Computed Three-Dimensional Atomic Force Microscopy Images of Biopolymers Using the Jarzynski Equality

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ABSTRACT: Three-dimensional atomic force microscopy (3D-AFM) has resolved three-dimensional distributions of solvent molecules at solid–liquid interfaces at the subnanometer scale. This method is now being extended to the imaging of biopolymer assemblies such as chromosomes or proteins in cells, with the expectation of being able to resolve their three-dimensional structures. Here, we have developed a computational method to simulate 3D-AFM images of biopolymers by using the Jarzynski equality. It is found that some parts of the fiber structure of biopolymers are indeed resolved in the 3D-AFM image. The dependency of 3D-AFM images on the vertical scanning velocity is investigated, and optimum scanning velocities are found. It is also clarified that forces in nonequilibrium processes are measured in 3D-AFM measurements when the dynamics of polymers are slower than the scanning of the probe.
The globular structure mimics chromosomes in the interphase (Figure 1a). A thin and long probe was used as a model to mimic that used in a recent work; this is long enough to penetrate inside the biopolymer (Figure 1b). The force–distance curves were computed at each x and y position using the Jarzynski equality, and then all the curves were merged to give a 3D-AFM image (see details in the Supporting Information).

Figure 2a shows the simulation system, and Figure 2b indicates an xz-slice of a 3D-AFM image at the center of polymer. Figure 2c is the color key for the image. The vertical scanning or penetration velocity ($v_{scan}$) is 1 μm/s in Figure 2.

The forces between the penetrating probe and the polymer are weakly attractive (approximately −20 pN) when the probe is outside the polymer, originating from the Lennard-Jones force between the probe and polymer in long-range. On the other hand, the forces when the probe is inside the polymer are repulsive and rapidly increase as the probe approaches the mica surface (where the beads comprising the polymer are constrained). These repulsive forces are attributed to the work pushing the polymer away by the probe during its penetration (see Movie S1 for the pushing motion). The most probable
speed \( (v_{\text{mp}}) \) of the beads is calculated by \( (2k_B T/m)^{1/2} \), where \( m \) is the mass of beads. Using an effective mass accounting for viscosity \( (m = 0.2 \text{ mg}) \), the most probable speed is 0.203 \( \mu \text{m/s} \). Since the motion or configurational relaxation of the polymer is thus slower than the penetrating speed, the probe must displace the polymer out of the way during its penetration. In Figure 2b, we can see several vertical lines (for example, \( x = -32.5 \) and \( 50 \) \( \text{nm} \)). The movies in which these lines were observed show that the penetrating probe drags the fiber down for a distance where the lines exist (Movie S3 and Movie S4). The probe was also found to push the same parts of fiber down, while the lines are seen (Figure S1). Accordingly, the vertical lines reflect such “dragging”. This is also because of the slow relaxation of the polymer: there is insufficient time for the polymer to avoid the penetrating probe.

The sliced images of the polymer at various heights are shown in Figure 2d. The heights where the polymer was cut are indicated by planes in Figure 2a. The relevant xy-slices of the 3D-AFM image are shown in Figure 2e. Figure S2 indicates selected parts where fiber structures match 3D-AFM images well, and Movie S5 shows the superimposed movie of Figure 2d,e. Figure 3 indicates that polymer structures are indeed, but not completely, resolved in the 3D-AFM image (Figure S2 and Movie S5). The structure–force correlation is quantified later.

Figure 2f shows slices of the 3D-AFM image computed using thermodynamic integration. In all images, only weak attractive forces \((\approx -15 \text{ pN})\) are seen. In this computation, the probe was stopped at a certain height and the potential energies were sampled and averaged (Movie S2). Most forces acting on the probe, which practically act on the end of the probe, were negative because the polymer and the end of the probe were located in energetically favorable positions during the equilibrium sampling process. This is the reason why attractive forces were observed.

The images computed using thermodynamic integration are completely different from those using the Jarzynski equality, since the work in a nonequilibrium process (pushing away fibers and/or dragging) was not accounted for in thermodynamic integration. Thus, no clear fiber structures are seen. Accordingly, it is significant to simulate 3D-AFM images using the Jarzynski equality in such cases where sample motion is slower than penetration speed, resulting in nonequilibrium work being performed. In other words, forces measured by the AFM experiments in the biological samples whose molecular motions are presumably slower than the probe penetration are not accurately represented by the mean force.

It is known that for certain systems 3D-AFM images (or force–distance curves) change depending on the vertical scanning velocity, and that the free energy profile...
force is in the range 1–100 pN, depending on the measurement conditions, and is <10 pN for the ideal condition in the dynamic mode.30,31 At this velocity, the fiber can avoid the penetrating probe, because the scanning velocity is slower than $v_{\text{mp}}$ and the forces are close to those obtained by thermodynamic integration (Figure 3b). Even at $v_{\text{scan}} = 0.2 \mu m/s \sim v_{\text{mp}}$, the fiber can still avoid the penetrating probe, resulting in weak forces.

As expected from the Maxwell–Boltzmann distribution, the speeds of almost all beads composing the fiber are less than $2.5v_{\text{mp}}$. Accordingly, when $v_{\text{scan}} \geq 0.5 \mu m/s (\sim 2.5v_{\text{mp}})$, the motion of the fiber is slower than the scanning probe (see Movie S7), and a sufficiently detectable force acts when the probe penetrates the polymer. At $v_{\text{scan}} = 0.5 \mu m/s (\sim 2.5v_{\text{mp}})$, we can see some fiber structures in the simulated 3D-AFM image. At $v_{\text{scan}} = 1 \mu m/s (\sim 5v_{\text{mp}})$, the image becomes clearer (Figure 3a and Figure S3). The fiber structures are also observed at $v_{\text{scan}} = 2 \mu m/s (\sim 10v_{\text{mp}})$ and $3 \mu m/s (\sim 15v_{\text{mp}})$, while the forces increase (Figure 3a and Figure S3).

Figure 3b shows the force–distance curves. For approaching curves (red lines), we can see that the forces increase when $v_{\text{scan}}$ is speeded up. On the other hand, the forces computed by using thermodynamic integration (black lines) are always close to the experimental detection limit and those evaluated by the Jarzynski equality at $v_{\text{scan}} = 0.1 \mu m/s$, since, as explained, the motions of beads comprising the fiber are faster than $v_{\text{scan}}$. The force–distance curves during retraction were computed by using the Jarzynski equality and are shown by the blue lines. There is no pushing away motion of fibers and dragging in the retracting process, so the force–distance curves have, as expected, no large peak, and there is almost no dependency on $v_{\text{scan}}$.

When the scanning velocity is in the range $2.5v_{\text{mp}} \leq v_{\text{scan}} \leq 15v_{\text{mp}}$ mainly two peaks are seen at $\sim 160$ and $\sim 360$ nm (Figure 3b, see Figure S4 for all velocities but with different scale). These two peaks (i and ii) originate from dragging and pushing away, respectively (see Figure S4). Thus, they are shared among $v_{\text{scan}} = 0.5 (\sim 2.5v_{\text{mp}})$, $1 (\sim 5v_{\text{mp}})$, and $2 (\sim 10v_{\text{mp}})$ $\mu m/s$ (also at $v_{\text{scan}} = 3 (\sim 15v_{\text{mp}}) \mu m/s$, Figure S4). Figure 3c shows snapshots when the probe feels a strong repulsion. Irrespective of $v_{\text{mp}}$, the probe pushes away the parts of fiber colored in blue and green at the peaks i and ii, respectively. The peak i is broadened because of the dragging of a part of the fiber colored in blue (Figure S4).

Even at $v_{\text{scan}} \geq 4 \mu m/s (\sim 20v_{\text{mp}})$, the faster the $v_{\text{scan}}$ is, the stronger the forces become (Figure 3a, Figures S3 and S4, and Movie S8). The probe, as mentioned, sometimes cuts the polymer, and the 3D-AFM images were computed before such breaks. When changing the contrast (see Figure S3 and Movie S8), the fiber structures are still seen at $v_{\text{scan}} = 4 \mu m/s (\sim 20v_{\text{mp}})$; however, there are some spots of high forces in addition to the fiber. There are cases where peaks in force reflect different fibers, and other cases originate from the dragging (Figure S4). It was found that the dragging increases when $v_{\text{scan}}$ is fast (Figure S5). Another reason for high forces is that the probe pushes downward not only a single fiber but also another one behind it (Figure S6). Therefore, the peaks of forces are not well-separated for each fiber. Accordingly, in the force–distance curve at $v_{\text{scan}} = 4 \mu m/s$ (Figure 3b, see Figure S4 for those at $v_{\text{scan}} = 7.5$ and $10 \mu m/s$), there are several peaks in addition to the two main peaks seen in the range $0.5 \mu m/s \leq v_{\text{scan}} \leq 3 \mu m/s$. When $v_{\text{scan}}$ is $7.5 (\sim 36v_{\text{mp}})$ and $10 (\sim 50v_{\text{mp}})$,

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**Figure 4.** Structure–force correlations at all vertical scanning velocities examined. (a) For $v_{\text{scan}} \leq 3 \mu m/s$. (b) For $v_{\text{scan}} \geq 3 \mu m/s$. (c) Averaged correlation against $v_{\text{scan}}$.
the 3D-AFM images become similar to static noise and the fiber structure is difficult to see (Figure S3 and Movie S8).

The structure−force correlation (C) at each height was evaluated by

\[ C(z) = \frac{1}{A} \int_{\frac{A}{F_{\text{max}}}} \sigma(x, y, z) \frac{F(x, y, z)}{F_{\text{max}}} \, dx \, dy \]

where A, F, and Fmax are the scanned area, forces at each position in 3D space (so the 3D-AFM image), and maximum force in the entire image, respectively. σ is 1 if the position is within 15 nm from the centers of beads and −1 if not, in which the position of the beads was shifted upward by 30 nm since the force is detected approximately 30 nm above the polymer.

At \( v_{\text{scan}} \geq 4 \mu m/s \), forces before the probe cut the polymer were used for the analysis, and the area A was changed according to the number of analyzed force−distance curves.

Figure 4 indicates the dependence of the structure−force correlation on \( v_{\text{scan}} \). Up to \( 3 \mu m/s \), the correlation increases when \( v_{\text{scan}} \) becomes larger (Figure 4a). Further increase of \( v_{\text{scan}} \), however, decreases the correlation because of the static noise (Figure 4b). Accordingly, the 3D-AFM image best matches the polymer coordinates at \( v_{\text{scan}} = 3 \mu m/s \) (∼15 \( p_{\text{mp}} \)) (Figure 4c).

Thus, there exists an optimum velocity range for vertical scan, and the force curve would reflect a rather detailed fiber structure when the scanning velocity is adequately adjusted.

Lastly, a comparison with the experiment in which the 3D organization of cytoskeletal fibers was visualized by 3D-AFM measurements is shown. This is the best example for comparison because both the actual structure and the 3D-AFM image are known. In the 3D-AFM image of cytoskeleton fibers (Figure 3C,D in ref 9), we can see high force regions running up and down in 3D space, reflecting the structure of the cytoskeleton fibers. Note that these images were processed to reduce the forces that originated by dragging. We mimicked the straight fiber structure by increasing the stiffness (Figure 5a) and computed its 3D-AFM image (see Supporting Information for details of the method).

In the successive xy-slices of the 3D-AFM image from higher to lower positions (Figure 5b and Movie S9), regions of high force appear in sequence according to their heights as in the experiments. In the sliced image of lower position, the afterimages of fibers in the higher position appear as weaker forces because of dragging. In the xz slice of the 3D-AFM image (Figure 5c), elongated triangles are visible. This shape reflects the position of fibers and the dragging afterward while the nanoprobe is moving down. The triangular shape is caused by the finite diameter of the probes, which laterally touches the fiber even when it is not perfectly on the center of the fiber. The dragging strength decreases as the probe moves away from the center (Figure S8). These characteristic triangles are also seen in the experimental images before the force reduction process (Figure S8). These characteristic triangles are also seen in the experimental images before the force reduction process (Figure S8). These characteristic triangles are also seen in the experimental images before the force reduction process (Figure S8).

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after laterally moving the fiber. In the experiment, on the other hand, the signal is weak above the fiber and gets stronger as the probe pushes the fiber downward. A plausible explanation is that cytoskeleton fibers in cells are attached to the cell membrane, and thus, the force would become larger while the probe pushes the fiber downward due to the interaction between fiber and membrane. However, such an interaction is not implemented on the simulation. Therefore, for relatively stiff straight fibers, the method developed here shows some qualitative agreement with the experiment, although the force magnitude during dragging is different.

In conclusion, we developed a method to compute 3D-AFM images of biopolymers using the Jarzynski equality. Our simulation demonstrated that 3D-AFM technology is even capable of resolving fluctuating biopolymers; some fiber structures were clearly observed in the simulated 3D-AFM images. This supports previous 3D-AFM measurements observing molecular chains.⁴⁻⁷,⁸ The computed forces increased when the scanning velocity becomes fast, which qualitatively reproduced force-scanning velocity relations in some experiments.⁹⁻²⁶ Moreover, the optimum scanning velocity was found in the range of several to 10 times faster than the most probable speed of the biopolymer. It was found that the use of thermodynamic integration to compute force–distance curves and 3D-AFM images is unsuitable when the motions of the samples are slower than the penetration speed of the AFM probe, because the system is far from thermodynamic equilibrium. It is expected that the motions of biomolecules are relatively slow; thus, the forces measured in the AFM measurements of biomolecules would be forces in a non-equilibrium process rather than the so-called mean force. The method developed here is applicable to various fibers in cells such as DNA and so on by changing parameters such as stiffness, providing an important theoretical base for such experimental measurements. As an example, it was applied for cytoskeleton fibers to be compared with recent experiments.⁹ Another important issue for the near future is to establish a method to convert 3D-AFM images to actual fiber structures in order to utilize 3D-AFM imaging as a tool to reveal structures of biopolymers. For this, AI using machine learning or some image analysis technologies are expected to help.

**ASSOCIATED CONTENT**

- **Supporting Information**
  - The Supporting Information is available free of charge at [https://pubs.acs.org/doi/10.1021/acs.jpcl.2c01093](https://pubs.acs.org/doi/10.1021/acs.jpcl.2c01093).
  - Simulation details and figures showing additional results such as fiber structure comparisons, velocities of beads of the fiber, and force–distance curves (PDF)
  - Movie of probe penetration into the biopolymer (Movie S1) (MP4)
  - Simulation during the thermodynamic integration (Movie S2) (MP4)
  - Force–distance curve at \( x = -32.5 \) nm and a movie of probe penetration (Movie S3) (MP4)
  - Force–distance curve at \( x = 50 \) nm and a movie of probe penetration (Movie S4) (MP4)
  - Superimposed movies of fiber structure and 3D-AFM images (Movie S5) (MP4)
  - 3D-AFM image at \( v_{\text{scan}} = 1 \) µm/s (Movie S6) (MP4)
  - Probe penetrating movies at different scanning velocities (Movie S7) (MP4)
  - 3D-AFM images at different scanning velocities (Movie S8) (MP4)
  - 3D-AFM image of cytoskeleton fibers (Movie S9) (MP4)

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**Author Contributions**


**Notes**

The authors declare no competing financial interest.

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■ ABBREVIATIONS
AFM, atomic force microscopy; 3D-AFM, three-dimensional atomic force microscopy

■ REFERENCES