$1.6 eV (reactions 3 and 4, Table V). Thus, even without considering the reaction barriers, the dissociation of the nitrogen molecule seems highly unlikely even at elevated temperatures. We also find that, similarly to the $N_2$ interstitial species, the $N_2$ species trapped by oxygen vacancies are stable with respect to dissociation. The corresponding reactions (reactions 5–11, Table V) refer to $N_2$ species in the oxygen vacancy on the left and to one of the product species in the vacancy and another in the interstitial position on the right. As one can see, all dissociation reactions considered in Table V are endothermic, hence, trapping of $N_2$ in the oxygen vacancy does not significantly reduce its dissociation energy. From this, one may infer that after $N_2$ PDA, the concentration of atomic or ionic nitrogen in the bulk film will be negligible.

However, atomic nitrogen can be introduced into the system by the plasma-assisted nitridation $^{18}$ ($N_2^+$), or using metal-nitride precursors in the film deposition. $^{39}$ Therefore, we consider next the energetics of the atomic nitrogen species.

1. $N$ atom incorporation

The interstitial nitrogen atom in its ground-state configuration makes a covalent bond with the threefold-coordinated lattice oxygen. This “dumbbell” structure is similar to that of the interstitial oxygen atom discussed previously in zircon, $^{38}$ zirconia, $^{39}$ and hafnia. $^{14}$ The structure of the defect is shown...
in Fig. 4, and the corresponding electron density is depicted in Fig. 3(b). The electronic ground state is a doublet. This is in contrast with atomic nitrogen in vacuum, whose quasiparticle ground state is almost 3 eV lower than the doublet. An additional electron also fully localizes on the O–N bond with an energy gain of 4.3 eV, increasing the bond length by about 0.1 Å. The relaxation energy after the electron trapping is about 1.2 eV, compared to over 2 eV for interstitial oxygen. In contrast to the N₂ molecule and an atomic oxygen, the atomic nitrogen interstitial has no affinity for a second electron. However, atomic nitrogen is also stable as a positive ion. The local relaxation in this case is distinctly different [Fig. 3(c)]. The nitrogen–oxygen pair is now very electron deficient, and in fact, nitrogen forms a weak bond with a second lattice oxygen (N–O bonds are 1.46 and 1.59 Å). This is accompanied by an energy gain of ~1.2 eV. Removal of another electron forces the nitrogen to a symmetric position, with two strong equivalent bonds (1.40 Å) to lattice oxygen sites and an energy gain of 0.6 eV. Thus interstitial atomic nitrogen may exist in monoclinic hafnia in four stable charge states (+2, +1, 0, and −1).

2. N reactions with interstitial oxygen species

In contrast with the N₂, an atomic nitrogen binds to an oxygen interstitial with an energy gain of around 1.0–1.5 eV depending on the charge state (reactions 7–10, Table III). This process is associated with the breaking of the O–O bond of the dumbbell and formation of the NO₂ quasimolecule [Fig. 5(b)]. The O–O distance is now ~2.2 Å (cf. 1.5 Å in the neutral dumbbell[14]), while the two N–O bonds are ~1.3–1.4 Å. Interestingly, in this configuration there is no clear distinction between the interstitial and the site oxygen—the local symmetry for both oxygen ions remains similar. The energy gain in the reactions of charged oxygen and nitrogen interstitial atoms is even greater (reactions 9 and 10, Table III). Note, however, that in contrast with N₂, the electronegativity of the atomic interstitial is very close to that of the oxygen (reactions 14–18, Table II), so N and O interstitials are expected to have similar charges.

The stability of the interstitial NO molecular species suggests that atomic nitrogen may play an important role in immobilizing fast-diffusing oxygen interstitials, especially O−, thereby inhibiting the growth of the unwanted SiO₂ interfacial layer during anneal.

3. N reaction with oxygen vacancies

In considering reactions with vacancies we recall that the interstitial atomic nitrogen may accept the charge states +2, +1, 0, and −1, the anion vacancy +2, +1, and 0, and the atomic nitrogen substitution +1, 0, and −1. We also take into account the result that the nitrogen interstitial is substantially more electronegative than the vacancy, so the relevant reactions involve nitrogen in a charge state not more positive than that of the vacancy. These considerations leave five relevant reactions shown in Table IV (reactions 4–9). Similarly to N₂, atomic nitrogen passivates the neutral vacancy with an excess energy in the range of 2–6 eV. One should also expect the vacancy passivation by atomic nitrogen to be more effective kinetically due to a higher mobility of atomic versus molecular nitrogen. Notice, however, that for the same reason reactions involving V⁺⁺ will be faster than those with V⁺ or V⁰, as discussed before.

The nitrogen atom incorporation into the vacancy causes marginal outward relaxation of the three nearest Hf ions. A nitrogen atom at a vacancy has the highest electron affinity of any of nitrogen defects (see Table I). The addition of an electron (in other words N− incorporation) causes the N–Hf bond lengths to become smaller than the O–Hf distance in the perfect lattice. The corresponding relaxation energy is about 0.6 eV. For N− substitution the reverse relaxation occurs, i.e., the bond lengths increase, but with a similar energy gain.

An interesting and potentially important feature of both the nitrogen atom and molecule incorporated in an oxygen site is that both species can exist in the negative charge state. This means that the oxygen vacancy with N or N₂ in it can effectively accommodate three electrons and the third electron is strongly bound (see Table I).

On the other hand, our DFT calculations do not predict any electron affinity for the neutral oxygen vacancy in hafnia (see Refs. 14 and 40 for discussion). Thus the formation of negatively charged centers is stipulated by the large electron affinity of nitrogen species. Together with interstitial nitrogen species, these centers can serve as deep electron traps and be responsible for the negative oxide charging.

However, the existence of negatively charged nitrogen species may have also some positive effect as they interact with protons. For example, reaction 5 (Table VI) clearly shows that it is energetically favorable for the interstitial N−...
to trap the proton and form a neutral NH interstitial. Since atomic nitrogen has a high electron affinity, and is likely to exist in the negative charge state, this provides a method for removing excess charge in the oxide due to protons—a problem often seen in experimental studies. However, the small energy gain of $-0.6 \text{ eV}$ for the reaction implies the possibility of some NH dissociation at higher temperatures.

### C. Properties of NO and N$_2$O in hafnia

Our calculations of the interaction of N and N$_2$ with excess oxygen in the oxide have established that a NO interstitial binds with lattice oxygen sites. Reaction 5 (Table III) viewed from right to left clearly suggests that N$_2$O molecules are likely to dissociate into neutral or charged N$_2$ species and oxygen interstitials. It is likely that nitrogen dioxide (NO$_2$) will also dissociate to produce NO and oxygen interstitials. Therefore, PDA using nitric oxide, dinitric oxide, or nitrogen dioxide ambients will not be efficient in trapping oxygen and removing excess charge in the oxide due to protons—a problem often seen in experimental studies. However, we shall see that such states are metastable and more stable dissociated configurations exist. The fact that the molecule is hydrogen rich prompts the possibility that some hydrogen-related defects can be formed. In fact protons have been implicated in hole trapping in hafnia films and at interfaces. Therefore, we pay particular attention to possible dissociation paths of ammonia in hafnia.

In contrast to the molecular species discussed previously, ammonia is a nucleophile molecule and it binds to lattice Hf ions. The stable configuration corresponds to the ionic Hf–N bond aligned approximately along (011)-type directions [Fig. 6(a)], with the C$_3$ axis of the ammonia molecule aligned with this bond. The equilibrium Hf–N bond length is approximately 2.1–2.2 Å. The next nearest-neighbor Hf(2) ion lies approximately on the same axis and is separated from the nitrogen core by only 2.5–2.8 Å.

To understand the mechanism of diffusion of ammonia inside the lattice one needs to analyze its vibrations. The molecule’s thermal motion involves primarily four distinct groups of modes: stretching of the Hf(1)–N bond (S), libration of the Hf(1)–N bond (L), rotation of the NH$_3$ around its C$_3$ axis (R), and the ammonia’s so-called “umbrella” mode (U) [Fig. 6(a)]. Two nearly degenerate L-type modes have relatively low frequencies and manifest themselves by large amplitude “swings” of the NH$_3$ molecule, in which the C$_3$ axis of the molecule remains collinear with the Hf(1)–N bond. These swings are coupled to the R-type rotations of similar frequencies, so the directions of the N–H bonds of the molecule may adjust to a local environment. This L-R-type thermal motion remains reversible until the C$_3$ axis is aligned with the Hf(1)–Hf(2) direction. Once the Hf(1)–N–Hf(2) bonds are aligned, the S-mode softens, so a swap between the short and long Hf–N bonds becomes possible. As seen in the inset of Fig. 6(a), such molecular hops are controlled by the S and U vibrations of ammonia and involve only a small nitrogen displacement of under 0.4 Å.

### D. Incorporation, diffusion, and dissociation of NH$_3$

Apart from its usage for PDA of hafnia films, incorporation of ammonia into oxides is an interesting example of a complex molecular defect. We shall start with the assumption that ammonia incorporates into the monoclinic hafnia lattice intact. However, we shall see that such states are metastable and more stable dissociated configurations exist. The fact that the molecule is hydrogen rich prompts the possibility that some hydrogen-related defects can be formed. In fact protons have been implicated in hole trapping in hafnia films and at interfaces. Therefore, we pay particular attention to possible dissociation paths of ammonia in hafnia.

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The activation energy of the umbrella mode is \( \sim 0.1 \) eV (gas phase data\(^{41}\)), so frequent \( \text{NH}_3 \) hops between few shallow minima are readily observed in the MD simulations even at \( T=300 \) K. An alternative mechanism of ammonia hops has transient states between the oxygen-bridged Hf atoms [Hf(1) and Hf(3) in Fig. 6(a)]. This involves direct S-L-type coupling [see inset of Fig. 6(a)] and has a higher activation energy. Despite being fairly frequent (at least one event in 1 ps at \( T=300 \) K), S-U- and S-L-type hops do not contribute to molecular diffusion, since in such hops the molecule does not leave the original HfO\(_2\) interstitial cage.

We have been unable to find a diffusion path for the whole \( \text{NH}_3 \) molecule. In fact, further calculations show that the ammonia molecule in the \( m\)-HfO\(_2\) [Fig. 7(a)] is metastable and dissociates into \( \text{NH}_2^- \) and a proton. The compact (\( \text{NH}_2^-\text{-H}^+ \)) pair is best described as an \( \text{NH}_2^- \) ion replacing an oxygen ion in a three-coordinated site, while the displaced oxygen traps the proton and relaxes towards the volume interstitial position [Fig. 7(b)]. The energy of this configuration is by \( \sim 0.7 \) eV lower than that of the associated molecule. However, the energy barrier between the two configurations is substantially higher than thermal energies. This is reflected by the fact that the molecular \( \text{NH}_3 \) configuration at 300 K is stable during the entire MD run (at least 6 ps). However, at \( T=600 \) K, which is still below usual PDA temperatures, the dissociation occurs typically within 1–2 ps.

Stability of the dissociated configuration [Fig. 7(b)] is stipulated by the fact that the \( \text{OH}^- \) (or \( \text{NH}_2^- \)) bonds are stretched by the large electrostatic potential gradient near the anion site. Dipole fields of the \( \text{NH}_2^- \) and \( \text{OH}^- \) shearing a single site, mutually counterbalance the crystal-field effect, and stipulate stronger proton bonds and local neutrality. Consequently, although the initial \( \text{NH}_2^-\text{-H}^+ \) dissociation between states \( a \) and \( b \) is exothermic, an infinite separation of \( \text{H}^+ \) and \( \text{NH}_3 \) is endothermic by 0.7 eV (reaction 1, Table VI). The latter can be achieved, e.g., by proton diffusion by hopping between the three-coordinated oxygen ions [Fig. 7(b)]. An alternative dissociation path, resulting in the formation of a neutral molecular hydrogen and \( \text{NH} \) (reaction 2, Table VI), is substantially less energetically favorable.

When separated from the proton, the \( \text{NH}_2^- \) radical may change its charge state when an external potential is applied. Our calculations suggest that this molecule can be either positive or negative, while the neutral configuration is thermodynamically unstable at any value of \( E_F \) (reaction 23, Table II). The same applies to hydrogen (reaction 24, Table II), which is only stable as a proton or a negative ion in hafnia (see Refs. 42 and 43 for discussion on hydrogen).

Depending on its charge state, the \( \text{NH}_2^- \) may lead to the formation of a neutral nitrohydrate and a negative or positive hydrogen ion (reactions 3 and 4, Table VI). Both reactions are endothermic by 1.7 and 0.3 eV, respectively. Despite the apparently low dissociation energy, our MD simulations at \( T=500 \) K shows that the \( \text{NH}_2^+ \) ion is stable—indicating that the dissociation barrier may be high.

Depending on its charge state, the \( \text{NH}_2^- \) molecule binds to the lattice quite differently. The \( \text{NH}_2^- \) ion is isoelectronic to the \( \text{OH}^- \) radical. Therefore, as expected, its most stable configuration is similar to the interstitial \( \text{OH}^- \) center, as reported for monoclinic zirconia.\(^{16} \) \( \text{NH}_2^- \) binds to three Hf ions with a bond length of around 2.3 Å [Fig. 1(a)]. In contrast, the \( \text{NH}_2^+ \) ion makes an ion-covalent bond with a three-coordinated oxygen ion (\( \text{O}–\text{N} \) distance is 1.4 Å) and an ionic bond with only one of the cations (\( \text{N}–\text{Hf} \) distance is 2.2 Å) [Fig. 7(b)].

Further dissociation of \( \text{NH}_2^- \) may lead to the formation of NH species. Calculations predict \( \text{NH}^0 \) to be stable, while \( \text{NH}^- \) is unstable with respect to electron donation to the CB, and \( \text{NH}^+ \) is unstable with respect to proton release (reaction 6, Table VI). \( \text{NH}^0 \) molecule forms a dumbbell configuration with a three-coordinated lattice oxygen similar to N interstitial (\( \text{N}–\text{O} \) distance is 1.47 Å). The equilibrium angle \( \text{ONH}^0 \) is 107° but is soft. Finally, dissociation of \( \text{NH}^0 \) is energetically unfavorable, as discussed previously (reaction 5, Table VI).

The presented results suggest that the likely final products of ammonia PDA are \( \text{NH}_2^- \), \( \text{NH}^0 \), as well as hydrogen. The latter is stable either as a proton or as a negative ion. The detailed dynamical behavior of hydrogen will be discussed elsewhere. \( \text{NH}_2^- \) and \( \text{NH}^0 \) species are unable to trap interstitial oxygen. This agrees with experimental studies showing an increase in interface SiO\(_2\) thickness during NH \( \text{PDA} \). In addition, \( \text{NH}_2^- \) and \( \text{NH}^0 \) (but not \( \text{NH}_2^- \)) can react exothermally with the existing anion vacancies (see reactions 9 and 10, Table IV). The resultant defects create electronic levels near or inside the valence band of hafnia. Therefore, unlike atomic and molecular nitrogen species trapped in oxygen vacancy, \( \text{NH}_2^- \) and \( \text{NH}^0 \) substitutions are stable in only one charge state.

### IV. DISCUSSION

Our calculations identified the most stable nitrogen-containing species and the corresponding energy levels with respect to the band edges of the monoclinic hafnia. It is revealed that most of the stable nitrogen-contained products (as well as intrinsic defects) may have multiple charge states depending on the availability of the electrons in the system. In the MOS architecture the main source of electrons in the dielectric is the channel silicon and poly-Si or metallic gate. Therefore, to identify the most likely charge states, the calculated electric levels of defects must be aligned with the silicon bands. Such an alignment is illustrated in Fig. 8, where the electric levels are adjusted to the experimental band-gap energy as described in the Appendix, and the ex-

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**Figure 7.** Equilibrium configurations of the \( \text{NH}_2^- \) interstitial: (a) \( \text{NH}_2^- \) and (b) \( \text{NH}_2^+ \).
experimental band offsets are used for the valence and the conduction bands. Here we consider the main effects caused by these defects.

A. Structural effects

Our calculations predict that all the neutral and negatively charged stable nitrogen species (N$_2$, N, NH$_2^-$, NH$_3^-$, and H$^-$) incorporate into oxygen vacancies with a substantial energy gain. However, this process is diffusion limited. Since the diffusivity of N$_2$, NH$_2$, NH$_3^-$, and H$^-$ is unlikely to be high, the process of vacancy passivation by molecular nitrogen or ammonia may be incomplete, leaving significantly nonuniform concentrations of interstitials and anion vacancies. In contrast, atomic nitrogen is expected to be rather more mobile resulting in the more effective passivation of oxygen vacancies. A similar argument applies to the processes involving anion vacancies in charge states +1 and 0. They are significantly less mobile than the bare V$^{++}$ due to the electrons localized inside. Consequently, the time to attain thermodynamic equilibrium might be long, and the substitution by the PDA agent in practical anneals may be incomplete.

B. Electron trap effects

Our calculations put the oxygen vacancy electrical levels into the silicon band gap (Fig. 8), which would make them type-B defects. However, this attribution is a result of our calculation procedure in which the DFT band-gap correction is applied to electron affinities of all defects irrespectively of their origin (see the Appendix). Such approximation may become inadequate for the doubly charged oxygen vacancy whose (unoccupied) electronic state splits down from the CBM due to a strong outward displacement of the three nearest-neighbor hafnium ions. Thus, a vacancy state originates from a hafnia conduction band, and its electron affinity ought to be calculated accordingly. Assuming that the vacancy level must be shifted up rigidly with CBM, one would obtain relaxed and unrelaxed electrical levels V$^{++}$/V$^+$ at 0.5 and 1.3 eV below CBM. These values give a lower limit for the V$^{++}$ vertical electron affinity. For the sake of consistency we retain the values obtained by the defect-independent procedure outlined in the Appendix, but acknowledge that anion vacancies may belong to a type A, i.e., be resonant with the Si CB. Therefore, they may act as shallow traps. Accepting this as a working assumption, the role of nitrogen PDA with regard to the shallow trap problem reduces to the effectiveness of the incorporation of nitrogen species into anion vacancies.

Nitrogen incorporation into the oxygen vacancy sites leads to the lowering of the defect levels, making them less active as electron traps. In this respect, all the considered PDA will reduce the shallow trap concentration, although to a different extent as discussed before.

However, another shallow trap candidate could be a small radius electron polaron in the form of Hf$^{3+}$ ion, similar to the Zr$^{3+}$ centers observed in zirconia. The electron self-trapping if effective may present a serious problem in the high-$k$ MOSFETs. However, our density-functional calculations do not predict this defect as stable, possibly due to the known limitations of local approximations regarding localization problem. Therefore, we leave the problem of small-polaron-assisted trapping for further investigation.

C. Fixed charge effects

Both N and N$_2$ interstitials and substitutions are deep centers, and according to Fig. 8 their relaxed affinities (electrical levels) are all below the VBM of Si, which would make them type-C defects. This means that at equilibrium they ought to have a maximum negative charge. However, such an equilibrium state assumes that the electrons are supplied from the silicon valence band, which is difficult (if not impossible) for two reasons: (1) The effectiveness of the resonant tunneling strongly depends on the overlap between the states involved in the process. Therefore, defects located far away from the interface are ineffective electron traps, even if their energy is resonant with Si VB. (2) Charging occurs predominantly via resonant electron tunneling from the Si VB, i.e., it involves transitions to the unoccupied defect states. These states (shown as unrelaxed levels in Fig. 8) are mostly of type-B. Therefore, most of the nitrogen species are unavailable for a resonant tunneling from the silicon valence band. Hence, they may retain multiple nonequilibrium charge states for a very long time, and thus contribute to either positive or negative charge. The possible exceptions are NO interstitials and N substitutions, whose electrical levels are below the Si VBM, so they will quickly achieve maximum negative charge.

The only definite source of positive fixed charge in our calculations are protons and anion vacancies. With regard to these defects, atomic nitrogen and molecular nitrogen will reduce vacancy concentration, but may themselves produce negative or positive charge states, as discussed above. Ammonia anneal will result in a higher concentration of protons, but it is unclear how much of these will be evacuated during the anneal, so the increase in positive charge is expected with the NH$_3$ PDA.

Finally, we would like to emphasize that high-$k$ materials generally favor charged defect states due to their large polarization energy. This is quantified for m-HfO$_2$ in Table II.
We conclude that nitrogen’s capacity for reducing fixed charge in hafnium oxide is limited. Therefore, the problem of fixed charge build up and \( V_T \) instability is not resolved by PDA. Hinkle and Lukovsky\(^{18}\) reported that bulk only nitridation does not decrease and may even increase fixed charge in the oxide film, which is in qualitative agreement with our calculations.

**D. Growth of the interfacial SiO\(_x\) layer**

We assume that growth of the SiO\(_x\) layer at the interface is controlled by a migration of oxygen towards the interface. Therefore, we considered how various PDA gases interact with oxygen interstitials. Our calculations predict \( N_2 \) does not bond to oxygen interstitial in any charge state (Table III). Therefore, interstitial oxygen is free to diffuse towards the interface. In contrast, atomic N strongly bonds to the interstitial oxygen, forming less mobile NO\(^-\) molecules. As a result oxygen diffusion towards the interface is blocked, thus inhibiting growth of an interfacial SiO\(_x\) layer. This conclusion is consistent with the data on nitrogen remote plasma deposition processing,\(^{18}\) where reduction of interfacial silica growth has been observed.

Ammonia molecules in \( m\)-HfO\(_2\) dissociate spontaneously resulting in the formation of NH\(_x^{+/−}\), NH\(_0\), H\(_x^+\), and possibly H\(_2\) and H\(^-\). Of these products, only protons will effectively bond to the interstitial oxygen ions and exclusively to those in the charge state \(-2\). At the same time, the most mobile charge state of oxygen, O\(^-\),\(^{15}\) does not interact strongly with protons. Therefore, ammonia PDA will not inhibit effectively the growth of the interfacial SiO\(_x\) layer. The same applies to the PDA with nitric oxide.

**E. Accuracy of calculations and future work**

Despite spectacular advances in the \( ab \) \( iniito \) total-energy techniques, the calculations of the relative energies of defects in different charge states are still not routine. Main difficulties arise from the (often interrelated) errors due to the local or semilocal approximations in a density functional and to the effects of periodic boundary conditions used with not sufficiently large supercells. These two approximations lead to an ill-defined zero energy in three-dimensional calculations, spurious electrostatic interactions across the supercells, underestimation of the single-particle energy band gap, etc. Although the resulting energy errors are mostly systematic, the correction terms are usually calculated empirically and must be treated with caution. For example, we calculate the energy correction for the monopole-monopole interaction between charged supercells (see the Appendix). For sufficiently large singly charged supercells and for systems with a large dielectric constant, this correction is small ($\Delta_{\text{mp}} = 0.08 \text{ eV}$ in our calculations). An uncertainty in $\Delta_{\text{mp}}$ is estimated at below 30% and mostly originates from the empirical value of the static dielectric constant and from the higher-order multipole interactions across the supercells. Such an uncertainty in total energy is still well within the accuracy of the DFT calculations. However, when considering a solid-state reaction of the type \( A^B \rightarrow A^{2+} + B^{2-} \), the overall correction term for the energies in the right-hand side is $8\Delta_{\text{mp}}$. This would amount to the uncertainty in the dissociation energy of nearly 0.2 eV.

The calculations of defect ionization potentials and electron affinities involve additional uncertainty related to the band-edge energies. In our calculations we empirically correct for the position of CBM but not for the VBM energy. We also assume that none of the defect levels are pinned to the conduction band. For the oxygen vacancy levels these approximations result in the uncertainty of the order of 0.5 eV, as discussed above. However, these approximations work reasonably well for other defects considered in this paper, so, much smaller energy error is expected. The minimization or even elimination of the discussed uncertainties is just becoming possible with improved density functionals (in particular, those going beyond the local-density approximation), and increased feasibility of calculations of larger systems.

Our calculations suggest that hafnium oxynitride may have certain advantages over HfO\(_2\) as a gate oxide. Due to the multiplicity of the NO oxidation states, this material may form stable amorphous structures with acceptable dielectric properties. Some preliminary results on hafnium oxynitride gates in MOSFET have been recently reported,\(^{46,47}\) but a more systematic study of film composition and electrical properties is required.

In this work we have considered only bulk structures close to their thermodynamic equilibrium. There exists strong experimental evidence\(^{18,19}\) that in certain cases a significant part of the electron traps are located in the bulk of the insulator. However, fixed charge distributed far from the channel is well screened and, therefore, has only limited effect on the channel mobility. So, to understand the processes in the channel, an extension of calculations is required towards systems which include interface effects explicitly. The work in this direction is currently under way. Also, we note that bulk DFT calculations only give an indication of the defect charge states that are thermodynamically possible. Some of these states may or may not be relevant depending on the values of the electron chemical potential. Moreover, as charge transport through the dielectric is generally slow, the actual defect states may be controlled kinetically rather than thermodynamically. Therefore, a credible estimation of the defect concentrations must also include effects of the kinetics of the interface growth and PDA.

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APPENDIX: CALCULATION OF FORMATION AND IONIZATION ENERGIES, AND ELECTRON AND HOLE AFFINITIES

The formation energy of a defect in the charge state $q$ is given by

$$G(D^q, E_F) = E_D^0 - E_0 - E_D^{\text{qas}} + qE_F,$$  \hspace{1cm} (A1)

where $E_D^0$ denotes the total energy calculated for system $X$ at the equilibrium geometry and excess supercell charge $q$ in units of the electron charge $e$, $E_0$ is the energy of the perfect HfO$_2$ crystal in charge state $q$, $E_D^{\text{qas}}$ is the energy of the isolated molecule, and all energies are calculated in the same supercell. Depending on the value of $E_F$, the thermodynamically stable charge state of the specific defect may change. The total energies for the charged supercells were calculated using the compensating uniform background potential method.\(^{34,35}\) The calculated unscreened energy correction for the monopole-monopole interaction in the monoclinic supercell is 1.97 eV. The screened correction was calculated by scaling this value by the isotropic part of the static dielectric constant $\varepsilon_{\text{HfO}_2} = 24$, to give energy corrections $\Delta q_{q} = +0.08$ eV and $4\Delta q_{q} = +0.32$ eV for the singly and doubly charged supercells, respectively. The higher-order electrostatic corrections (dipole-dipole, dipole-quadrupole, etc.) were neglected in our calculations.

Next, we define the reaction energy associated with the solid-state reaction of the type $AB \rightarrow A + B$, as follows:

$$E_{\text{re}} = E_{\text{AB}}^0 + E_0^0 - E_A^q - E_B^q,$$  \hspace{1cm} (A2)

where $Q$, $q$, and $(Q-q)$ are, respectively, the charges of the initial molecular defect $AB$, and of its dissociation products $A$ and $B$, and the energies $E_{\text{AB}}^0$ have the same meaning as in Eq. (A1). The energies of the charged supercells are corrected for the electrostatic interactions, and the energy of a perfect HfO$_2$ supercell, $E_0^0$, is added in order to avoid double counting. Note that $E_{\text{re}}>0$ indicates an exothermic reaction from left to right.

In order to study stable charged defect states and the possible role of defects in photo- and thermostimulated processes, as well as in electronic devices, one needs to know the electron affinities and ionization energies of the defect states with respect to the bottom of the conduction band of hafnia and to other electron or hole sources, such as silicon. To achieve that, we compare total energies of the initial and final systems with the same number of electrons. The main inaccuracy of this approach is related to the underestimation of the band gap in the DFT calculations. This means that the defect states appear to be closer to the valence-band and conduction-band edges in hafnia. The relative error in the energy-level position with respect to the gap edges depends on a defect and is impossible to establish without proper calibration using the experimental data.

Defining the absolute value of the defect ionization energy $I_p(D^q)$ as the vertical excitation energy of an electron from the defect with the charge $q$ to the bottom of the conduction band, we have

$$I_p(D^q) = E_0^0 + E_D^{q+1} - E_0^0 - E_D^q + \kappa 1,$$  \hspace{1cm} (A3)

where the value $E_D^{q+1}$ is calculated for the geometry of the relaxed defect with charge $q$, and $\kappa 1$ is a correction for the position of the bottom of the conduction band. Similarly, we can define the electron affinity of the defect $\chi_e(D^q)$ (i.e., the energy gain when the electron from the bottom of the conduction band is trapped at the defect) as follows:

$$\chi_e(D^q) = E_0^0 + E_B^0 - E_0^0 - E_B^{q+1} + \kappa 2.$$  \hspace{1cm} (A4)

Here the correction $\kappa 2$ can be generally different from $\kappa 1$. One can consider both “vertical” and “relaxed” electron affinities. In the latter case the lattice relaxation after the electron trapping is included in $E_0^{q+1}$. We can also define the hole affinity of the defect $\chi_h(D^q)$, i.e., the energy gain when a free hole is trapped from the top of the valence band to the defect as follows:

$$\chi_h(D^q) = E_0^+ + E_B^0 - E_0^+ - E_B^{q+1} + \kappa 3.$$  \hspace{1cm} (A5)

Again, dependent on whether the lattice relaxation in the final state is included or not, one will obtain different affinities. The vertical hole affinity provides a useful estimate of the position of the defect state with respect to the top of the valence band. One can also verify, that the relaxed affinity is related to the defect’s $q+1/q$ electric level as defined elsewhere (e.g., Ref. 48).

To define the corrections $\kappa 1$, $\kappa 2$, and $\kappa 3$ we use the following considerations: (i) We assume that the main inaccuracy in defining the relative positions of defect states with respect to the band-gap edges is due to unoccupied Kohn–Sham states, and that the underestimated band gap is mainly due to the too low position of the conduction-band minimum. Therefore, we use an approximation that $\kappa 1 = \kappa 2 = \kappa$ and $\kappa 3 = 0$. These conditions are difficult to fully justify without comparison with experiment. (ii) Using these conditions and definitions [Eqs. (A4) and (A5)] it is easy to obtain

$$\chi_h(D^q) + \chi_e(D^{q+1}) = E_s(\text{exp}),$$  \hspace{1cm} (A6)

where both affinities correspond to relaxed final defect states. This condition holds in all calculations, which ensures the consistency of our approach. (iii) We use the experimental value of $E_s(\text{exp}) = 5.68$ eV (Ref. 23) to define the difference

$$\kappa = E_s(\text{exp}) - E_s(\text{theor}),$$  \hspace{1cm} (A7)

and correct the defect ionization potentials and electron affinities. This gives $\kappa = 5.68 - 3.92 = 1.76$ eV, which is used in all calculations.

Although this method is approximate, fixing the value of $\kappa$ allows us to present the results of our calculations in one scale. Another advantage is that, in order to find defect affinities with respect to electrons at the bottom of a silicon conduction band or holes at the top of a silicon valence band, within the same method one can use the experimental value of the band offset with Si. This scale can be changed if a more “accurate” or relevant value for $\kappa$ will be found. This will require only a shift of our predicted values by a constant.
44. V. Ryabchuk, Int. J. Photoenergy 6, 95 (2004).